

# Star formation: protostellar collapse

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# Outline

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## 1. Introduction

## 2. Methods

- AMR vs. SPH

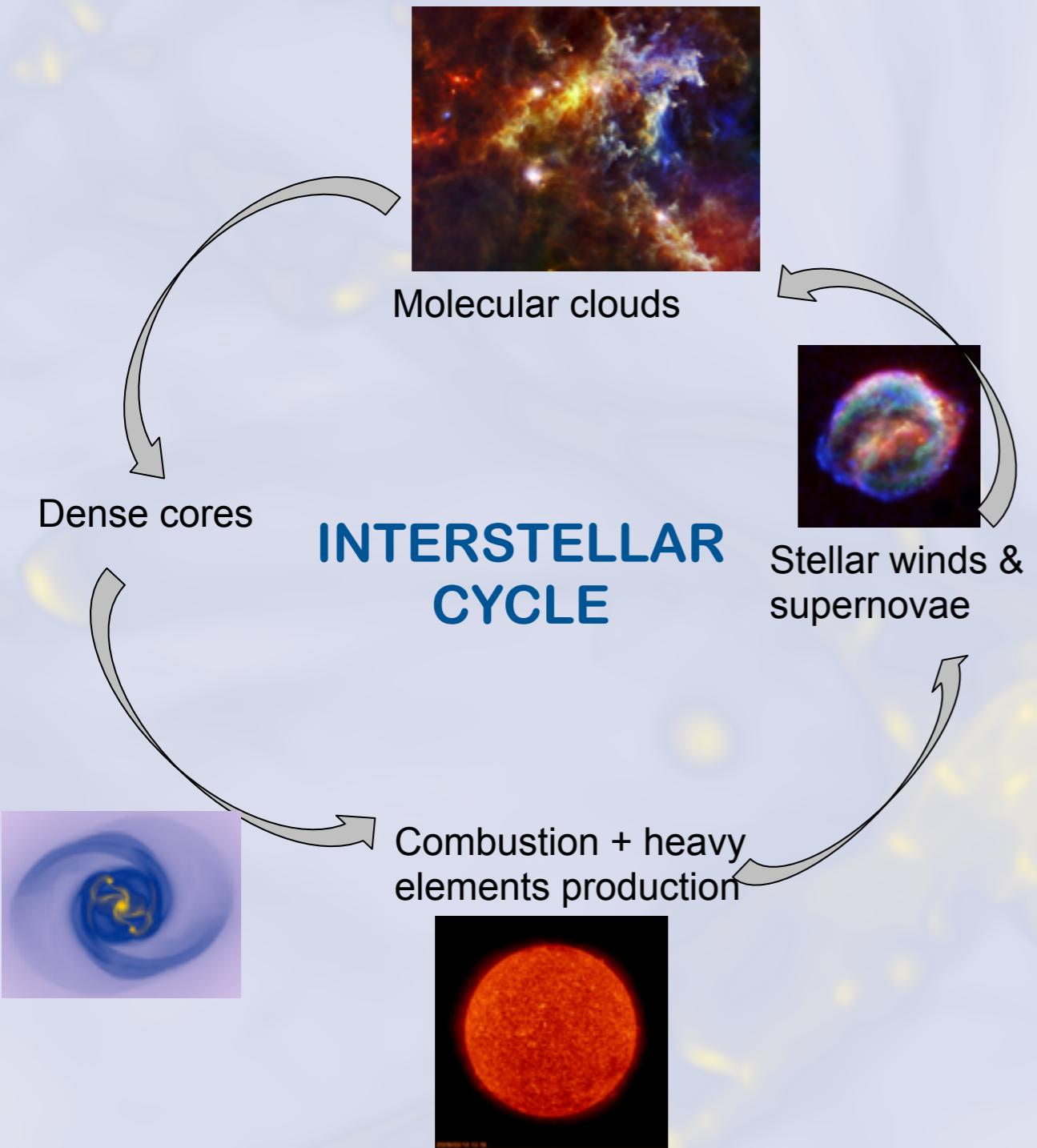
## 3. Low mass dense core collapse

- RHD and RMHD collapse
- Disk formation and fragmentation crisis
- Synthetic observations

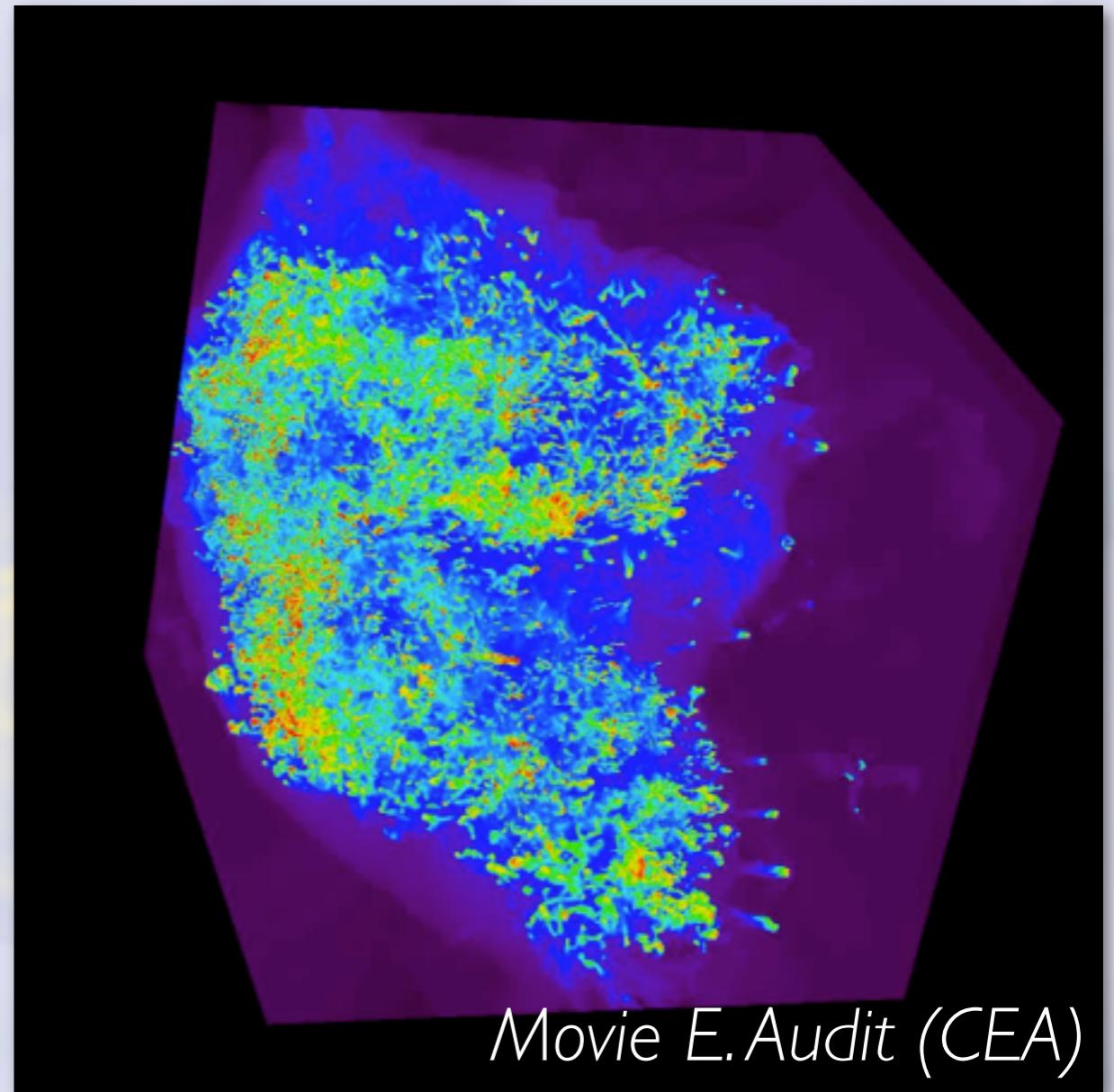
## 4. Massive dense cores collapse

- Early fragmentation inhibition
- Disk & outflow formation

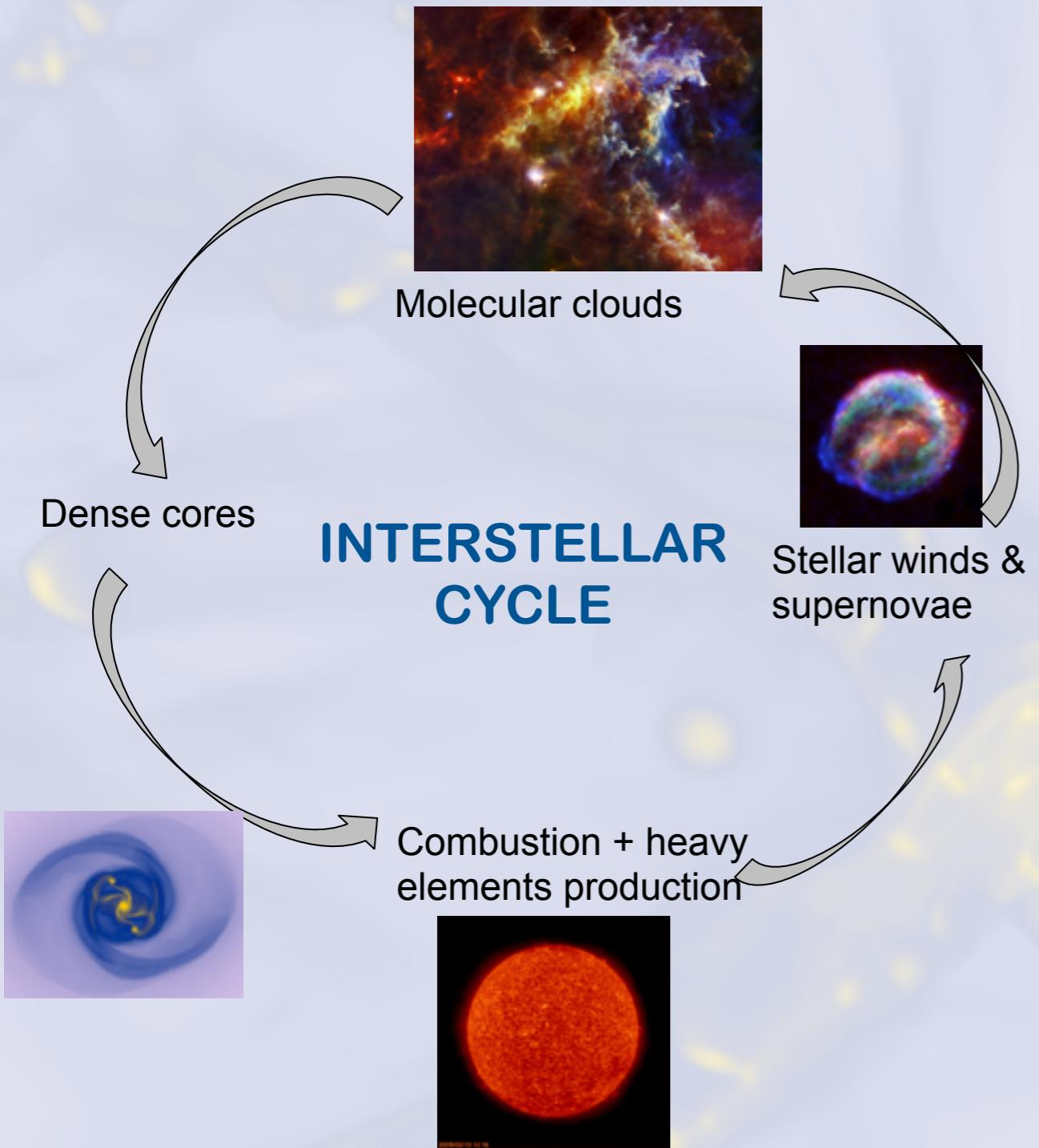
# Why is star formation so important?



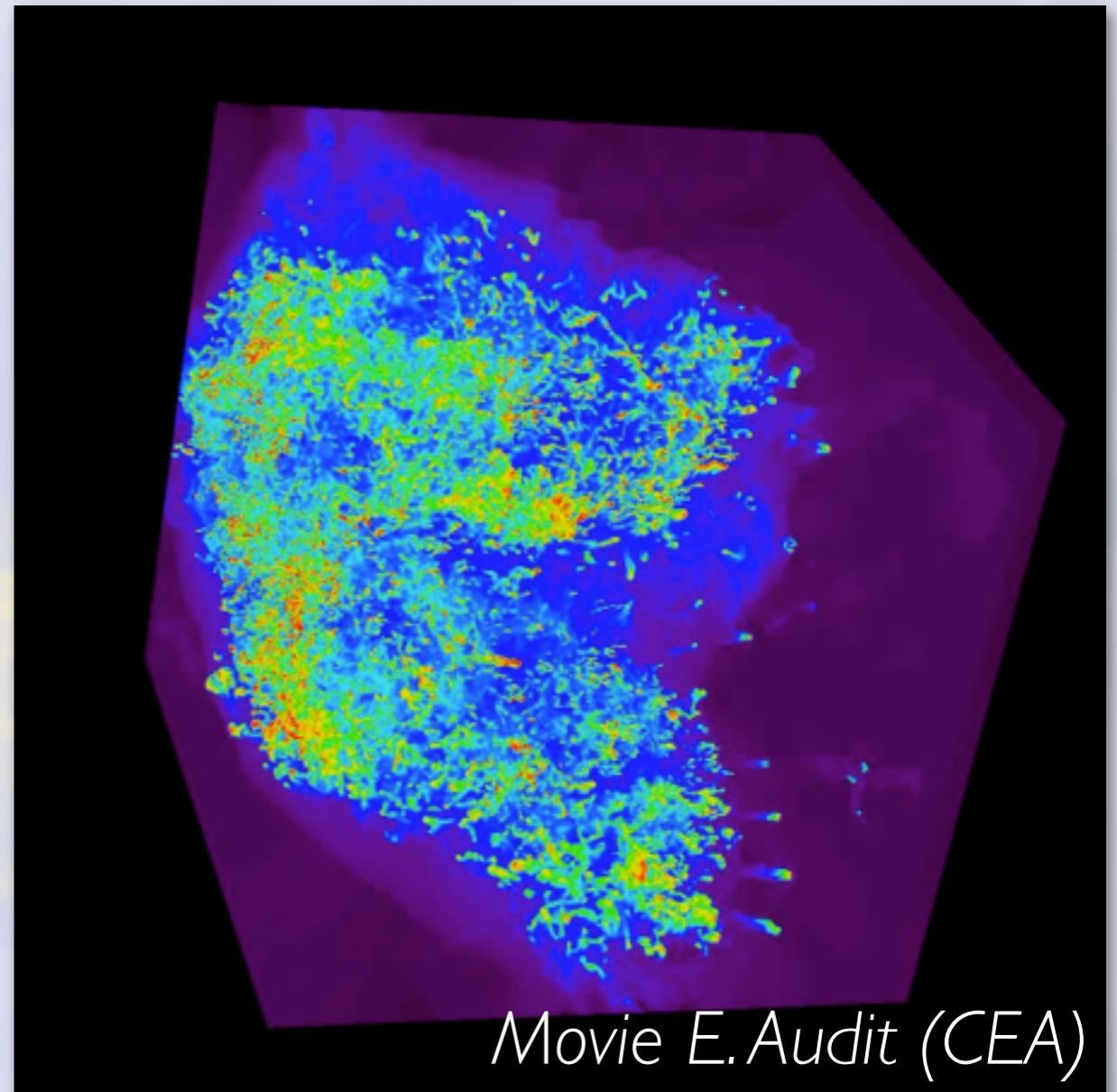
Turbulent molecular cloud



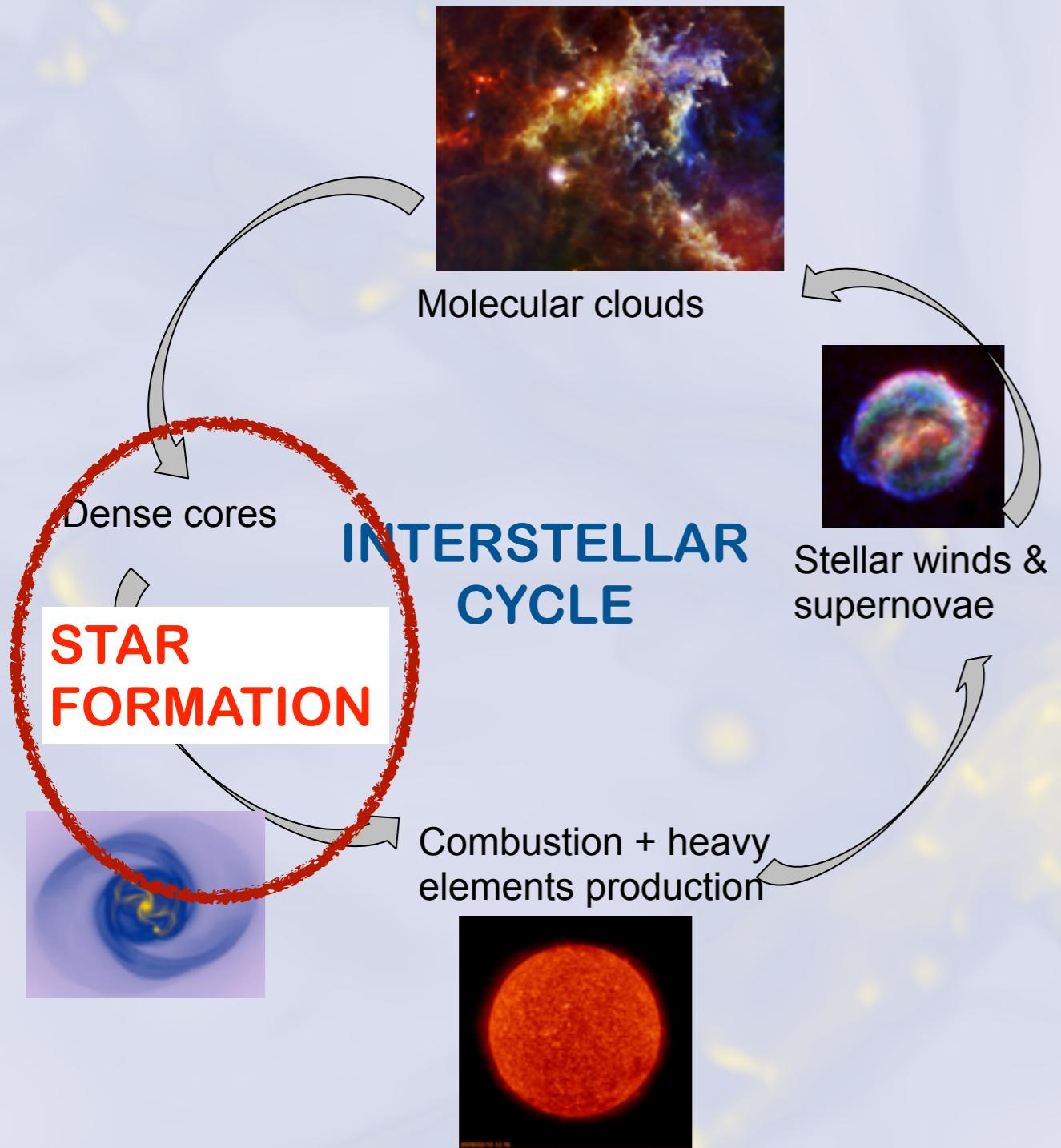
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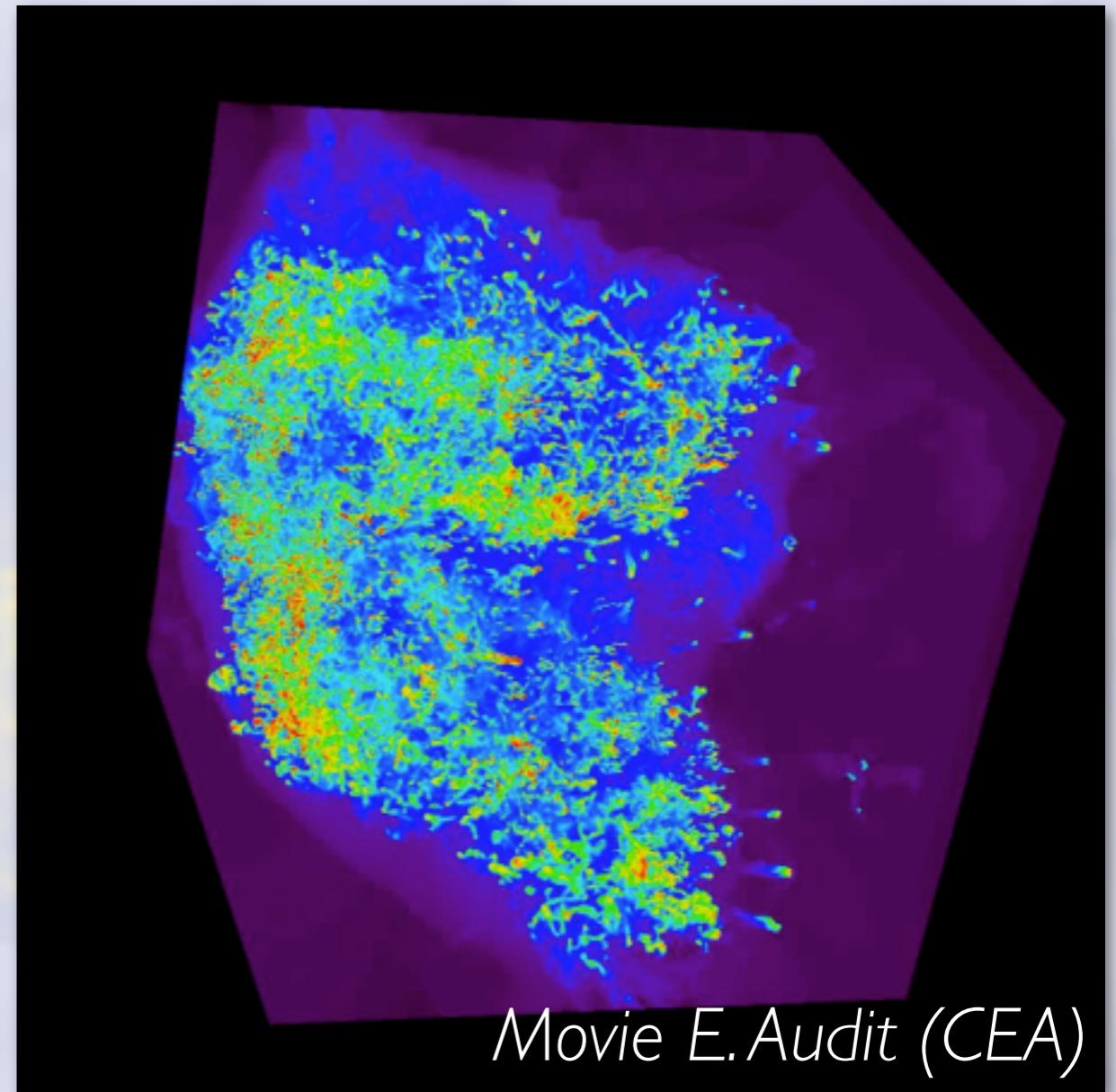
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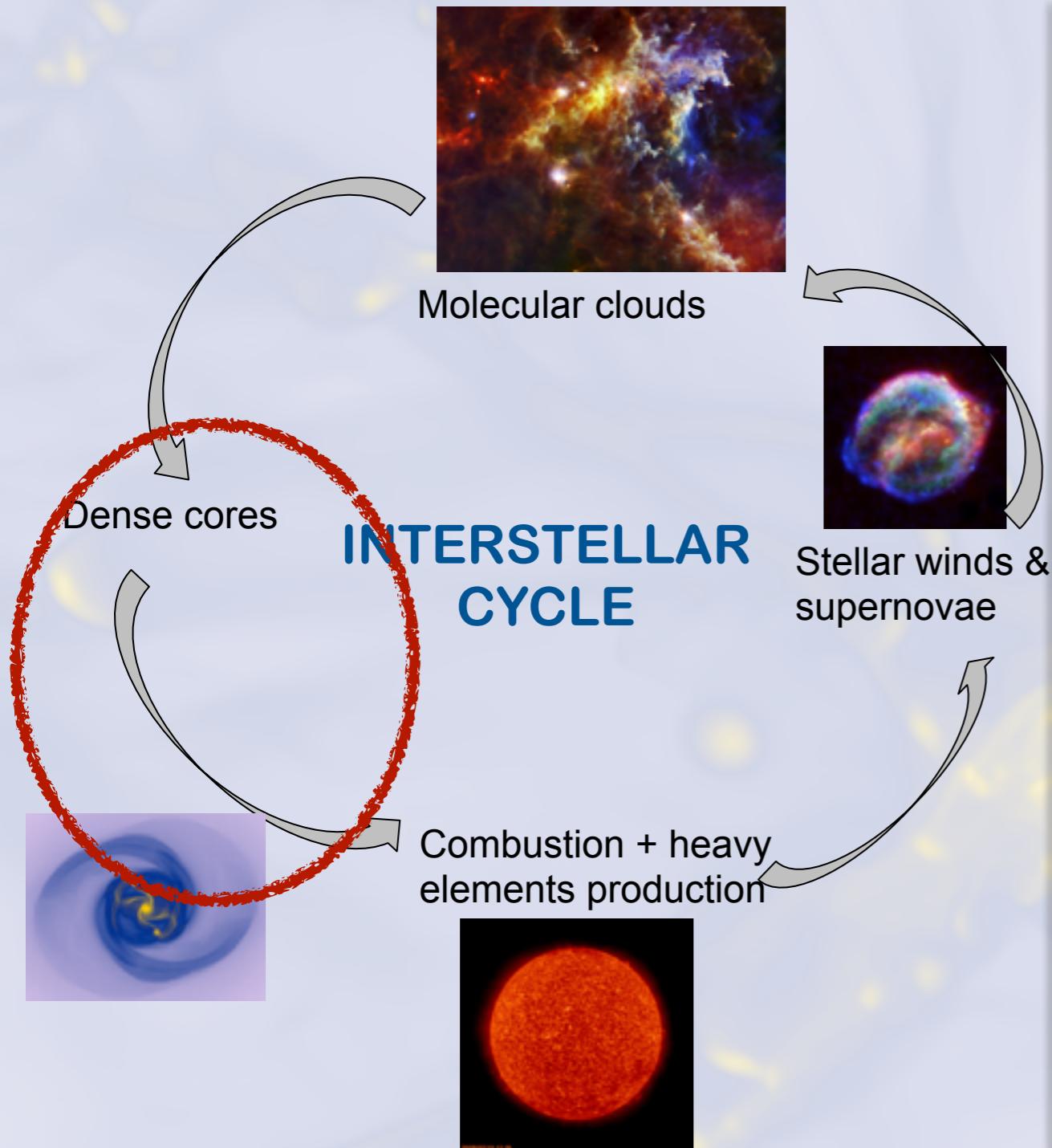
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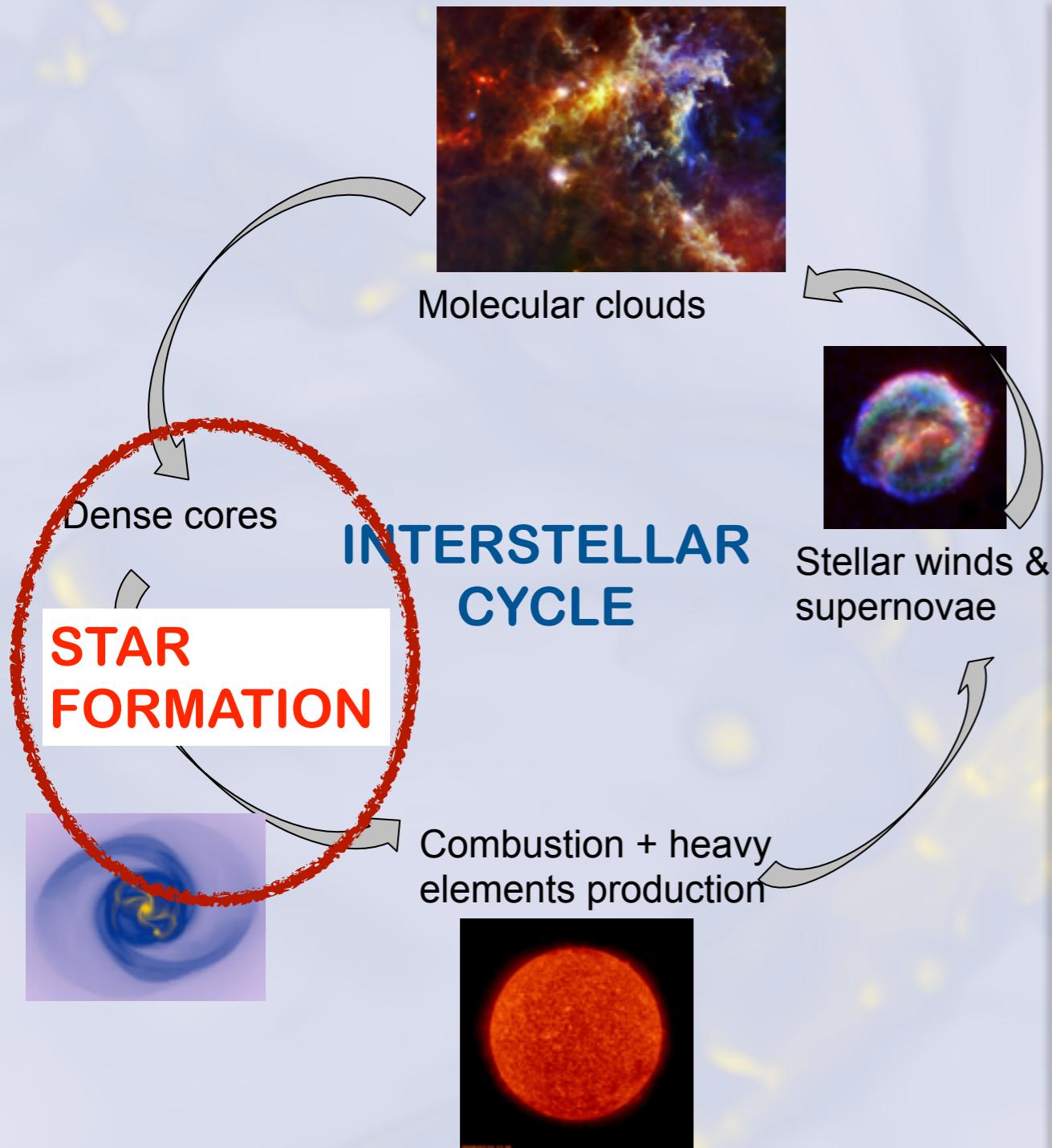


# Why is star formation so important?



- ✓ Very few pbs in astrophysics without link to stars
- ✓ From large to small scales
  - interstellar cycle
  - galaxy formation and evolution
  - planet formation/life
- ✓ A lot of **open questions**, e.g. :
  - angular momentum/magnetic flux
  - disk formation
  - fragmentation, multiplicity, IMF, CMF
  - star/brown dwarf/planet formation
  - massive star formation
- \* Motivation for instrumentation, e.g., **JWST, ALMA & HERSCHEL** <=> **THEORETICAL** support

# Why is star formation so important?

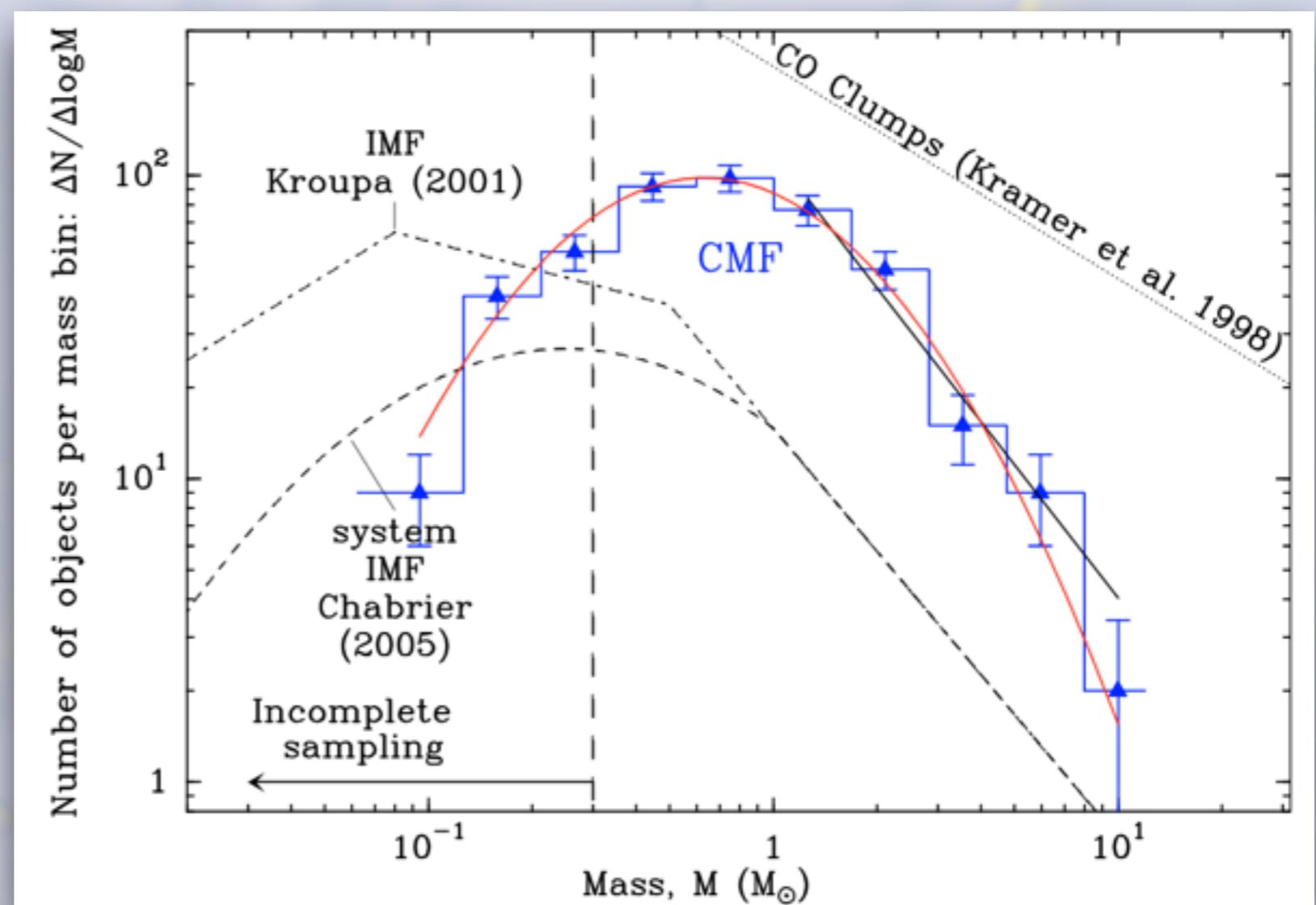


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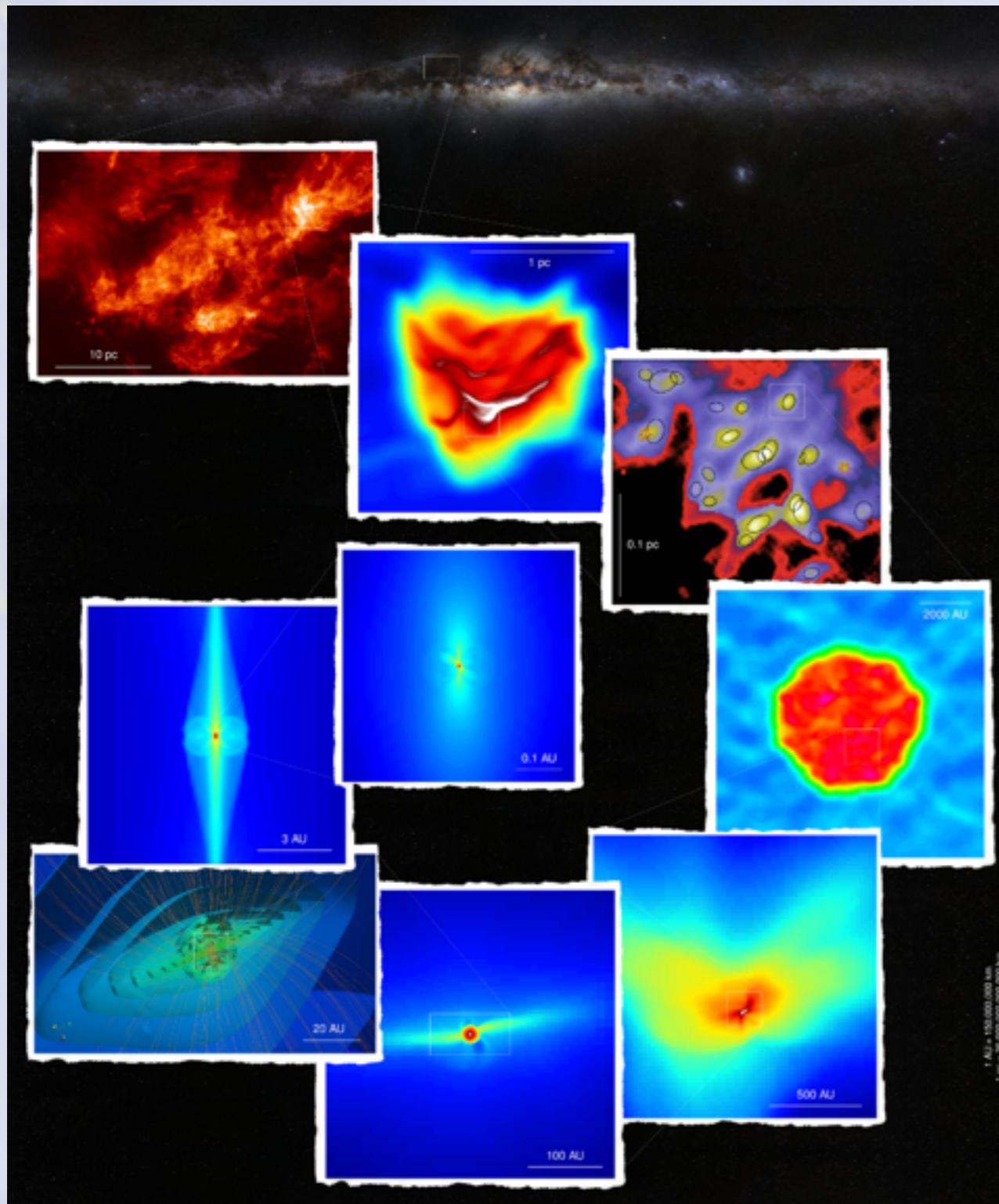
# Dense core formation

- At the sonic scale for the majority
- Dense core are the progenitors of stars
- 1-1 relation between core mass function and initial stellar mass function?

Konyves et al. (2010)  
HERSCHEL Observations



# Star formation: building blocks & challenge

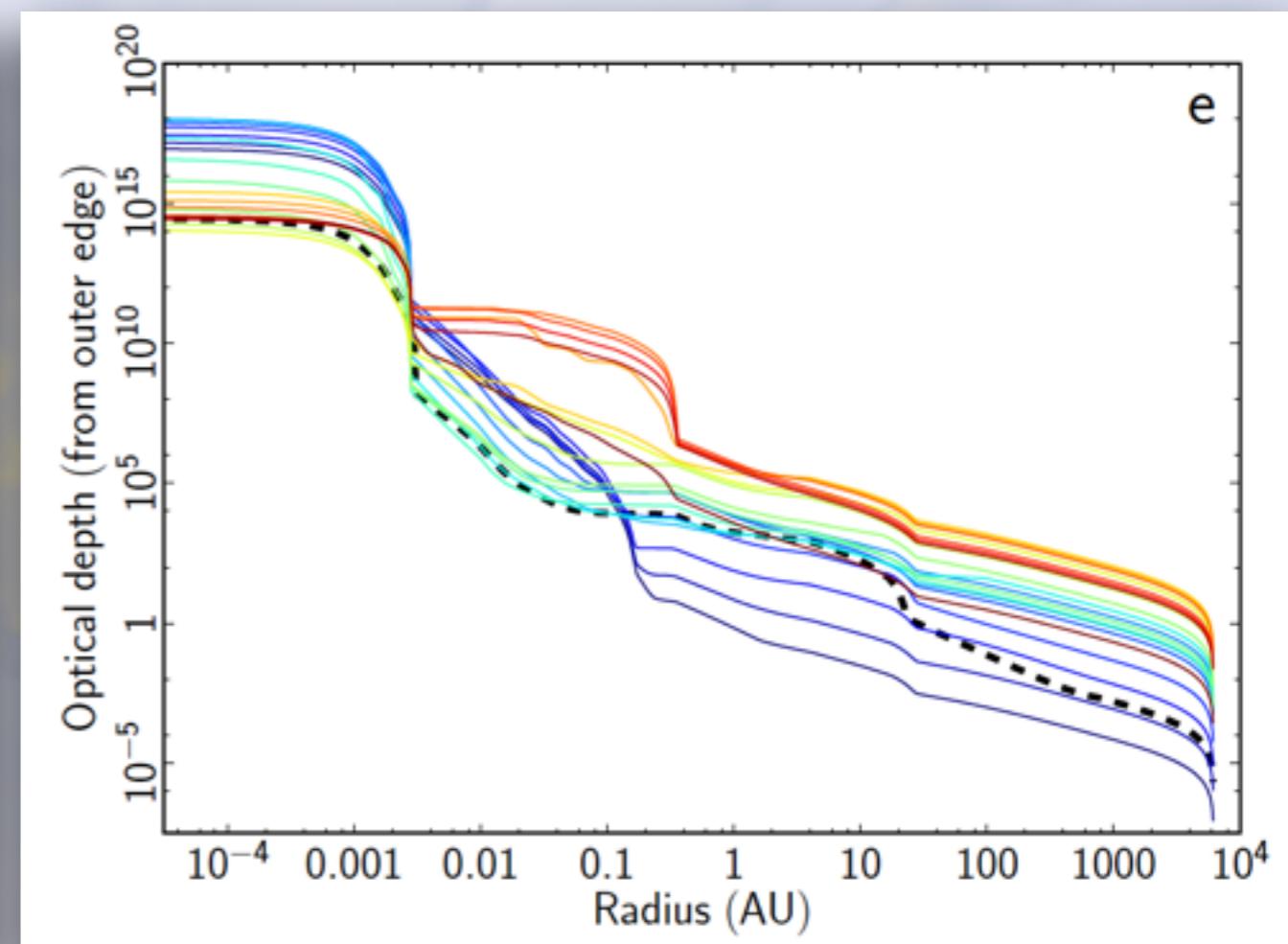
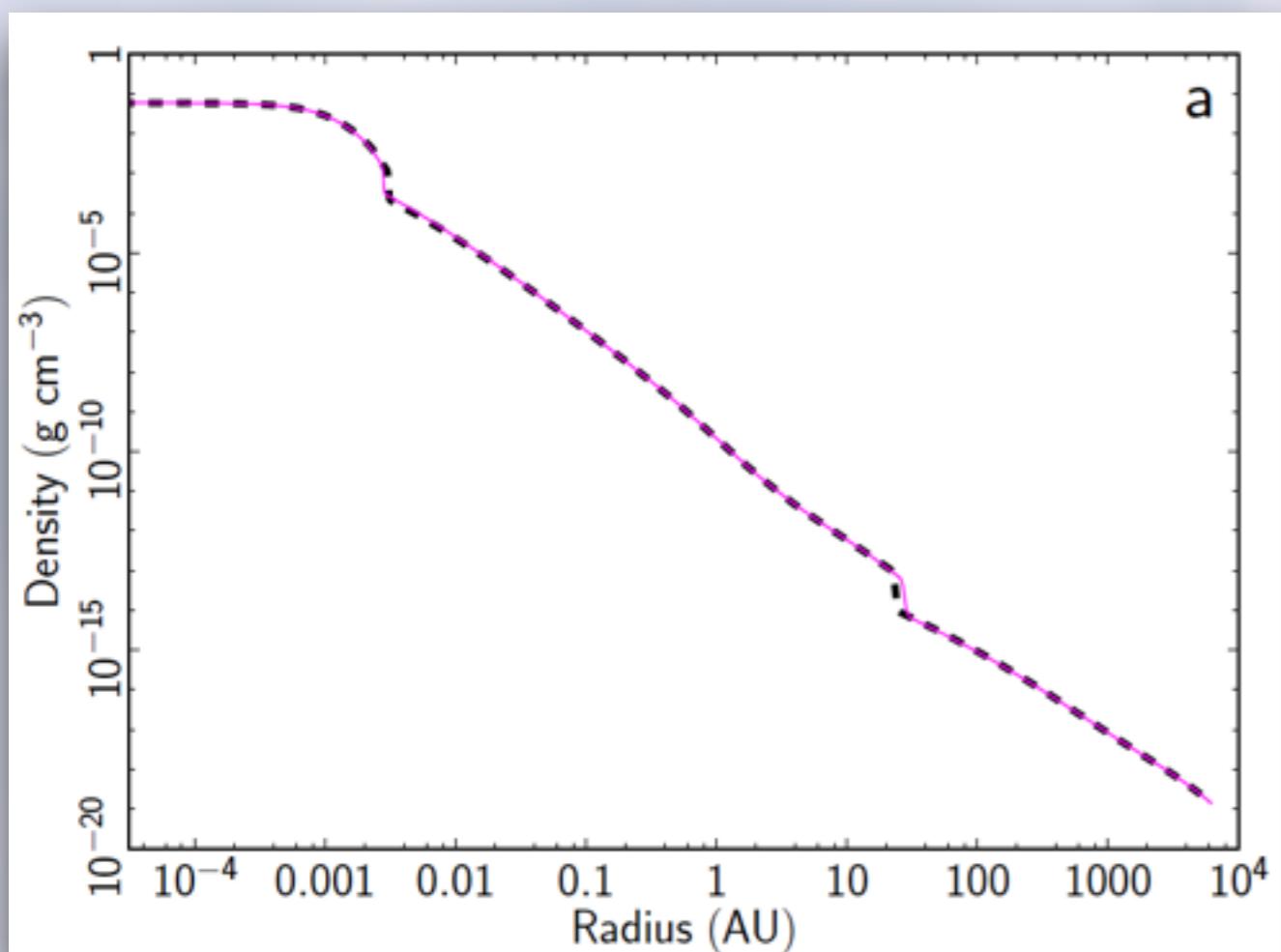


Vaytet et al. (2013)

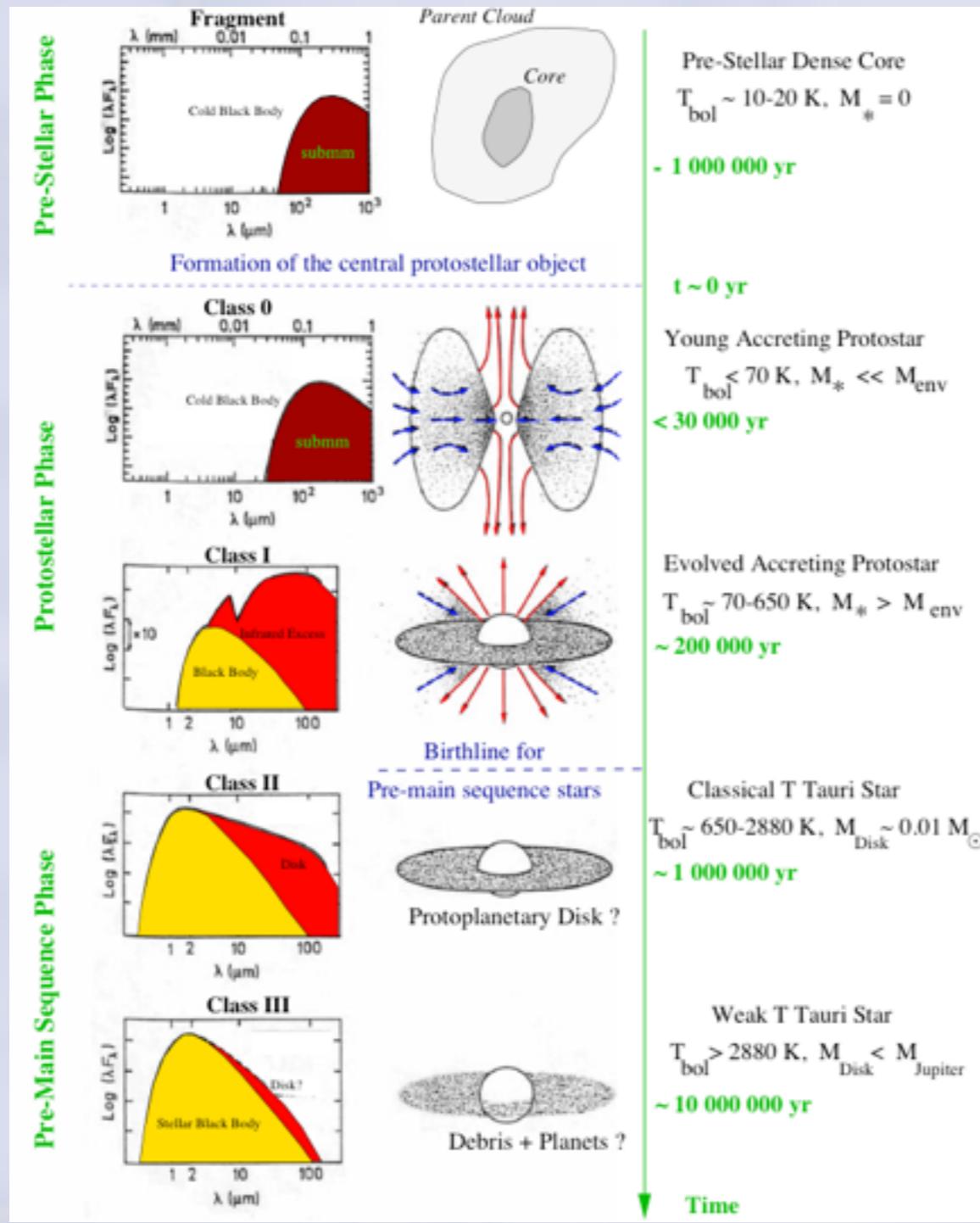
- from parsec scale ( $10^{18}$  cm) to stellar radius ( $10^{10}$  cm)
- density: from  $1 \text{ cm}^{-3}$  to  $10^{24} \text{ cm}^{-3}$
- temperature:  $10 \text{ K}$  -  $10^6 \text{ K}$
- ionisation depends on density and temperature... (*ideal vs non-ideal MHD*)
- chemistry, dust grain evolution ( *$H_2$  formation, growth, evaporation*)
- initial conditions for stellar evolution (*entropy level, magnetic field flux/geometry, angular momentum*)

# Star formation: the challenge

- ✓ Follow the dynamics over a wide range of physical scales:
  - **time** scales: free-fall time ( $\sim 10^{4,5}$  yr) to second
  - **spatial** scales: parsec to stellar radius
  - **physical** scales: density ranges from  $1 \text{ cm}^{-3}$  to  $10^{24} \text{ cm}^{-3}$

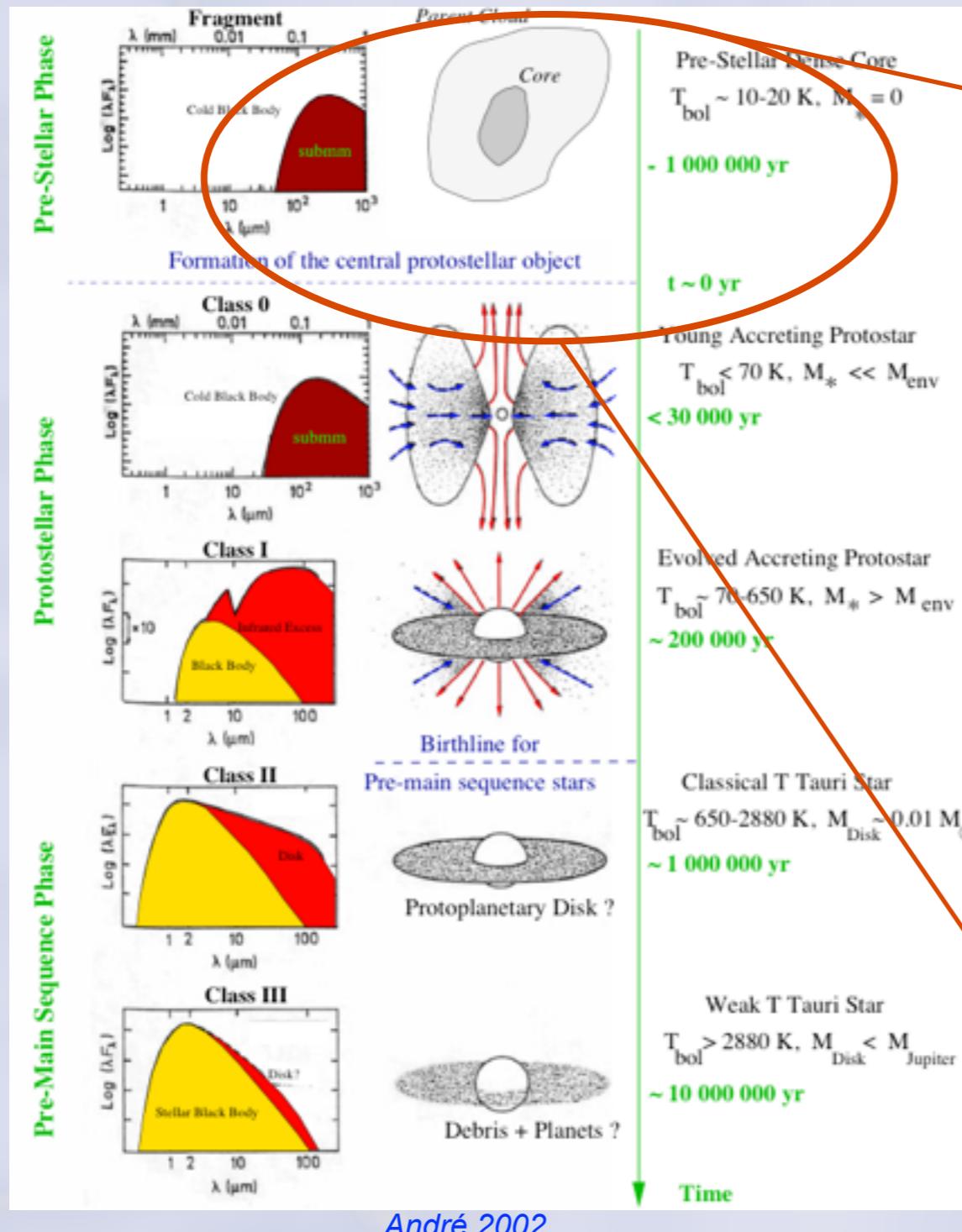


# Star formation evolutionary sequence



André 2002

# Star formation evolutionary sequence



Prestellar dense core collapse  
**First collapse**

**Isothermal**  $\downarrow 10^{4,5} \text{ yr}$

**First Larson core**  
**Adiabatic**

$a \text{ few } 10^3 \text{ yr}$

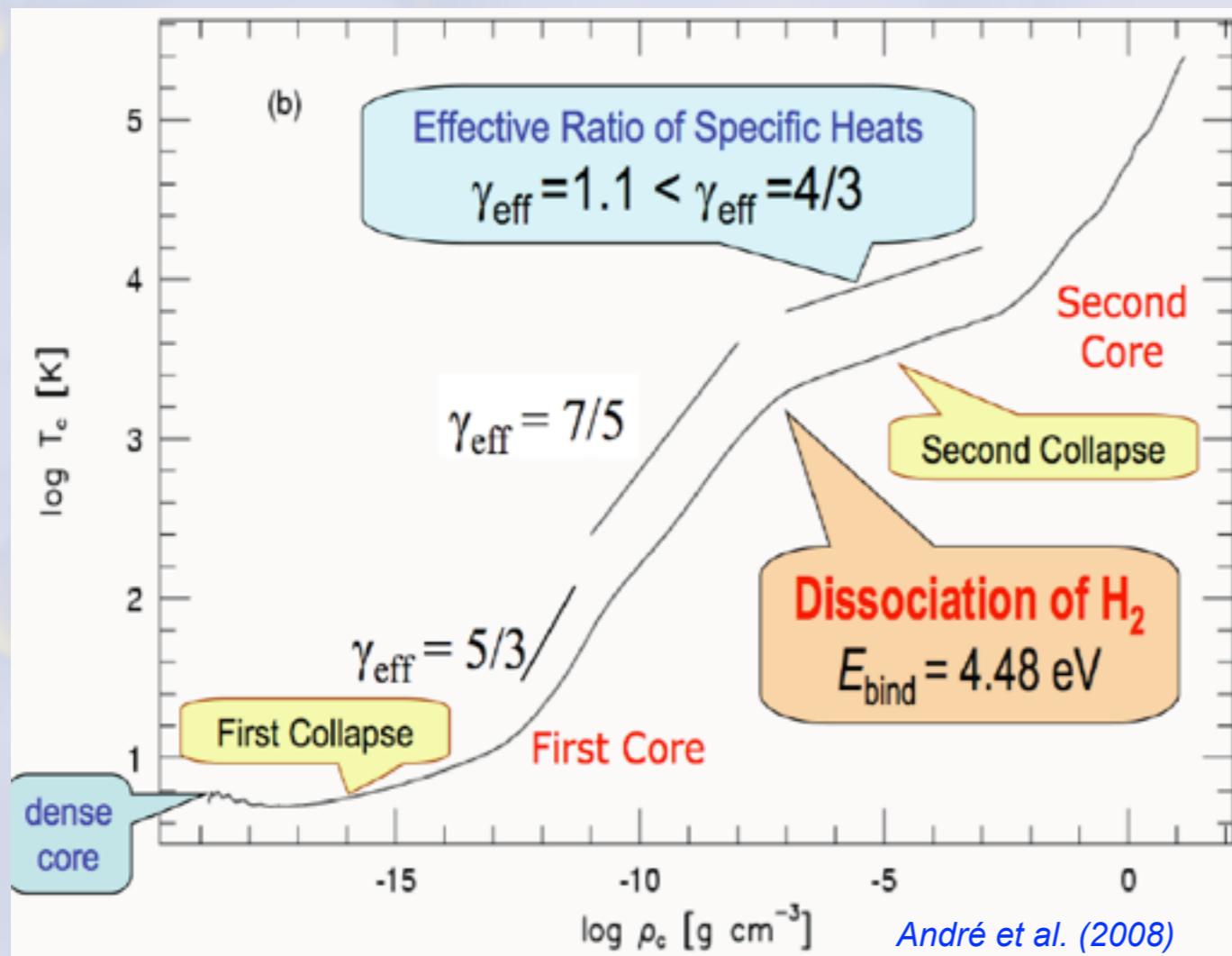
**$H_2$  dissociation**  
**Second collapse**

**Quasi -  
isothermal**

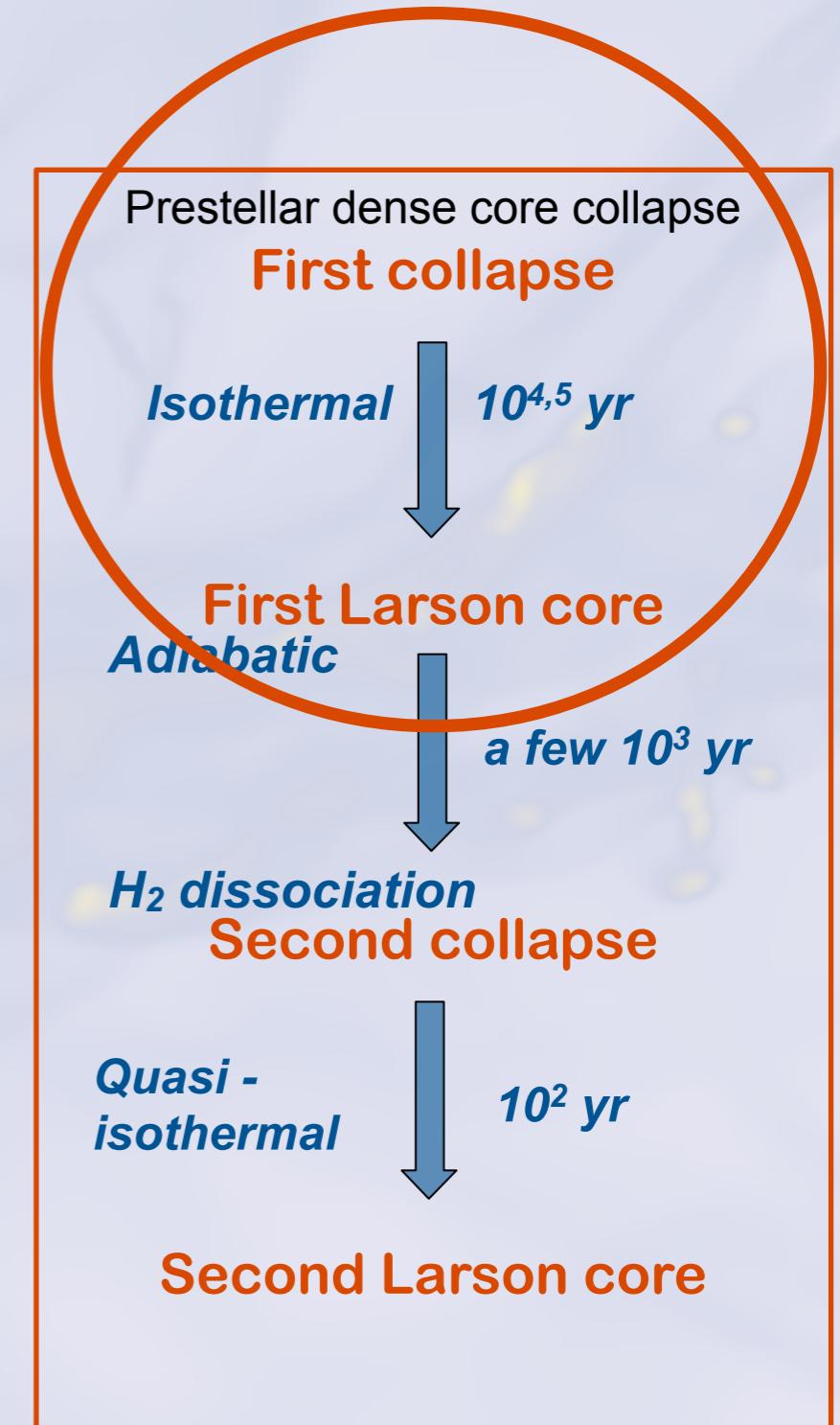
$10^2 \text{ yr}$

**Second Larson core**

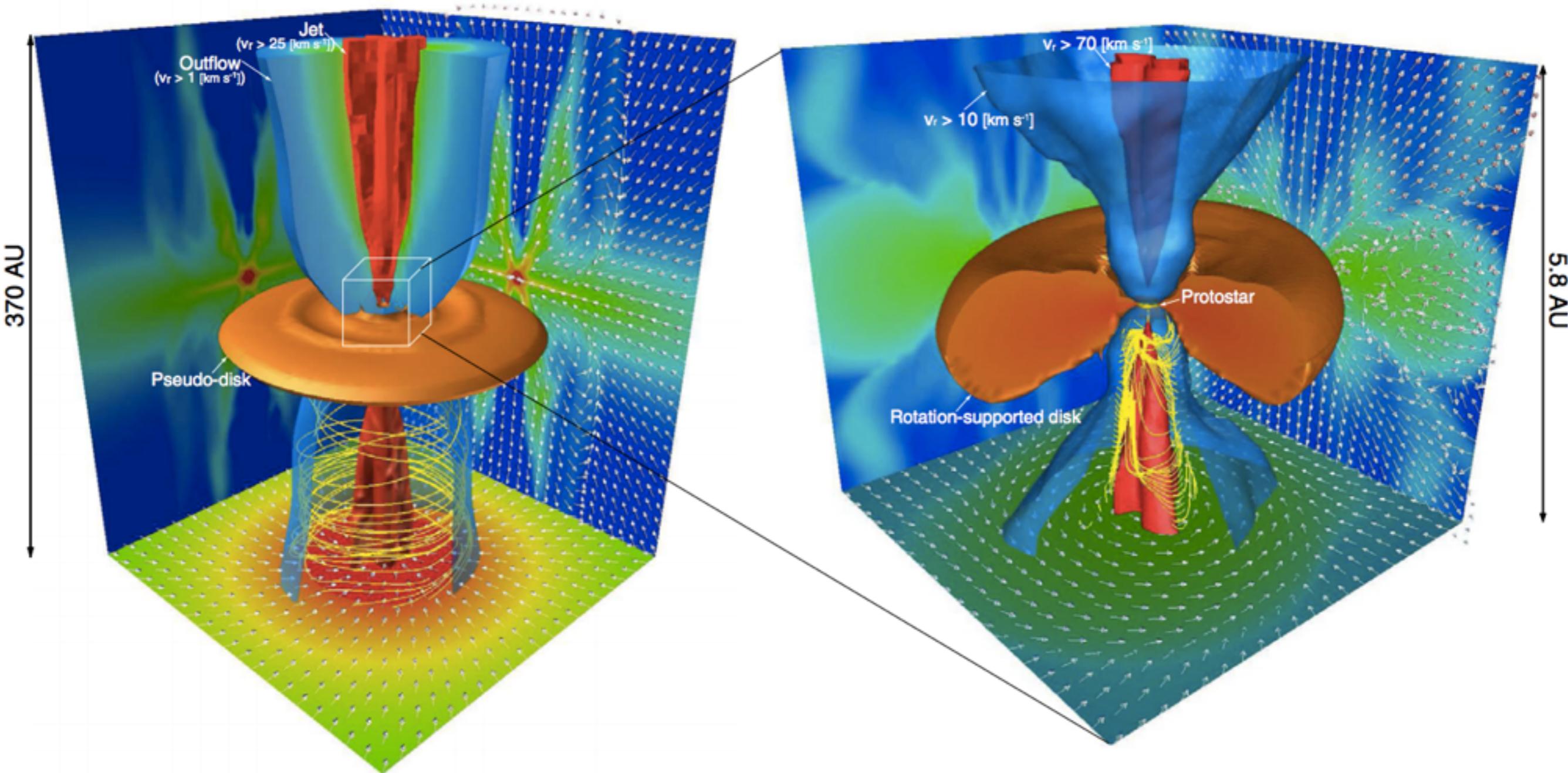
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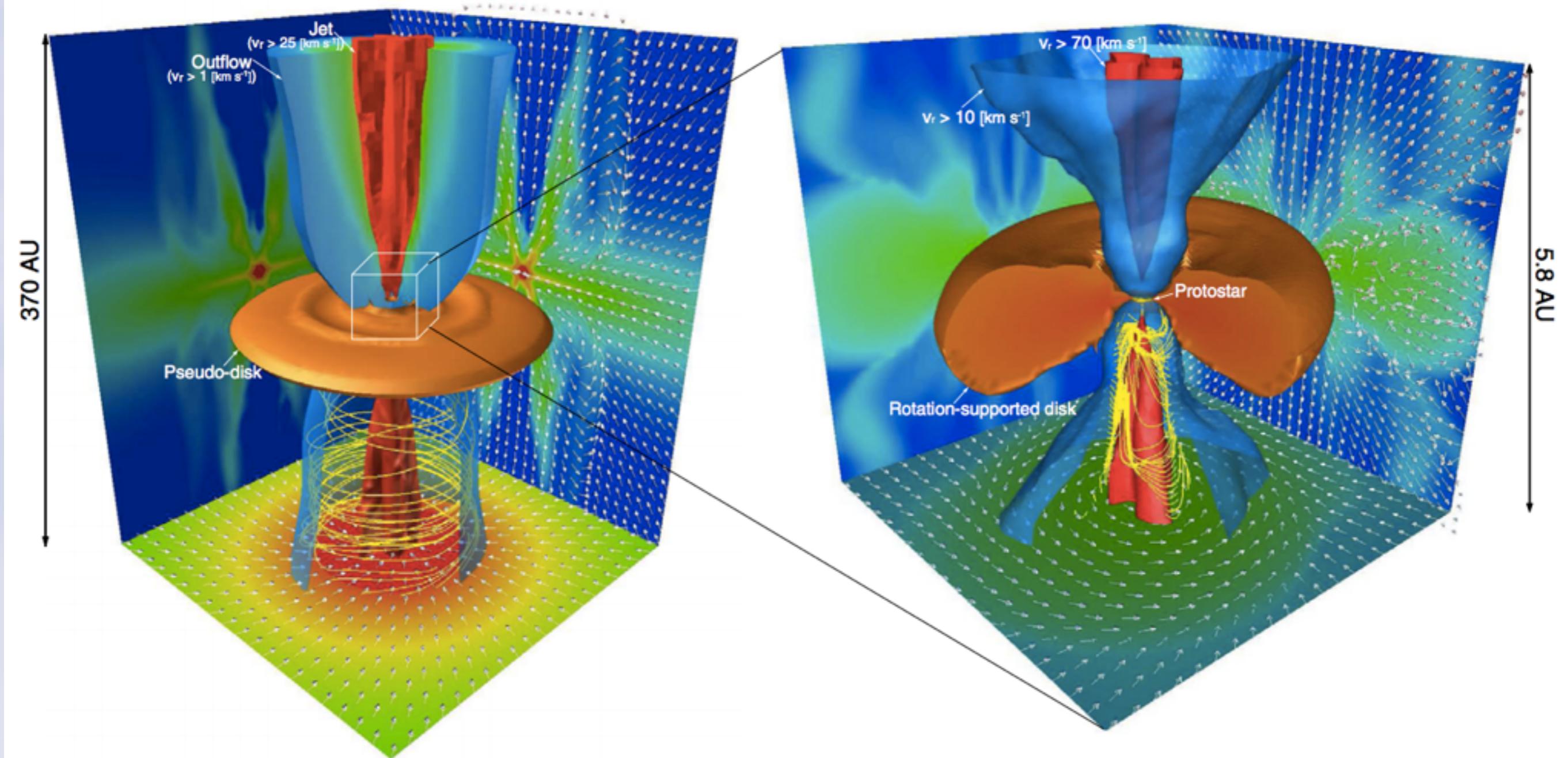
$$M_{\text{Jeans}} \propto \rho^{\frac{3}{2}} n^{-2}$$



# Protostellar core



# Protostellar core

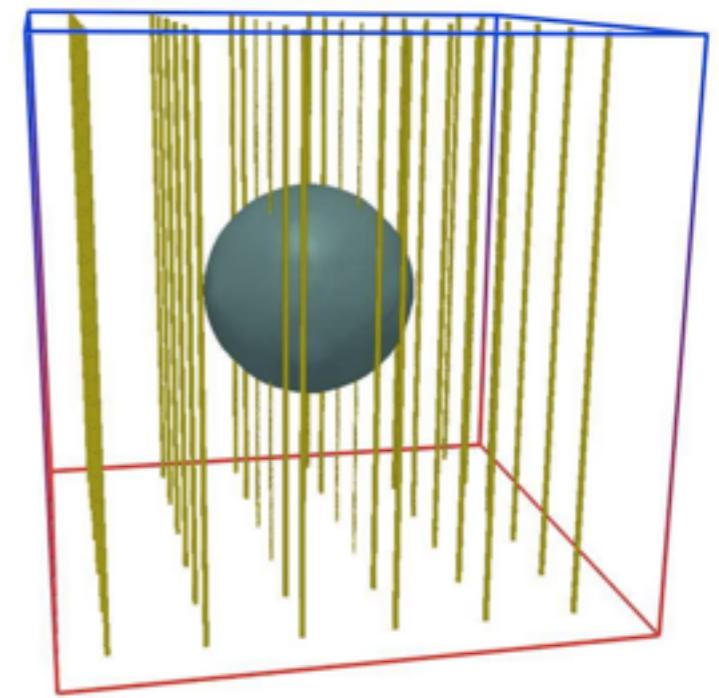


# Numerical experiments

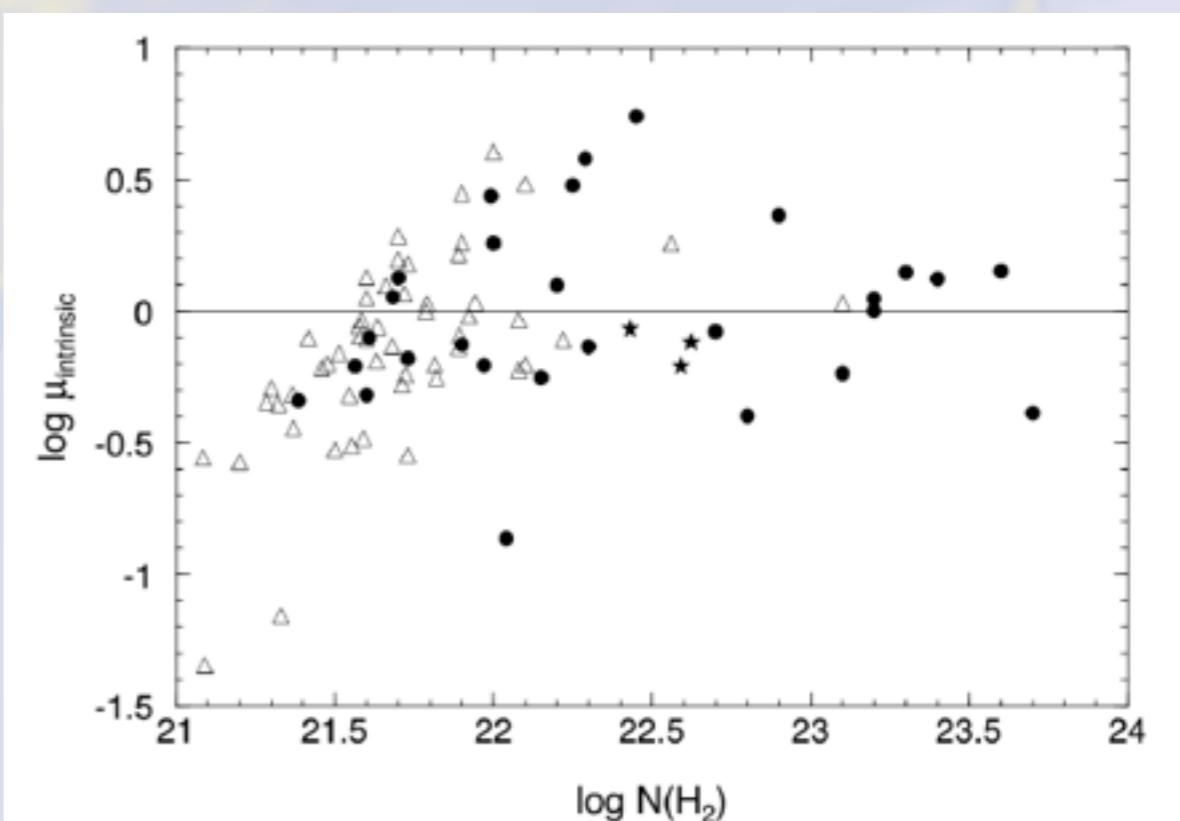
## Typical initial conditions:

- $1 M_{\odot}$  isolated dense core
- uniform / BE-like density profile
- uniform temperature (10 K,  $\alpha = E_{\text{th}}/E_{\text{grav}}$ )
- solid body / differential rotation ( $\beta = E_{\text{rot}}/E_{\text{grav}}$ )
- $m=2$  density perturbation / turbulent velocity field
- organised magnetic field

$$\mu = (\varphi/M)_{\text{crit}} / (\varphi/M) \text{ (observations } \mu \sim 2-5)$$



Refinement criterion solely based on the Jeans length

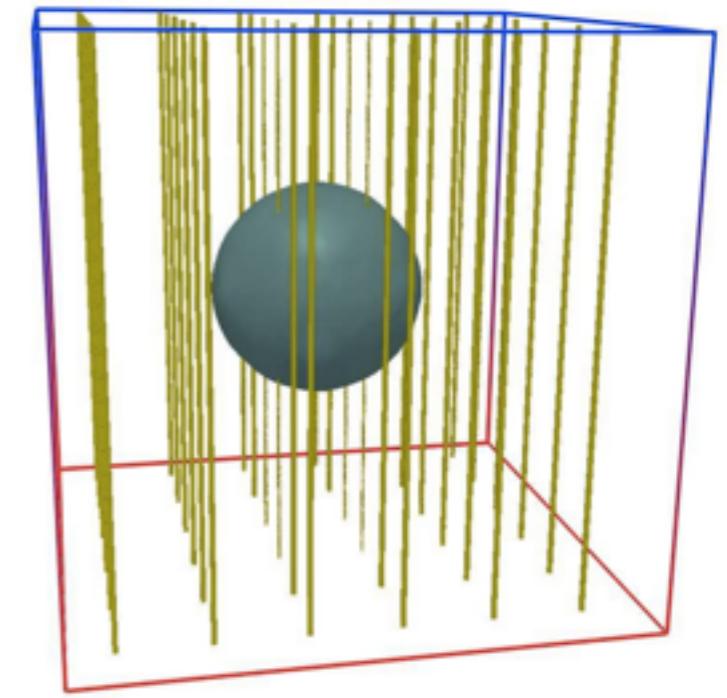


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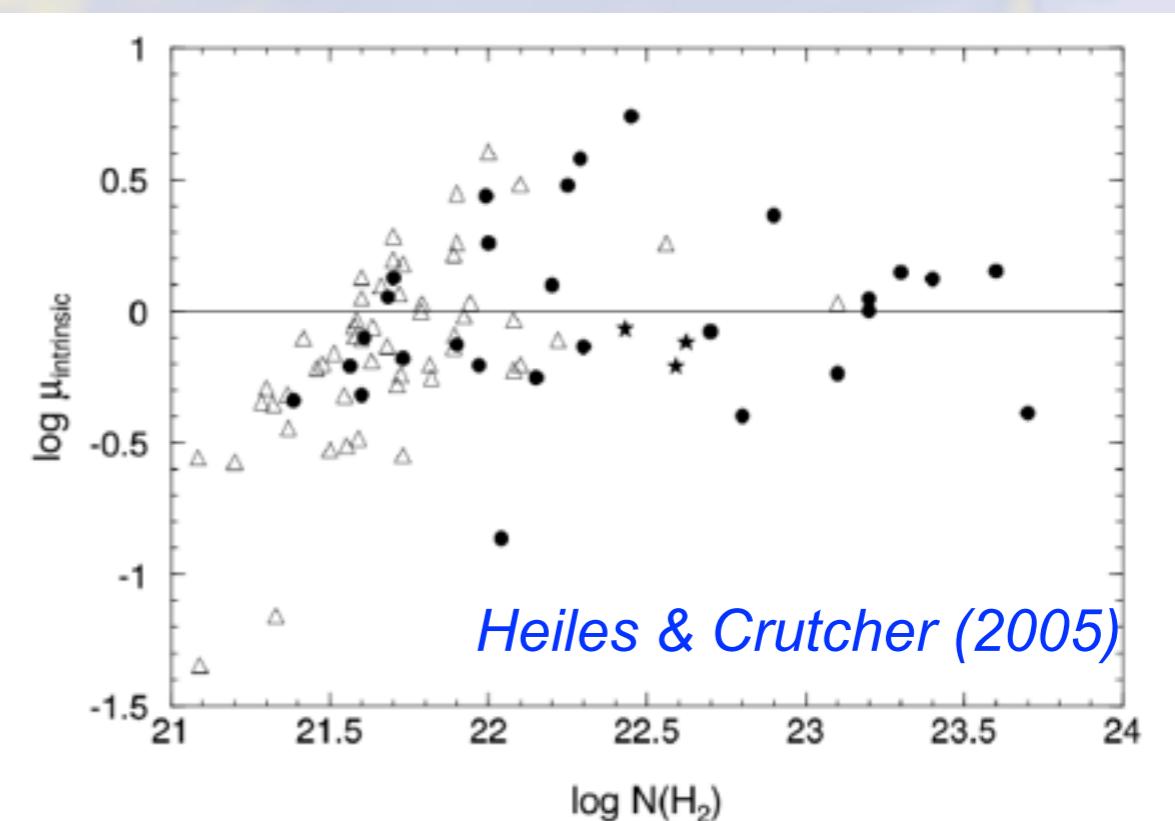
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Banerjee & Pudritz (2006)

Refinement criterion solely based on  
the Jeans length



# Effect of magnetic fields and rotation

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Consider a cloud of initial radius  $R$ , mass  $M$  and temperature  $T$

## Thermal support

- $E_{\text{th}}/E_{\text{grav}}$  **decreases** when  $R$  decreases

$$\frac{E_{\text{th}}}{E_{\text{grav}}} = \frac{3M/m_p k T}{2GM^2/R} \propto R$$

## Centrifugal support

- Angular momentum conservation
- $E_{\text{rot}}/E_{\text{grav}}$  **increases** when  $R$  decreases

$$j = R_0^2 \omega_0 = R^2 \omega(t)$$

$$\frac{E_{\text{rot}}}{E_{\text{grav}}} = \frac{MR^2 \omega^2}{GM^2/R} \propto \frac{1}{R}$$

## Magnetic support

- Magnetic flux conservation
  - $E_{\text{mag}}/E_{\text{grav}}$  is **constant** when  $R$  decreases
- $\mu = (\Phi/M)_{\text{crit}}/(\Phi/M)$  (observations  $\mu \sim 2-5$ )

$$\frac{E_{\text{mag}}}{E_{\text{grav}}} = \frac{B^2 R^3}{GM^2/R} \propto \left(\frac{\phi}{M}\right)^2$$

# Effect of magnetic fields and rotation

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**Consequences:**

**Centrifugal forces become dominant**

- flattening of the envelope
- formation of a centrifugally supported disk

**Magnetic forces stay comparable to gravity**

- flattening of the envelope
- NO formation if a supported structure
- formation of a pseudo-disk (Galli & Shu 1993)

**Magnetic fields brakes the cloud**

- transfer angular momentum from the inner part to the envelop

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# Numerics for star formation

## ★ 2 numerical methods :

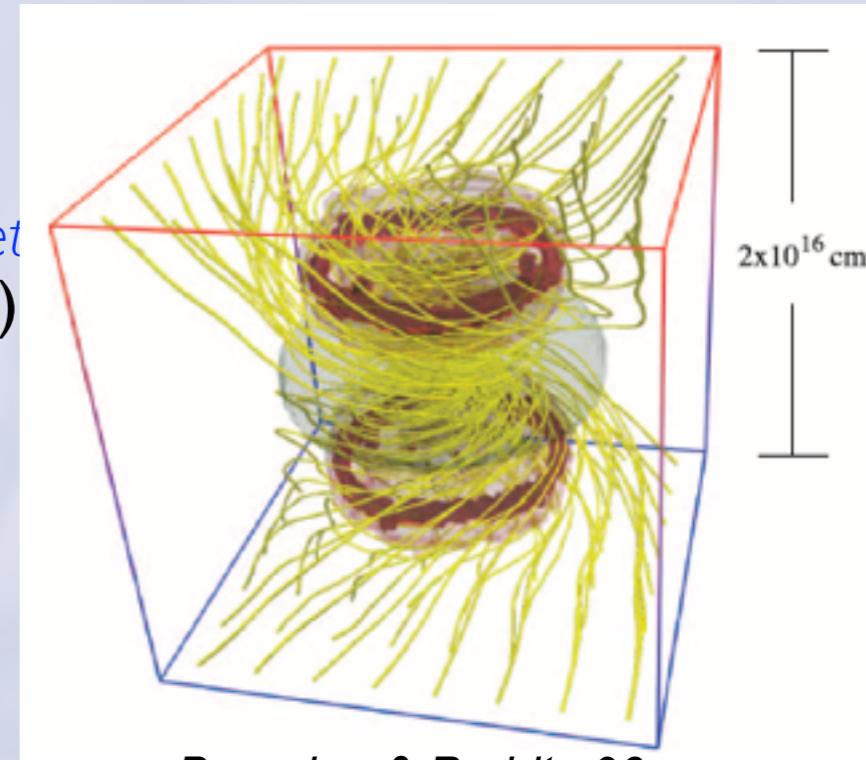
- **Grid based code (AMR)** : RAMSES code ([Teyssier 2002, Fromang et al. 2006, Commerçon et al. 2011a](#)), ORION code ([Krumholz et al.](#)) FLASH code ([Banerjee, Seifried et al.](#)), etc...

→ **Advantages :**

- ✓ accuracy
- ✓ shocks
- ✓ refinement criteria

→ **Disadvantages :**

- ✓ (headach)
- ✓ Eulerian



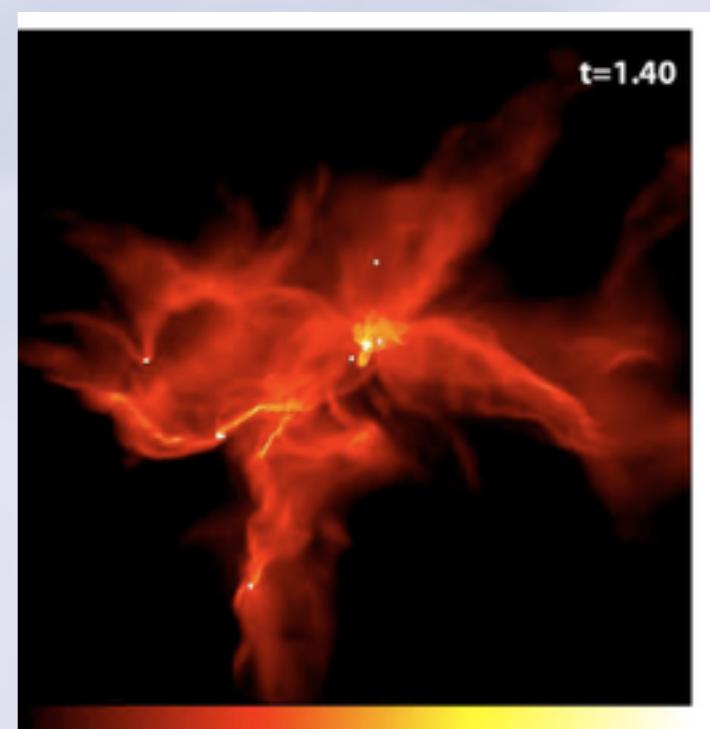
- **Lagrangian - SPH** : e.g. Bate & Price (RHD & MHD), Stamatellos et al. 2008 (RHD), etc...

→ **Advantages :**

- ✓ Lagrangian
- ✓ naturally adaptive
- ✓ (simpler)

→ **Disadvantages :**

- ✓ low density = low resolution
- ✓ noise, dissipative
- ✓ young



Bate et al. 02,03,08

# Numerical resolution criteria for SF

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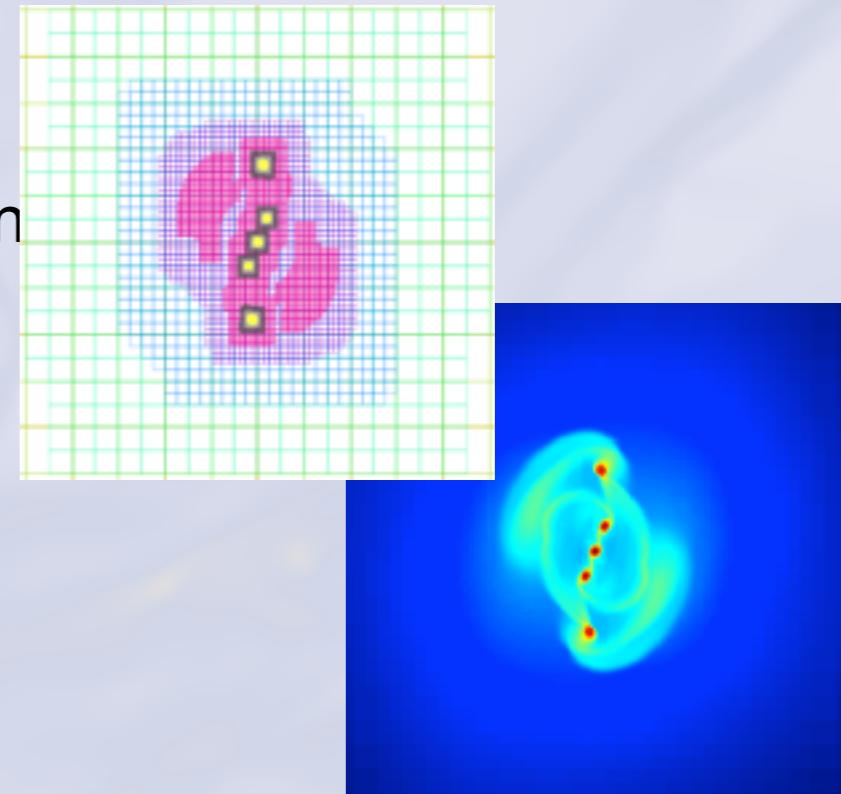
★ Gravitational instability → **Jeans** length

**AMR** : Refinement criteria  $N_J$  as a function of the local Jean

$$N_J \cdot \Delta x < \lambda_{\text{Jeans}}$$

↳ Truelove et al. 1997:  $N_J \geq 4$

↳ **Dynamical** criterion



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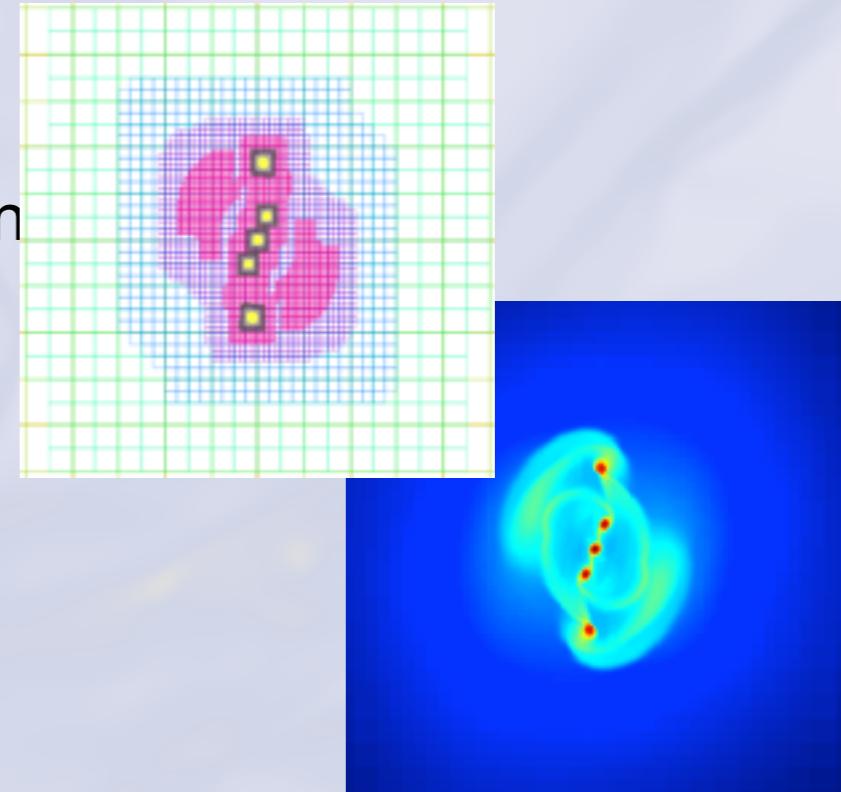
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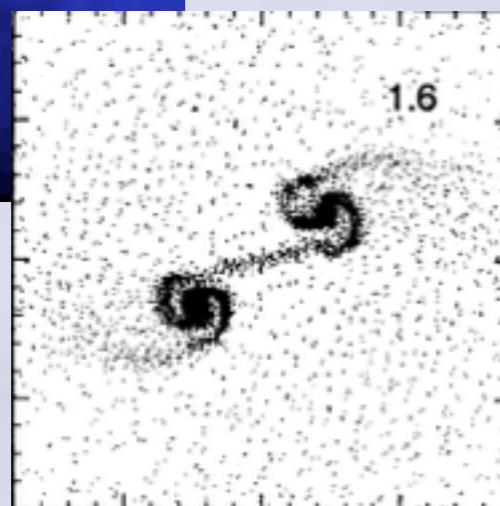
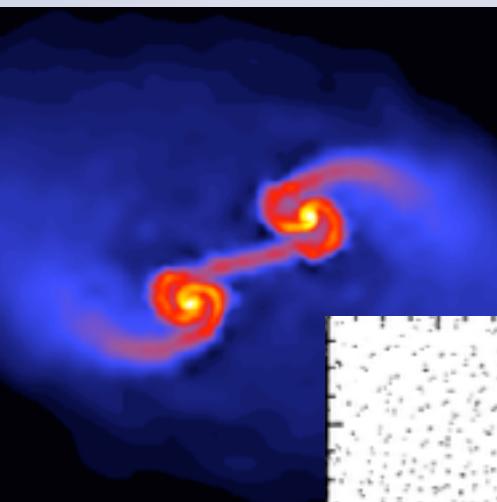
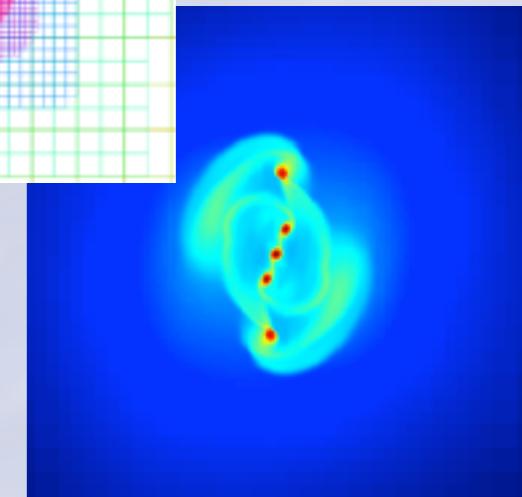
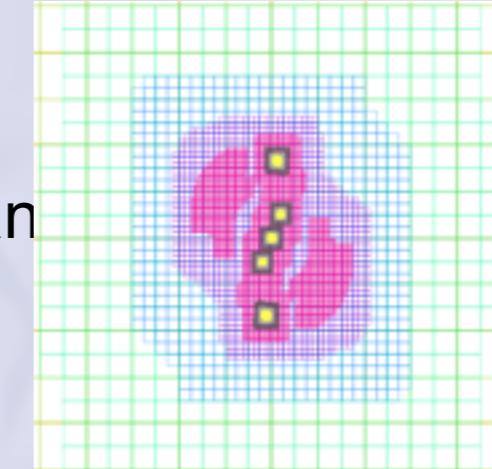
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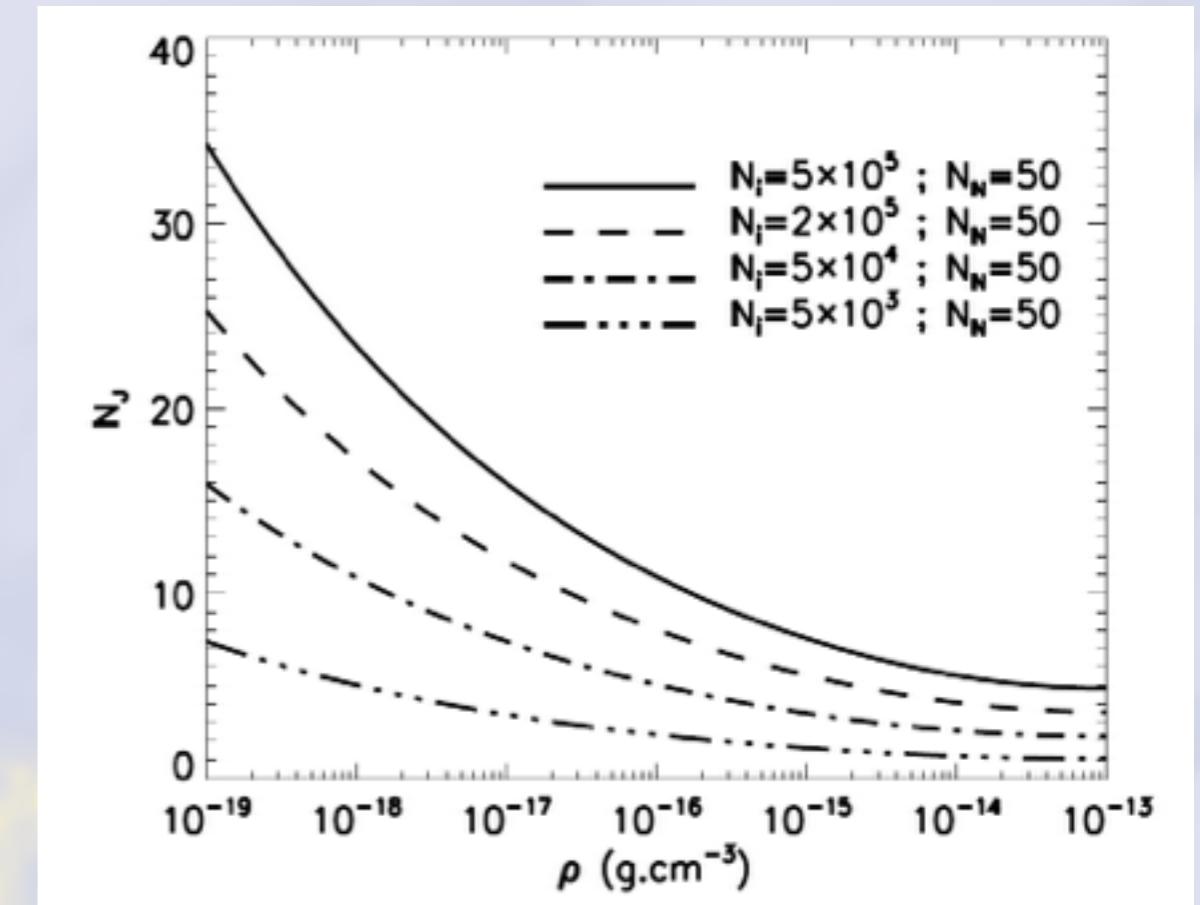
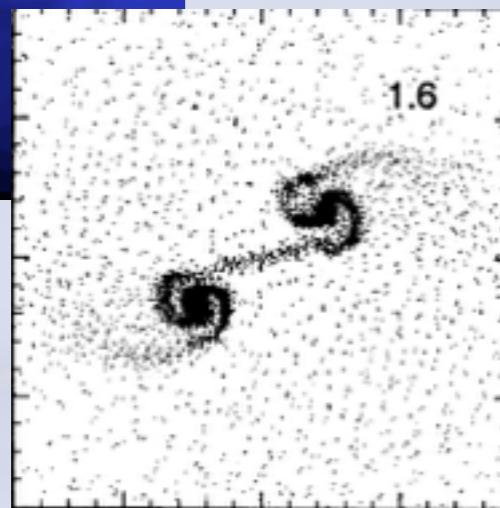
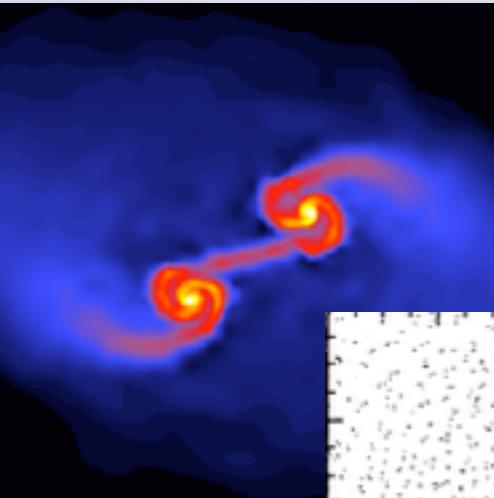


**SPH** : Total mass of the system particle + 2  $N_N$  ( $M_{\text{res}}$ ) should always be < than the local Jeans mass  $M_{\text{Jeans}}$  (Bate & Burkert 1997) → **static** criterion

↳ 2 parameters :  $N_p$  number of particles  
 $N_N$  number of neighbors

# Numerical resolution criteria for SF

AMR vs. SPH resolution:  $N_J^3 = M_{\text{Jeans}} / M_{\text{res}}$

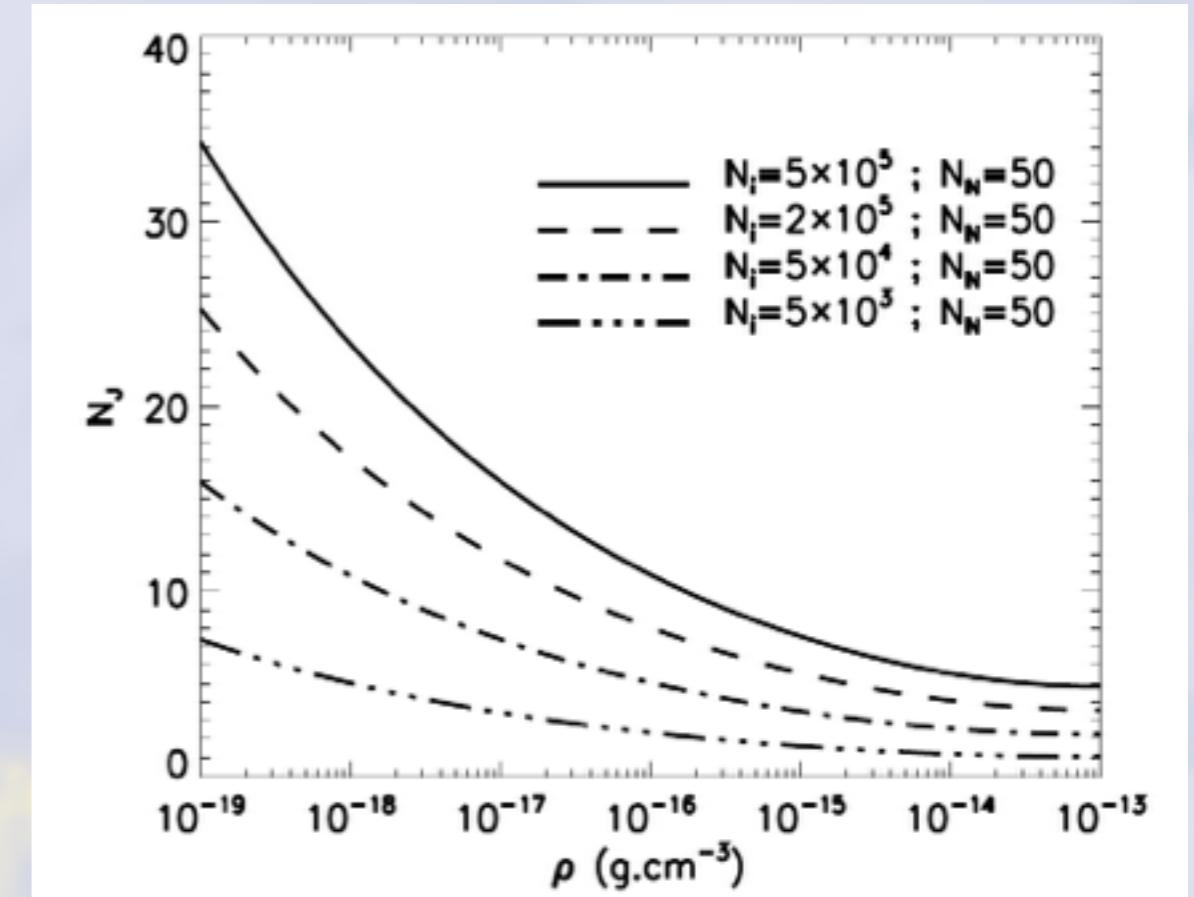


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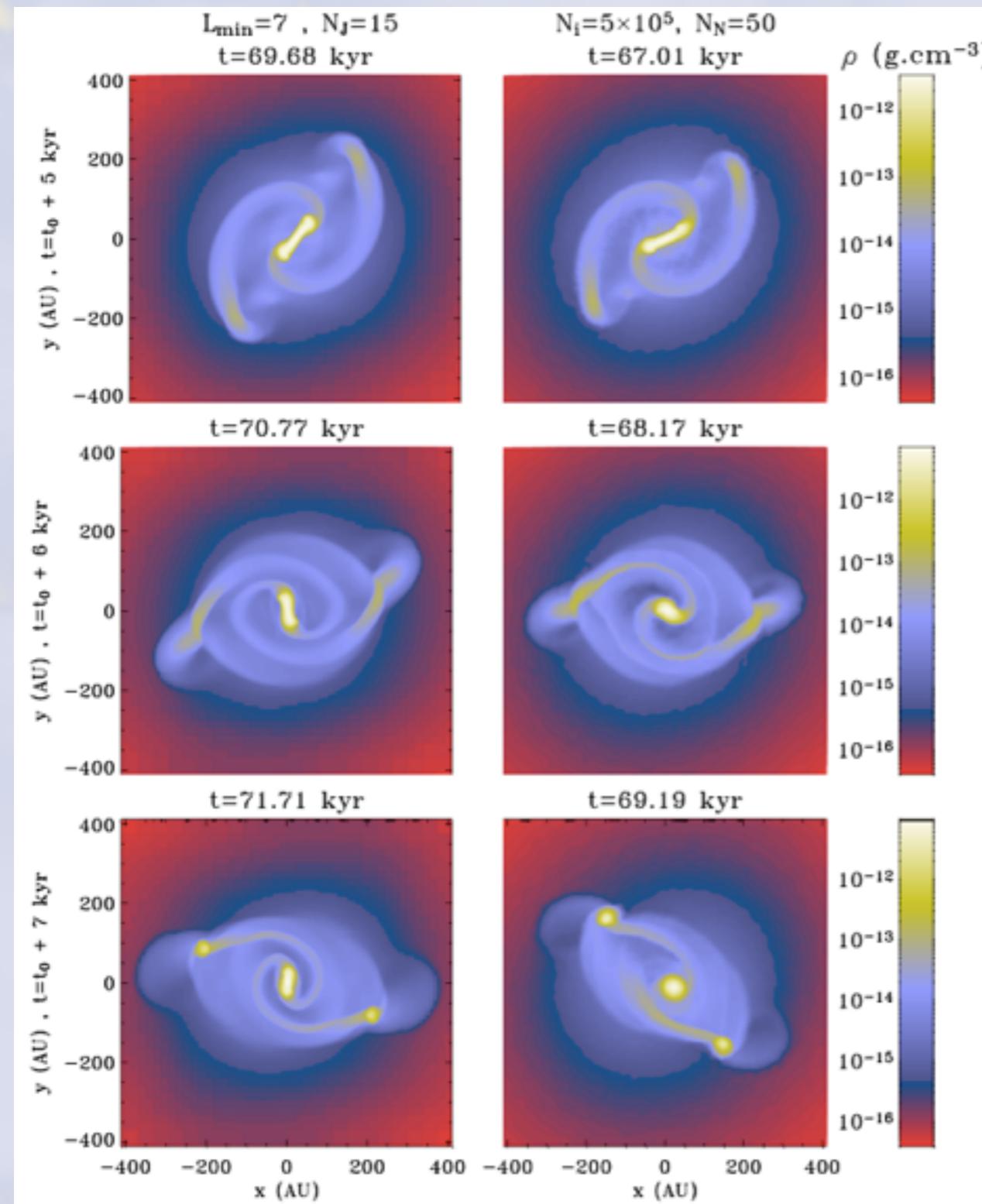
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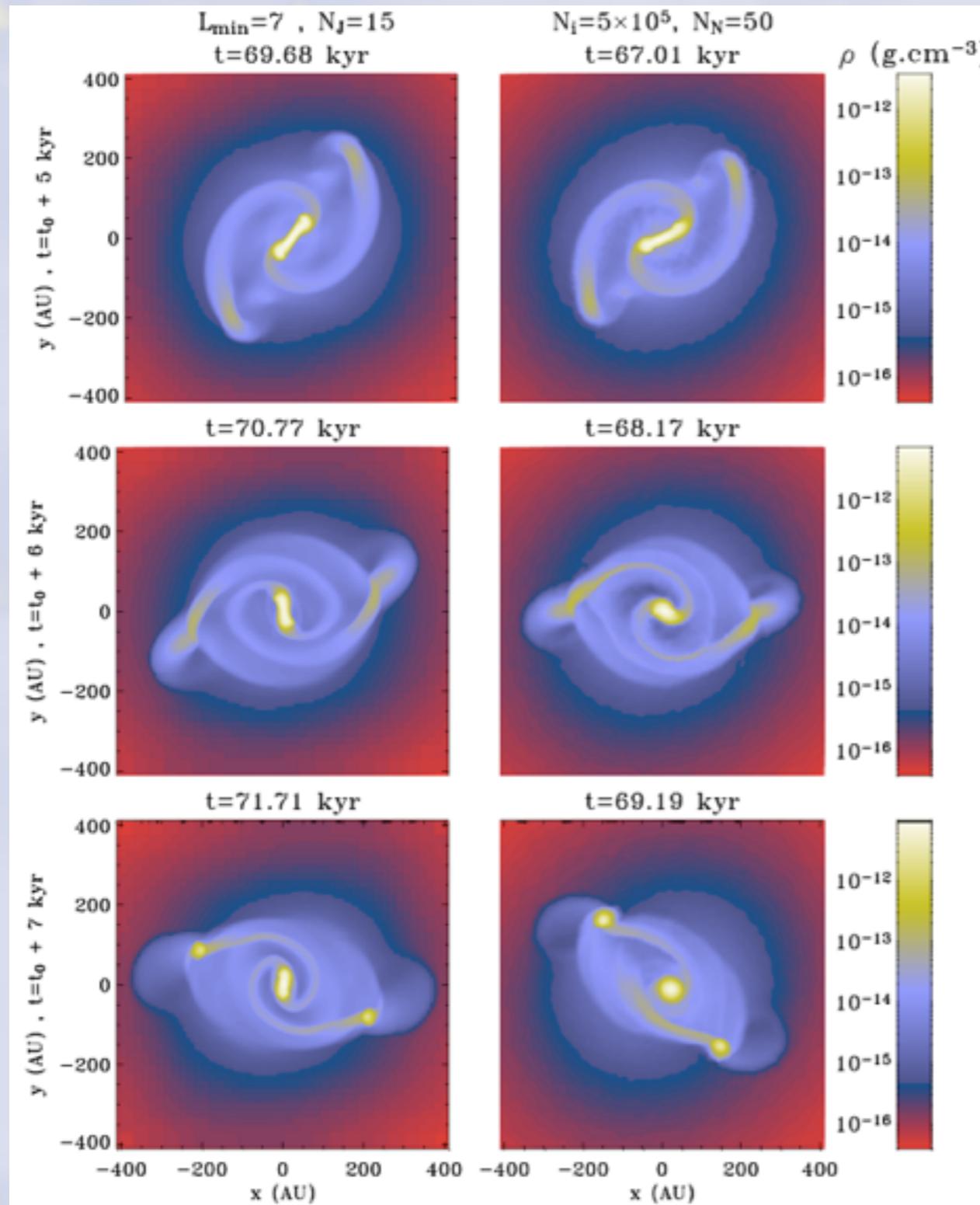
- ★ Debate on the accuracy of both methods:
  - => Are these methods appropriate for star formation?
  - => Are they converging?
- ☞ Identical initial conditions (uniform density & temperature sphere in solid body rotation, Boss & Bodenheimer test)
- ☞ Same equations (Euler equation: mass, momentum and total energy + barotropic closure relation)

# AMR vs. SPH: Convergence



Commerçon et al. 2008

# AMR vs. SPH: Convergence



**AMR:**  $64^3$  ( $L_{\min}=6$ ) ;  **$N_J=15$  !**

**SPH:**  $N_p=5\times 10^5$  ;  $N_N=50$

i.e.  $\sim 5300$  particles/Jeans mass !

- CONVERGENCE!

*Commerçon et al. 2008*

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# Radiation-magneto-hydrodynamics in **RAMSES**

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- ✓ Non-ideal MHD solver using Constrained Transport ([Teyssier et al. 2006, Fromang et al. 2006, Masson et al. 2012,2016](#)). In this work, just **ambipolar diffusion** with resistivity from **equilibrium gas-grain** chemistry ([Marchand et al. 2016](#))
- ✓ Multifrequency Radiation-HD solver using the Flux Limited Diffusion approximation ([Commerçon et al. 2011, 2014, González et al. 2015](#)). In this work, just **grey**
- ✓ Sink particles using clump finder algorithm ([Bleuler & Teyssier 2014](#))
- ✓ Gas-grain opacities from [Semenov et al. \(2003\)](#)

$$\begin{aligned}\partial_t \rho + \nabla \cdot [\rho \mathbf{u}] &= 0 \\ \partial_t \rho \mathbf{u} + \nabla \cdot [\rho \mathbf{u} \otimes \mathbf{u} + P \mathbb{I}] &= -\rho \nabla \Phi - \lambda \nabla E_r + (\nabla \times \mathbf{B}) \times \mathbf{B} \\ \partial_t E_T + \nabla \cdot [\mathbf{u} (E_T + P_T) - \mathbf{B}(\mathbf{B} \cdot \mathbf{u}) - E_{AD} \times \mathbf{B}] &= -\rho \mathbf{u} \cdot \nabla \Phi - \mathbb{P}_r \nabla : \mathbf{u} - \lambda \mathbf{u} \nabla E_r + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) \\ \partial_t E_r + \nabla \cdot [\mathbf{u} E_r] &= -\mathbb{P}_r \nabla : \mathbf{u} + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) + \kappa_P \rho c (a_R T^4 - E_r) \\ \partial_t B - \nabla \times (\mathbf{u} \times \mathbf{B}) - \nabla \times E_{AD} &= 0\end{aligned}$$

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**Gravitational**

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**Gravitational**      **Radiative**

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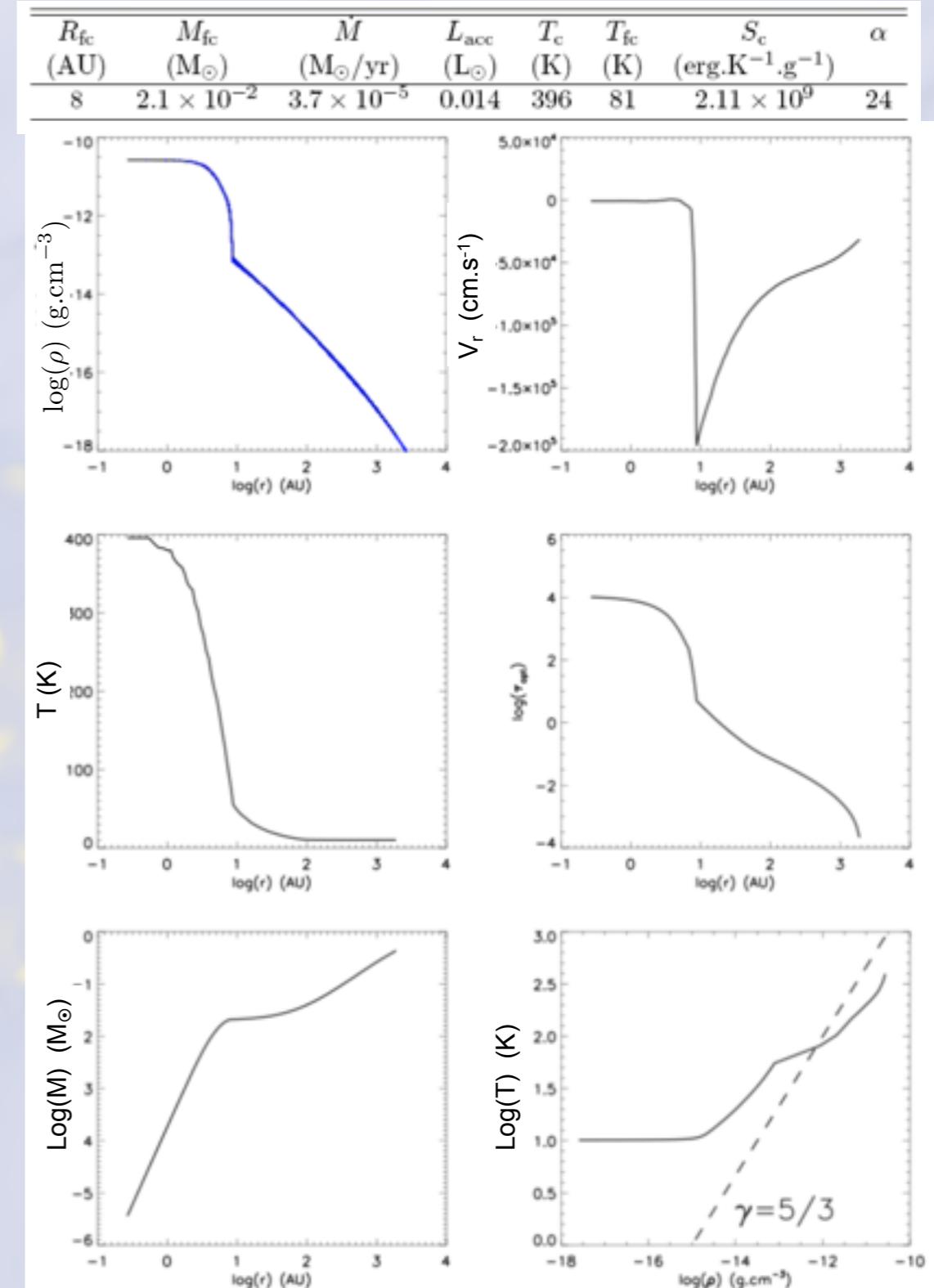
$$\begin{aligned}
 \partial_t \rho + \nabla \cdot [\rho \mathbf{u}] &= 0 \\
 \partial_t \rho \mathbf{u} + \nabla \cdot [\rho \mathbf{u} \otimes \mathbf{u} + P \mathbb{I}] &= -\rho \nabla \Phi - \lambda \nabla E_r + (\nabla \times \mathbf{B}) \times \mathbf{B} \\
 \partial_t E_T + \nabla \cdot [\mathbf{u} (E_T + P_T) - \mathbf{B}(\mathbf{B} \cdot \mathbf{u}) - E_{AD} \times \mathbf{B}] &= -\rho \mathbf{u} \cdot \nabla \Phi - \mathbb{P}_r \nabla : \mathbf{u} - \lambda \mathbf{u} \nabla E_r + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) \\
 \partial_t E_r + \nabla \cdot [\mathbf{u} E_r] &= -\mathbb{P}_r \nabla : \mathbf{u} + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) + \kappa_P \rho c (a_R T^4 - E_r) \\
 \partial_t B - \nabla \times (\mathbf{u} \times \mathbf{B}) - \nabla \times E_{AD} &= 0
 \end{aligned}$$

Gravitational      Radiative      Lorentz force

# Spherical collapse

$$\alpha = 0.50 = E_{\text{th}}/E_{\text{grav}}$$

- ✓ spherical symmetry conserved
- ✓ 1<sup>st</sup> core properties similar to Masunaga et al. (1999)
- ✓ accretion shock: supercritical radiative shock, i.e ***all*** the incident ***kinetic energy*** is ***radiated*** away (*Commerçon et al. 2011b*)

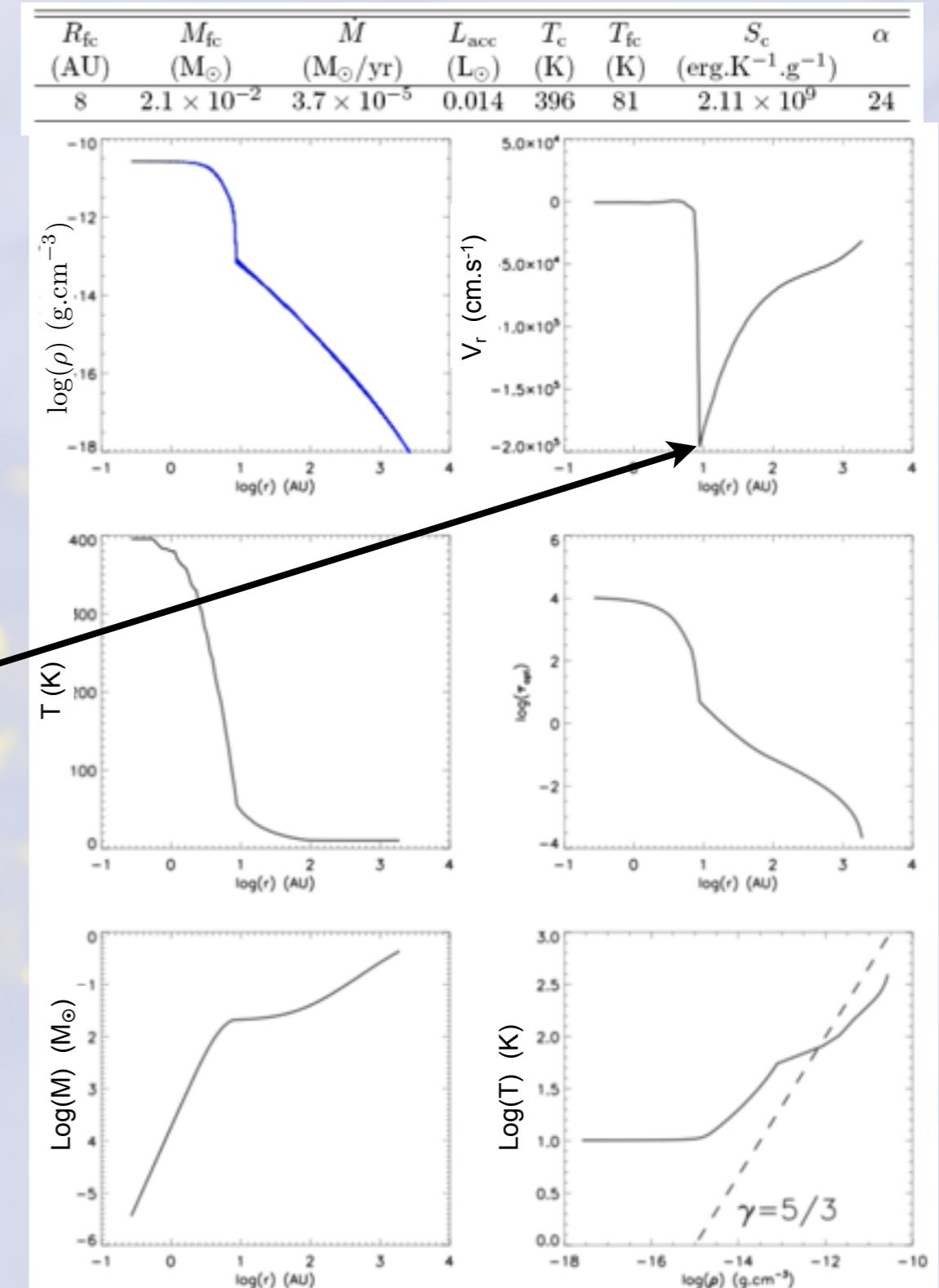


*Commerçon et al. 2011a*

# Spherical collapse

$$\alpha = 0.50 = E_{\text{th}}/E_{\text{grav}}$$

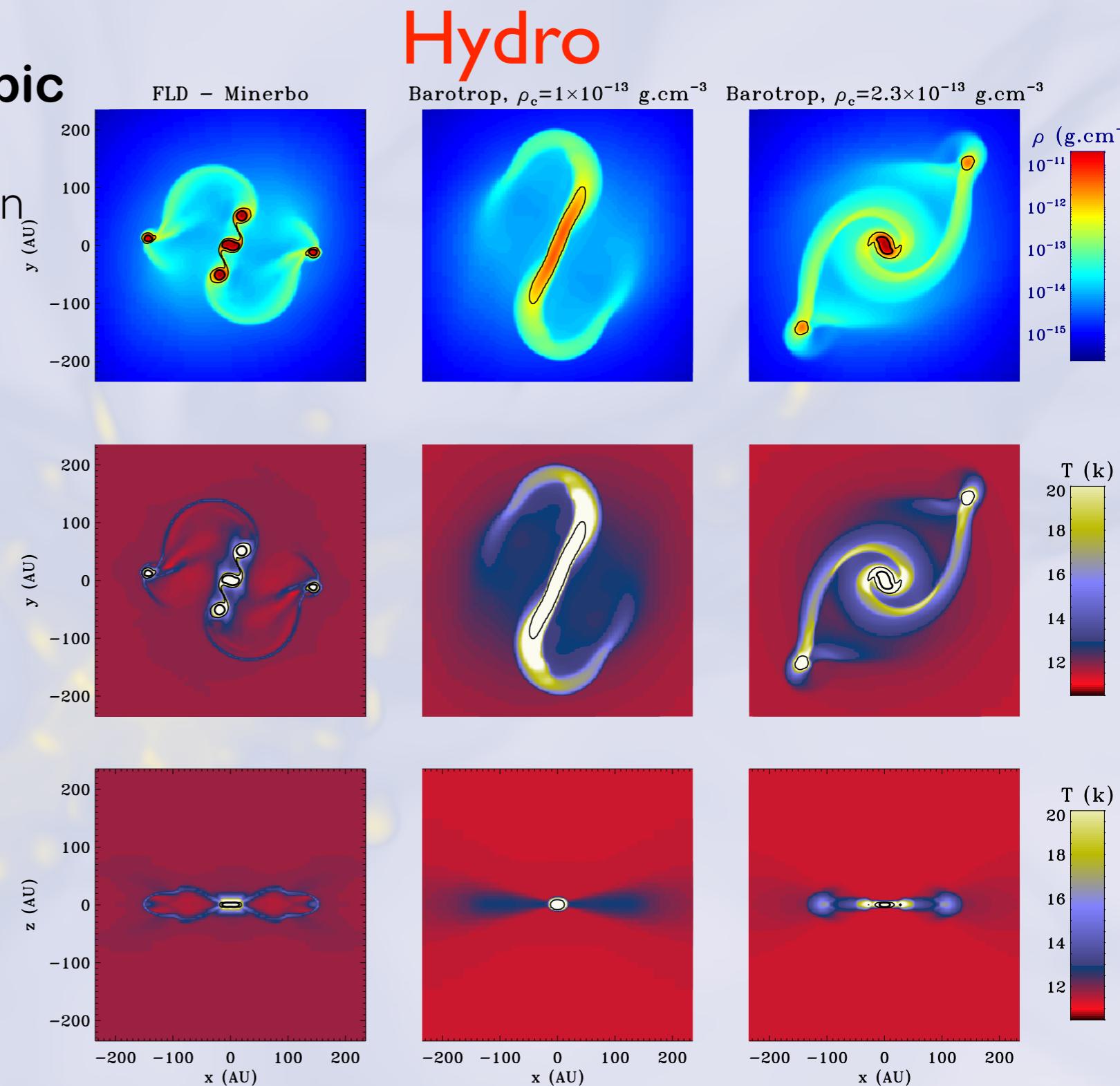
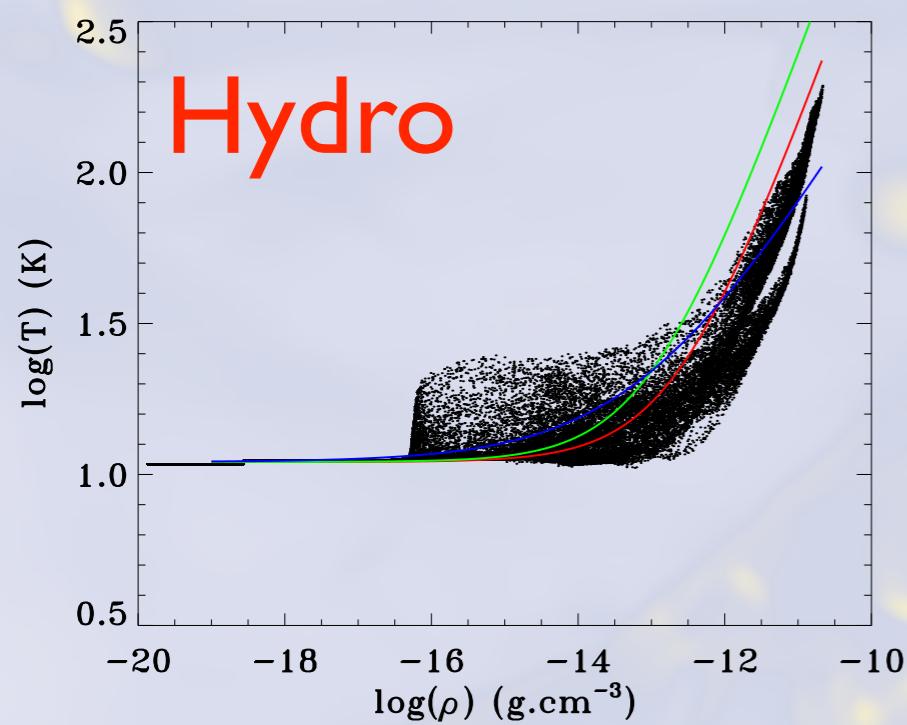
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# $1 M_{\odot}$ dense core collapse: Hydro

## Comparison to the barotropic case

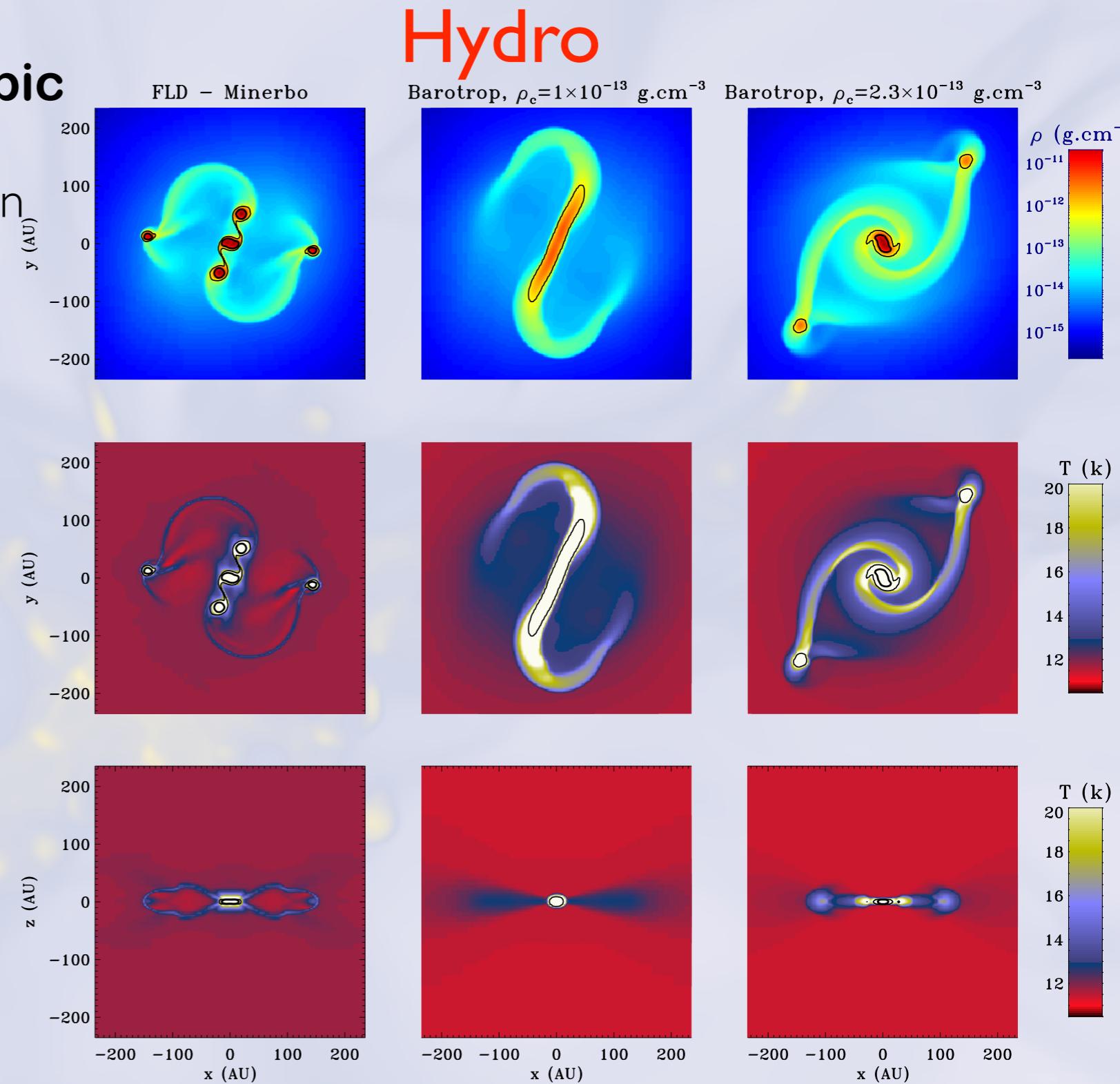
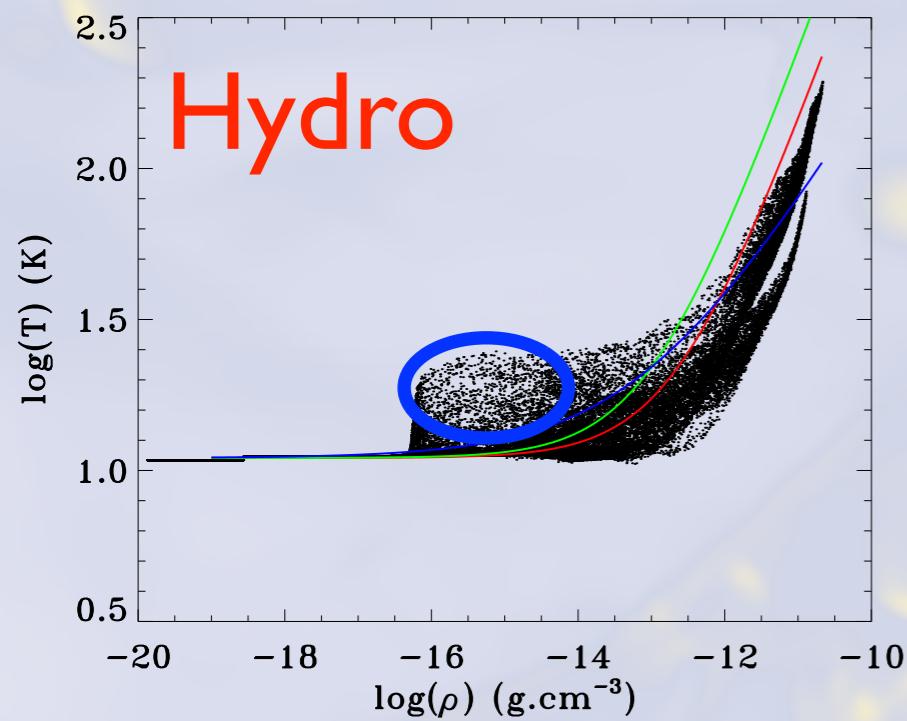
- **Hydro case:** more fragmentation
- gas cools efficiently in the vertical direction  
==> *lower* Jeans mass



# $1 M_{\odot}$ dense core collapse: Hydro

## Comparison to the barotropic case

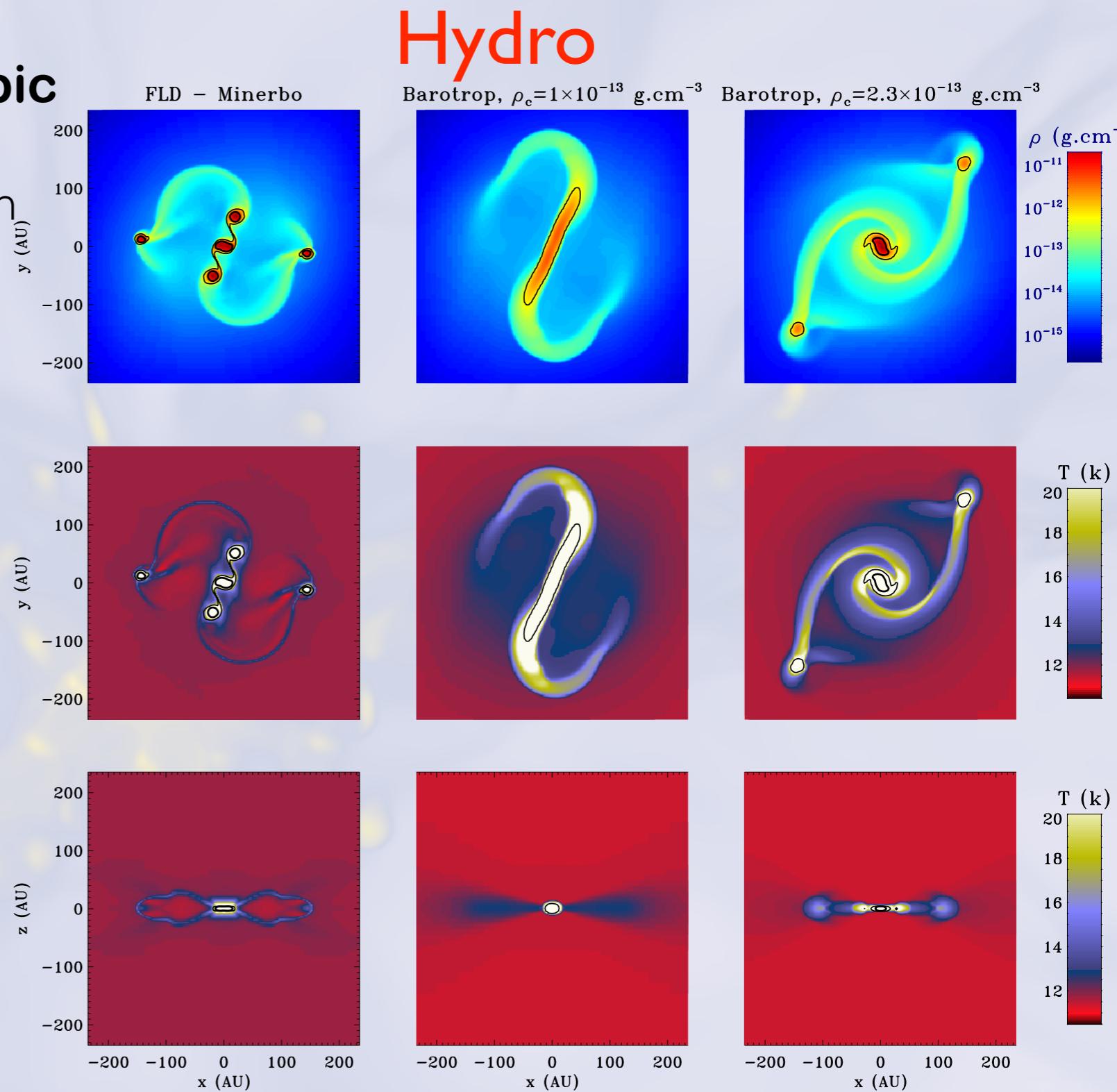
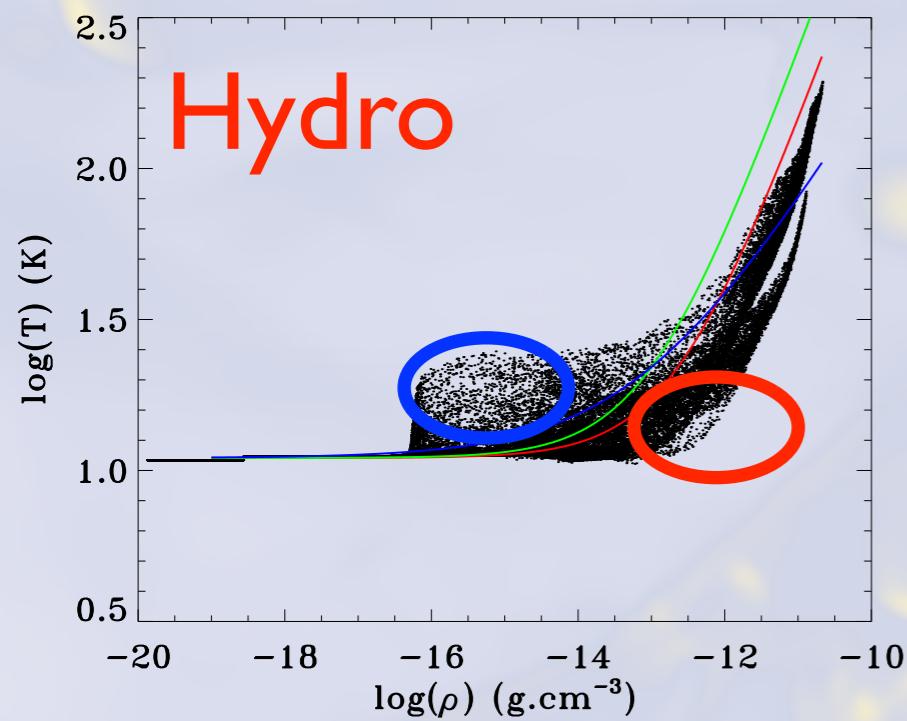
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# $1 M_{\odot}$ dense core collapse: Hydro

## Comparison to the barotropic case

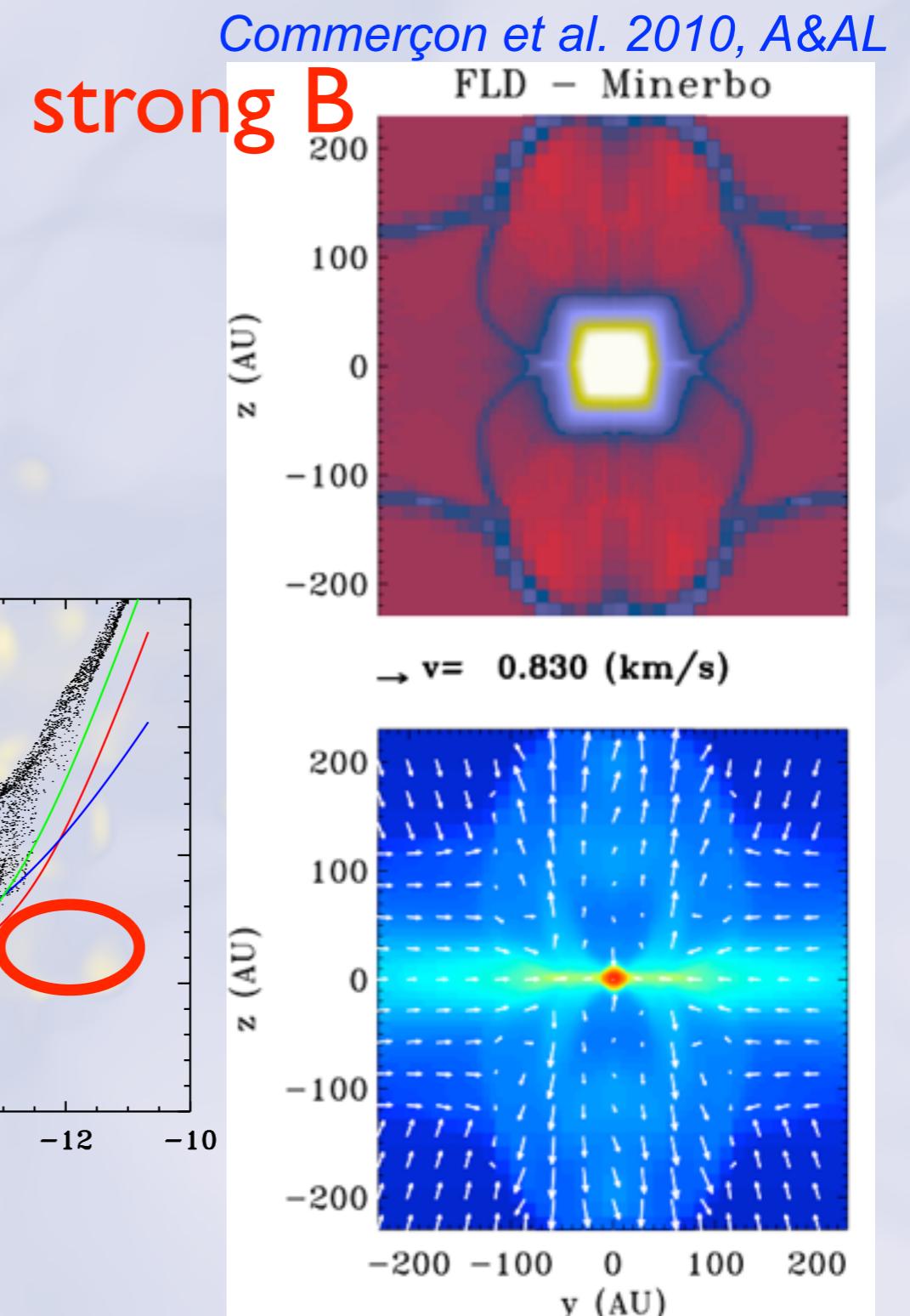
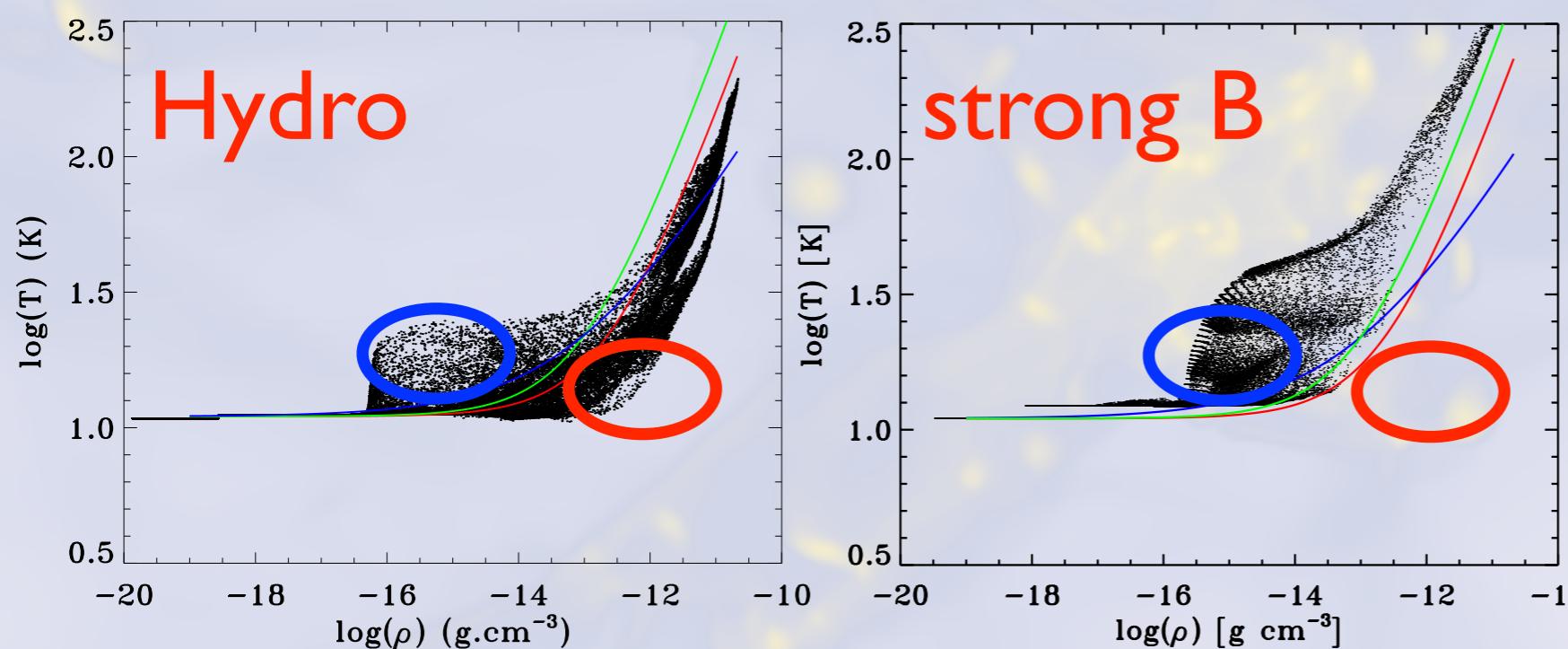
- **Hydro case:** more fragmentation
- gas cools efficiently in the vertical direction  
==> *lower* Jeans mass



# $1 M_{\odot}$ dense core collapse: Hydro vs. $\mu = 5$

## Comparison to the barotropic case

- Hydro case: more fragmentation
- RMHD: magnetic braking  $\Leftrightarrow$  radiative feedback ( $L_{\text{acc}}$ )

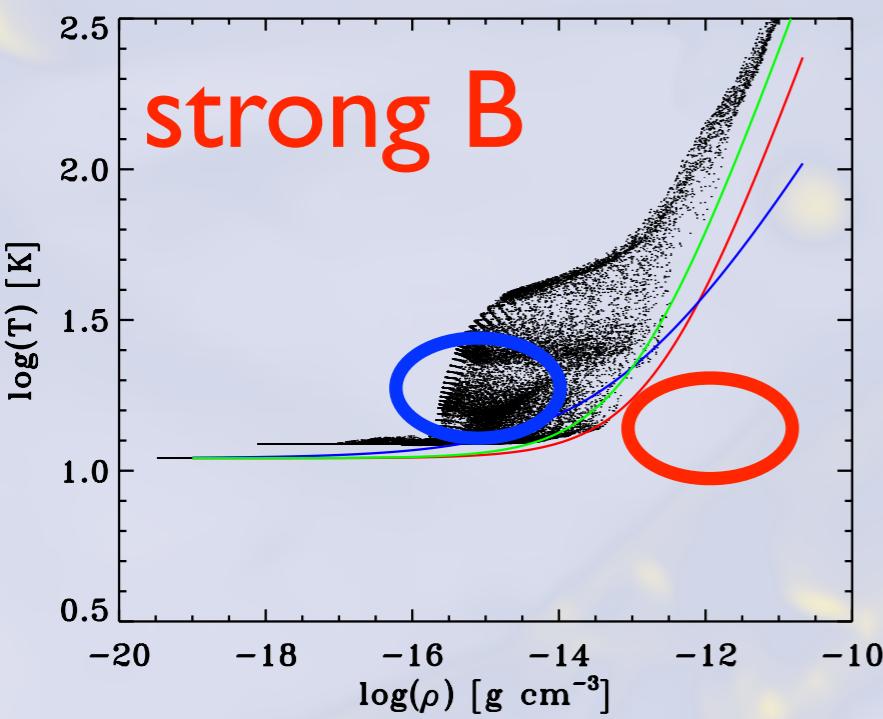


# $1 M_{\odot}$ dense core collapse: FLD vs. barotrop

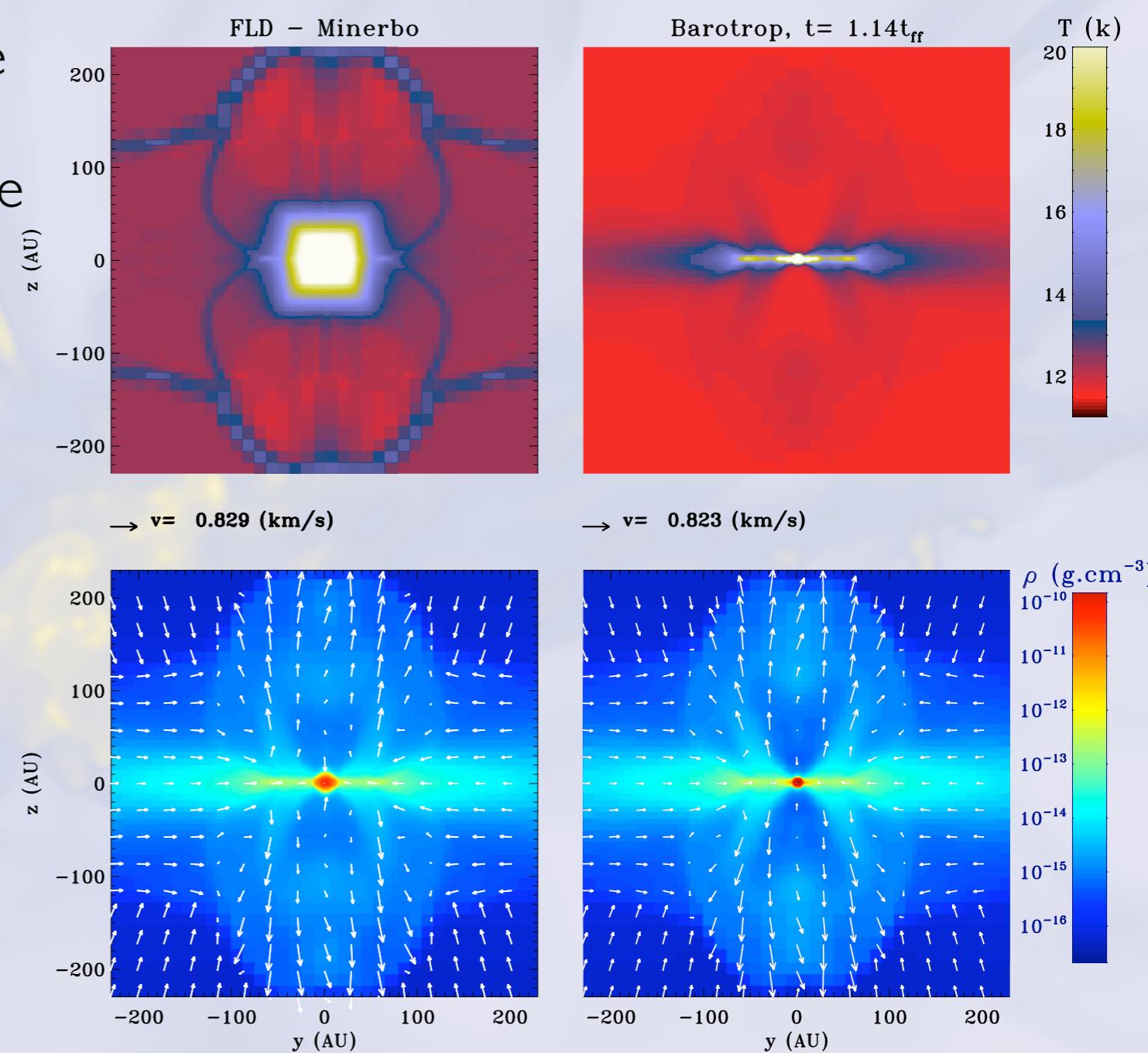
## Comparison to the barotropic case

- Hydro case: more fragmentation
- RMHD: **magnetic** braking  $\Leftrightarrow$  radiative feedback ( $L_{\text{acc}}$ )
- Significant differences in the temperature distribution

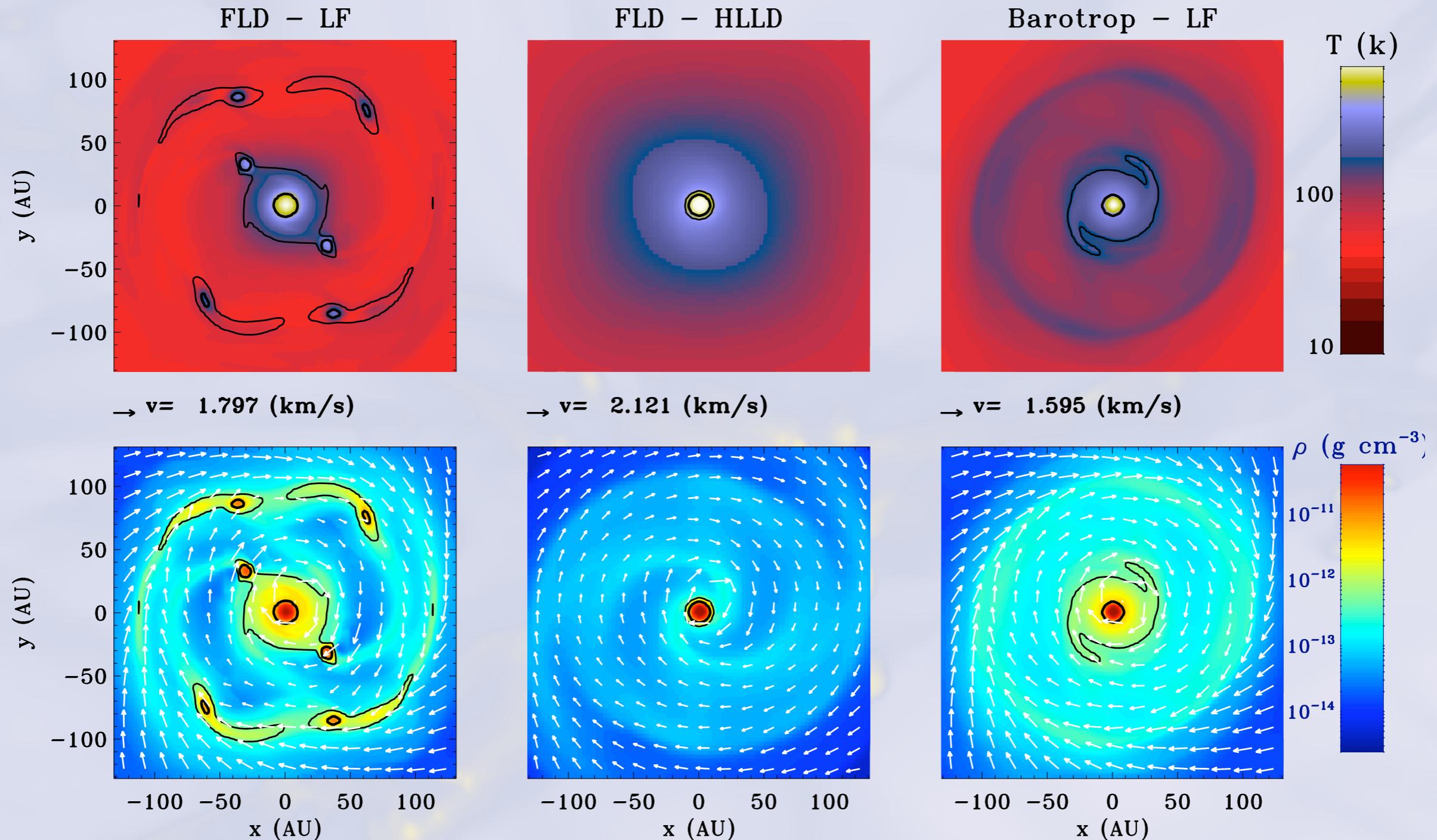
$\Leftrightarrow$  **observations**



*Commerçon et al. 2010, A&AL*



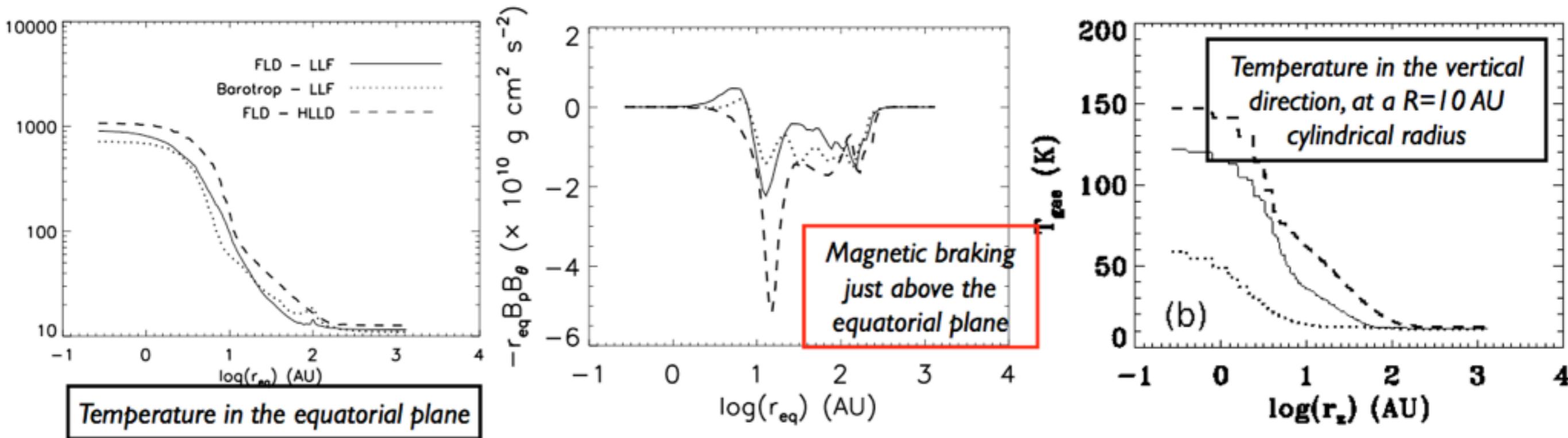
# Intermediate case, $\mu = 20$ - Numerical issue



Commerçon et al. 2010, A&AL

# Intermediate case, $\mu = 20$ - Numerical issue

Commerçon et al. 2010, A&AL



✓ Diffusivity of the solver => 2 effects that favor fragmentation:

- inefficient magnetic braking
- more massive disk

✓ Radiative feedback depends on the magnetic braking:  $L_{\text{acc}} \propto V_{\text{inf}}^3$  (supercritical radiative shock)!

# Influence of the magnetization

---

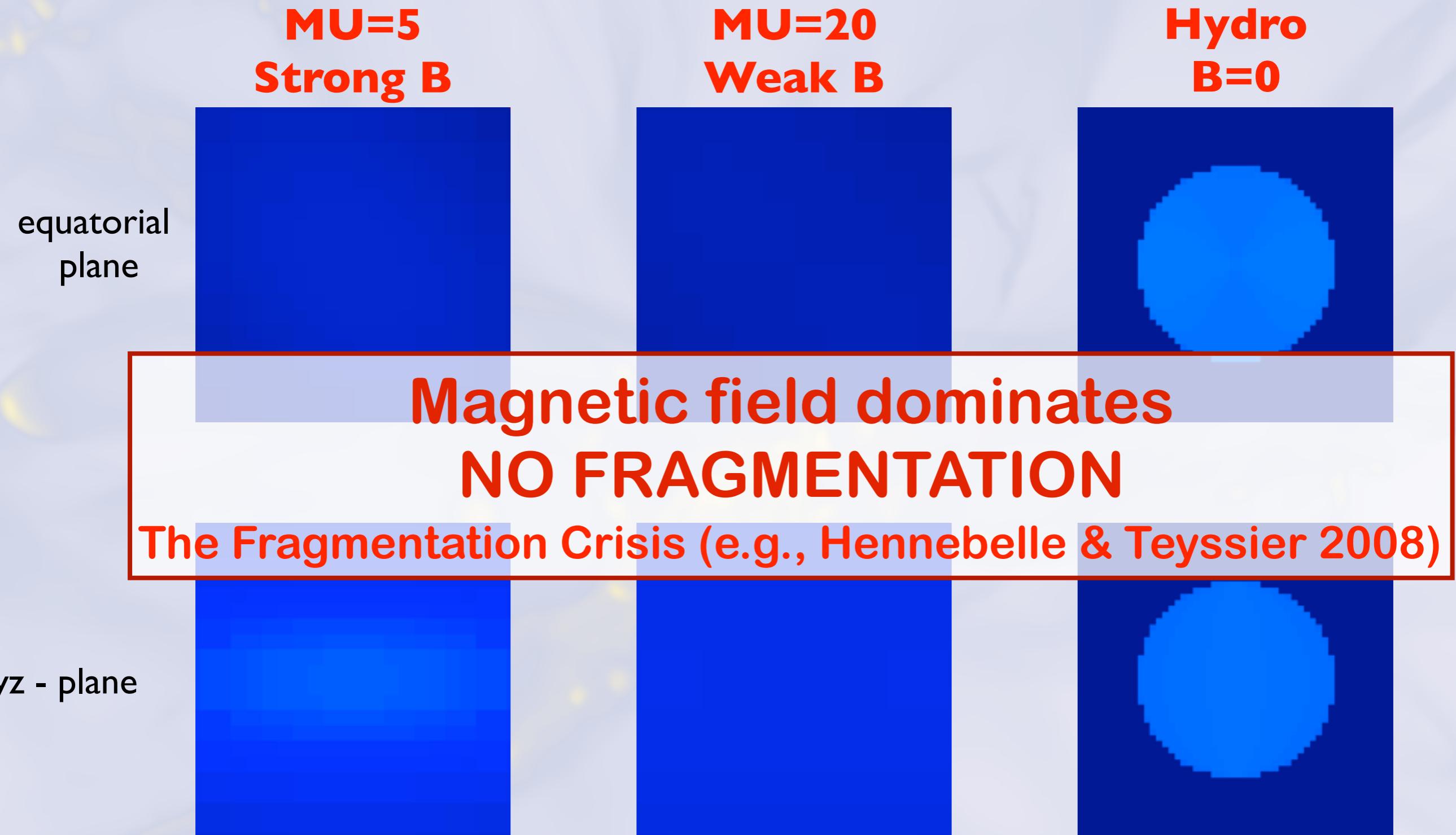


# Influence of the magnetization

---



# Influence of the magnetization



# Disk formation in magnetised cores

---

## ✓ Late formation

- end of class 0,  $M_{\text{env}} \ll M_{\text{env},0}$  (e.g., *Machida & Hosokawa 2013*)

## ✓ Misalignment

- no reason for the rotation axis and the magnetic field to be aligned (e.g., *Hull et al. 2013*)
- reduces magnetic braking efficiency (e.g. *Hennebelle & Ciardi 2009, Joos et al. 2012, Li et al. 2013*)

## ✓ Turbulent diffusion

- reconnection events fast with Ohmic diffusion only, collective effect at larger scale (e.g. *Santos Lima et al. 2012, Joos et al. 2013, Seifried et al. 2013*)

## ✓ Non-ideal MHD

- Ohm dissipation (*Tomida et al. 2013, 2015, Machida et al.*)
- Hall effect (*Krasnopol'sky et al. 2011, Tsukamoto et al. 2015, Wurster et al. 2016*)
- ambipolar diffusion (*Tsukamoto et al. 2015, Masson et al. 2016, Wurster et al. 2016*)

# Non ideal MHD

---

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left[ \mathbf{v}_n \times \mathbf{B} - \eta_\Omega (\nabla \times \mathbf{B}) - \eta_H \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{\|\mathbf{B}\|} \right\} - \eta_{AD} \frac{\mathbf{B}}{\|\mathbf{B}\|} \times \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{\|\mathbf{B}\|} \right\} \right]$$

## Non-ideal effects:

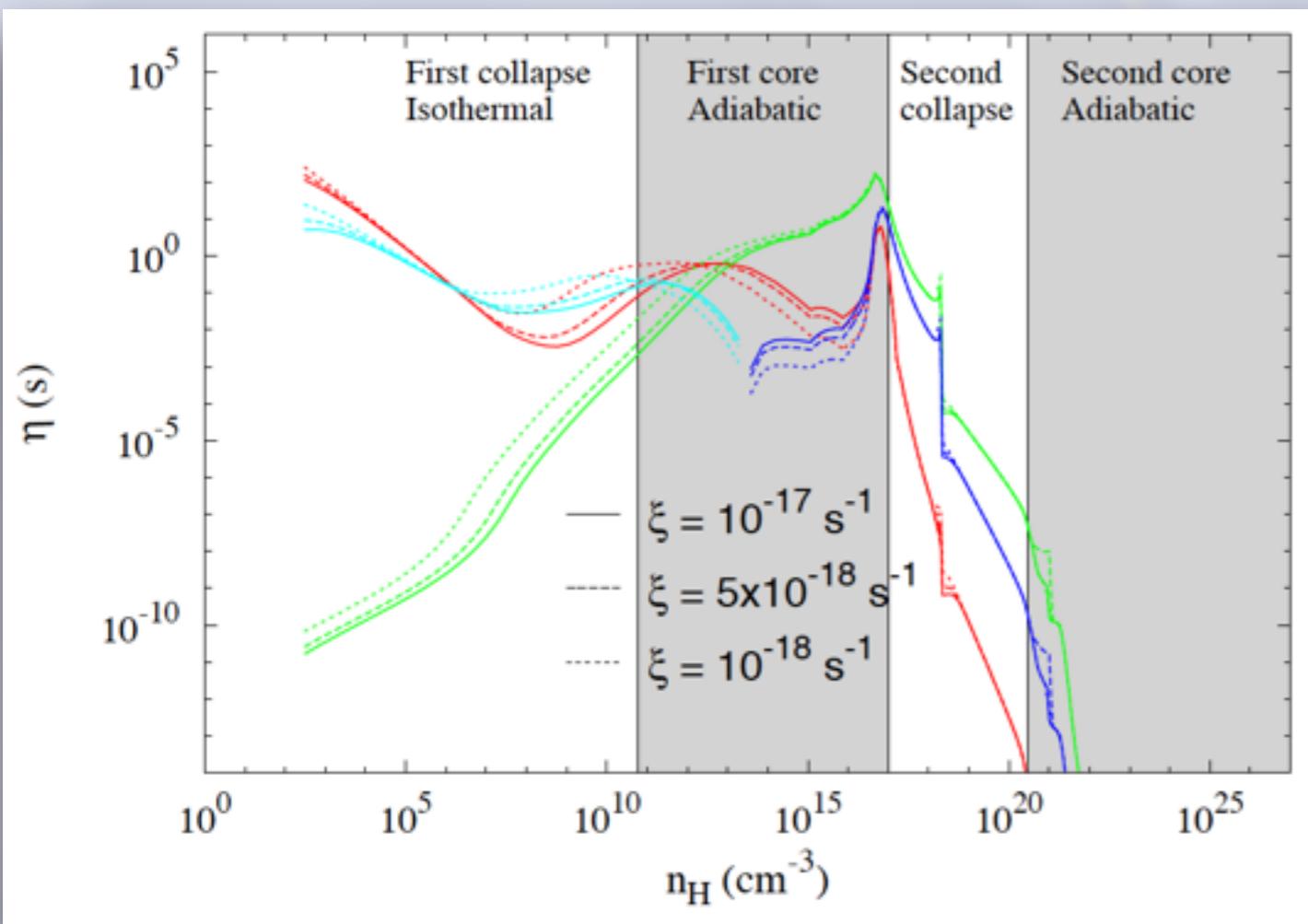
- rearrangement of magnetic field lines
- reconnection
- magnetic flux diffusion
- ... needs gas-grain chemistry

# Non ideal MHD

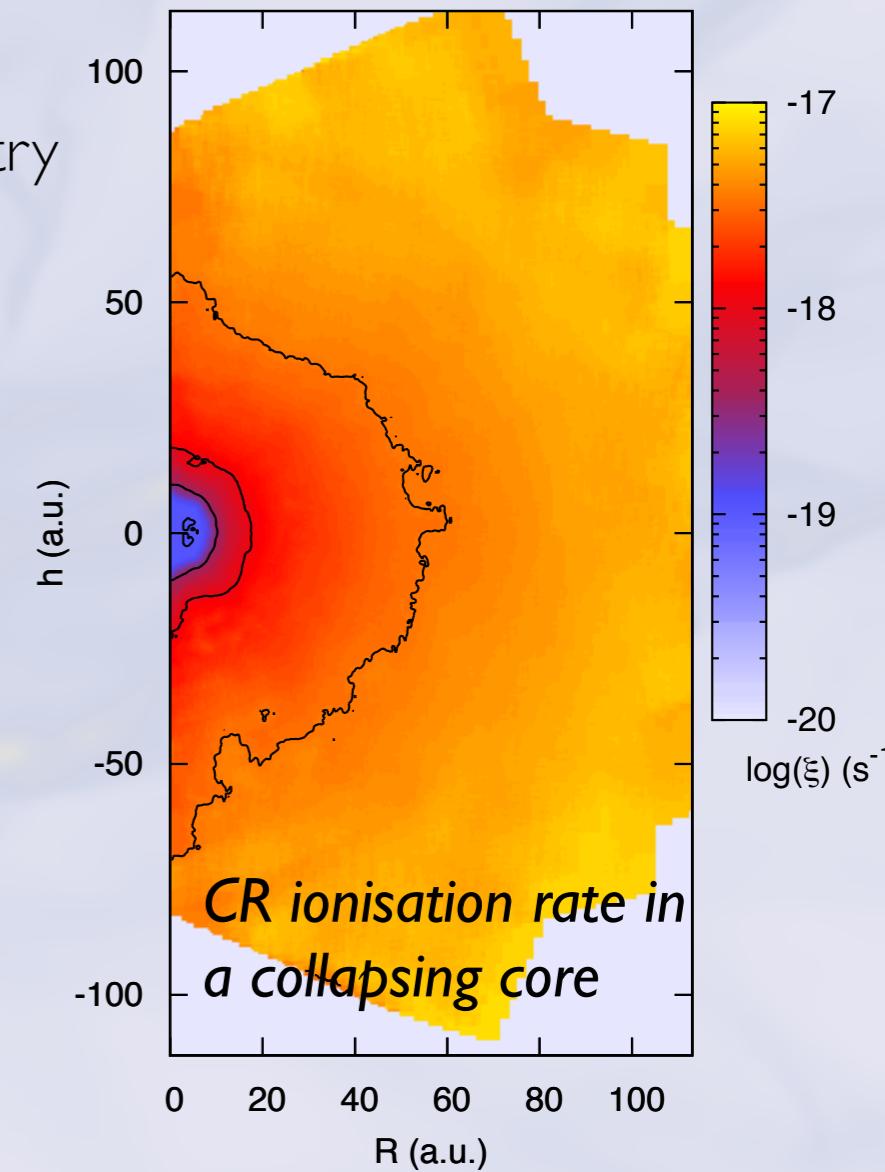
$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left[ \mathbf{v}_n \times \mathbf{B} - \eta_\Omega (\nabla \times \mathbf{B}) - \eta_H \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{\|\mathbf{B}\|} \right\} - \eta_{AD} \frac{\mathbf{B}}{\|\mathbf{B}\|} \times \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{\|\mathbf{B}\|} \right\} \right]$$

## Non-ideal effects:

- rearrangement of magnetic field lines
- reconnection
- magnetic flux diffusion
- ... needs gas-grain chemistry



Marchand et al. (2016)

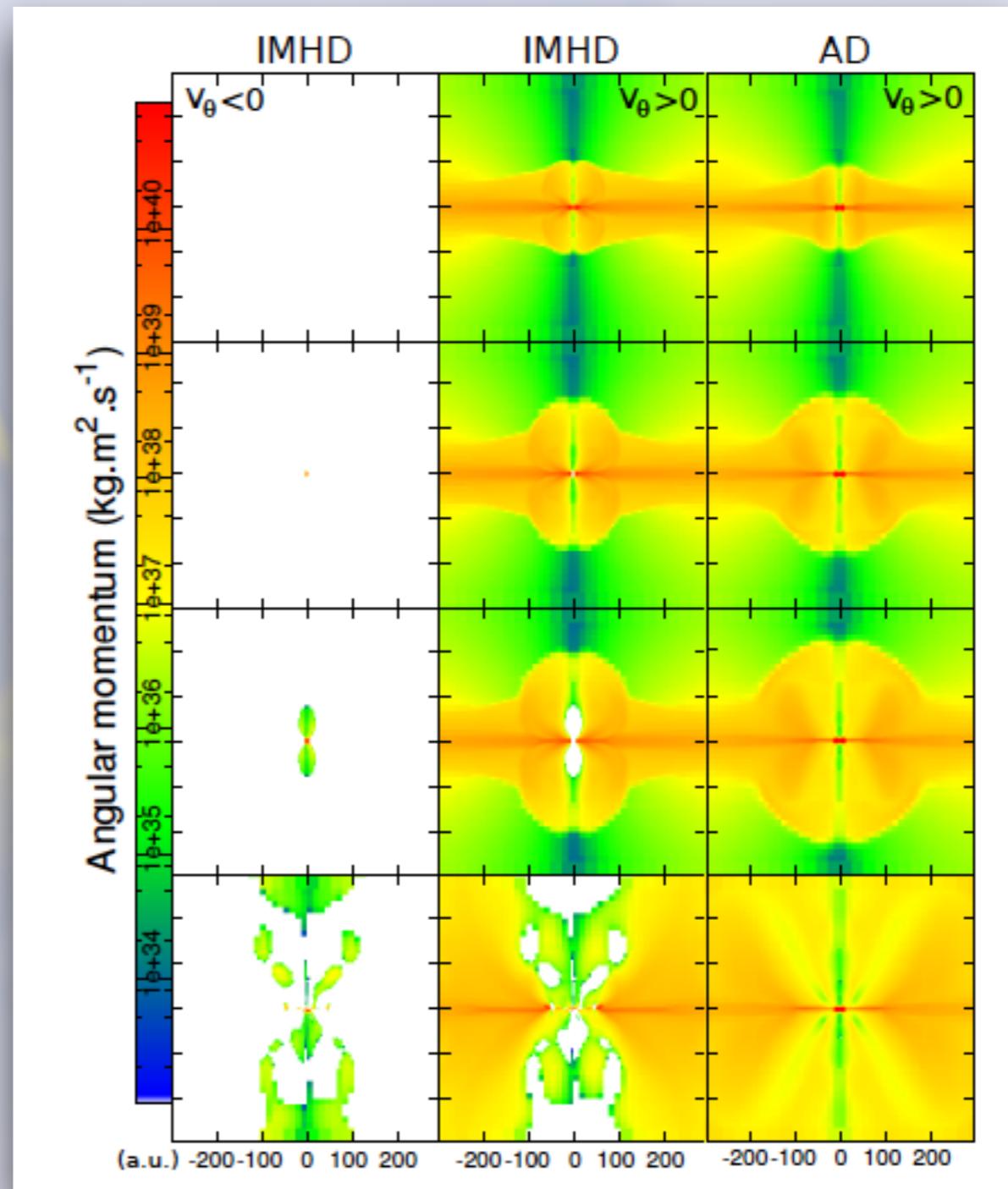


- 1/ **Grain evaporation** is the **most** important effect
- 2/ Needs at least 20 bins in dust grain size distribution to converge...

# Influence of non-ideal MHD

## Rotation and interchange instability

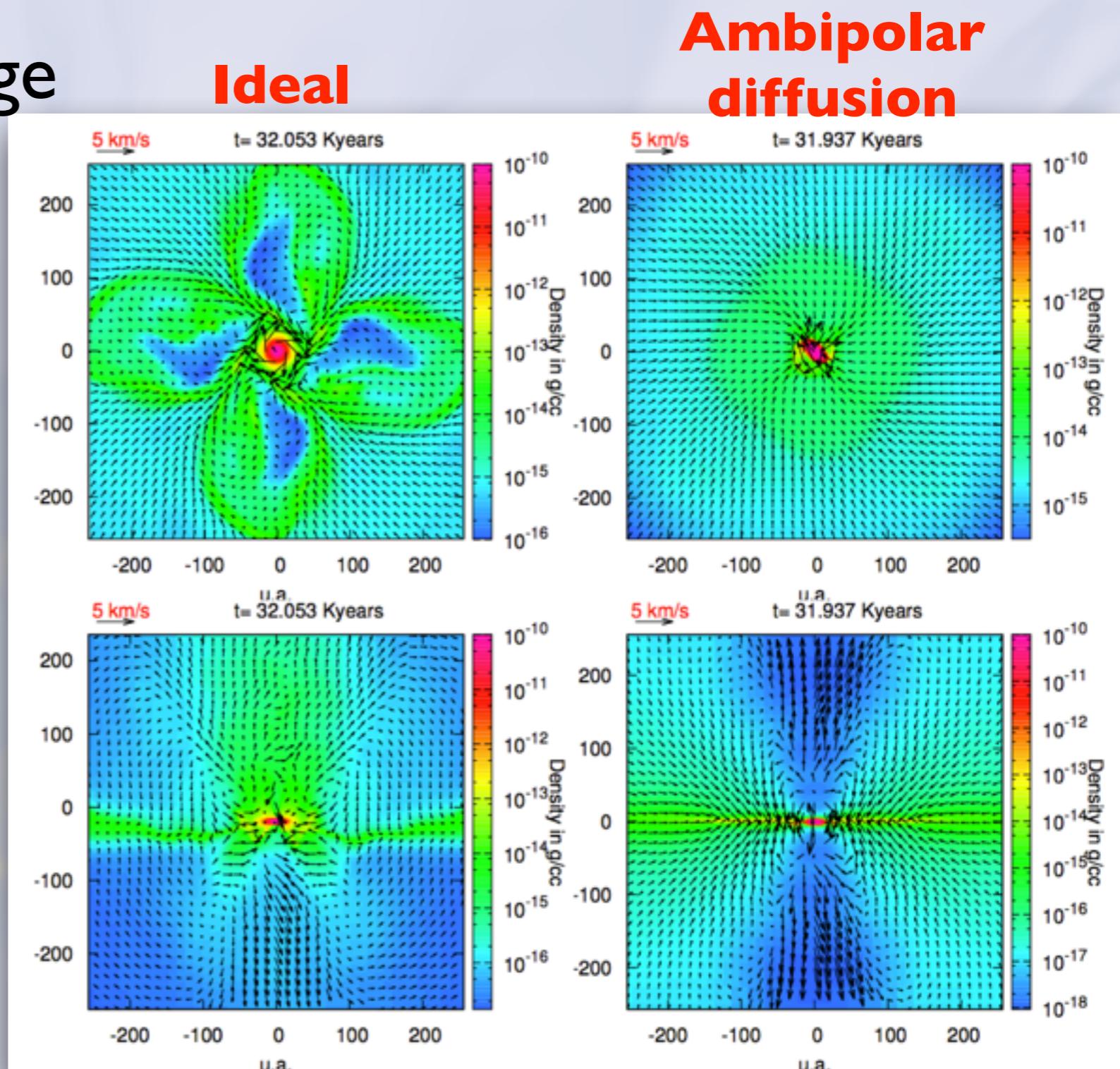
- reduce magnetic braking  
(suppress counter-rotation found in ideal MHD)



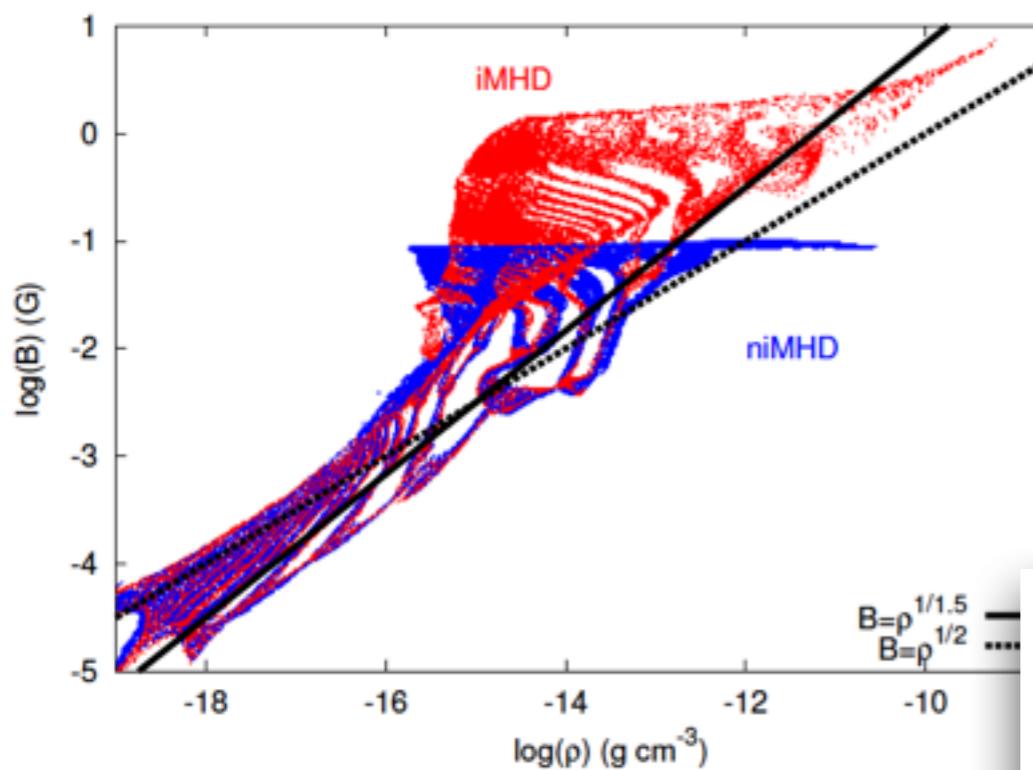
# Influence of non-ideal MHD

## Rotation and interchange instability

- reduce magnetic braking  
(suppress counter-rotation found in ideal MHD)
- reduce development of interchange instability
- changes at the first core scale
- diffusion is \*controlled\*

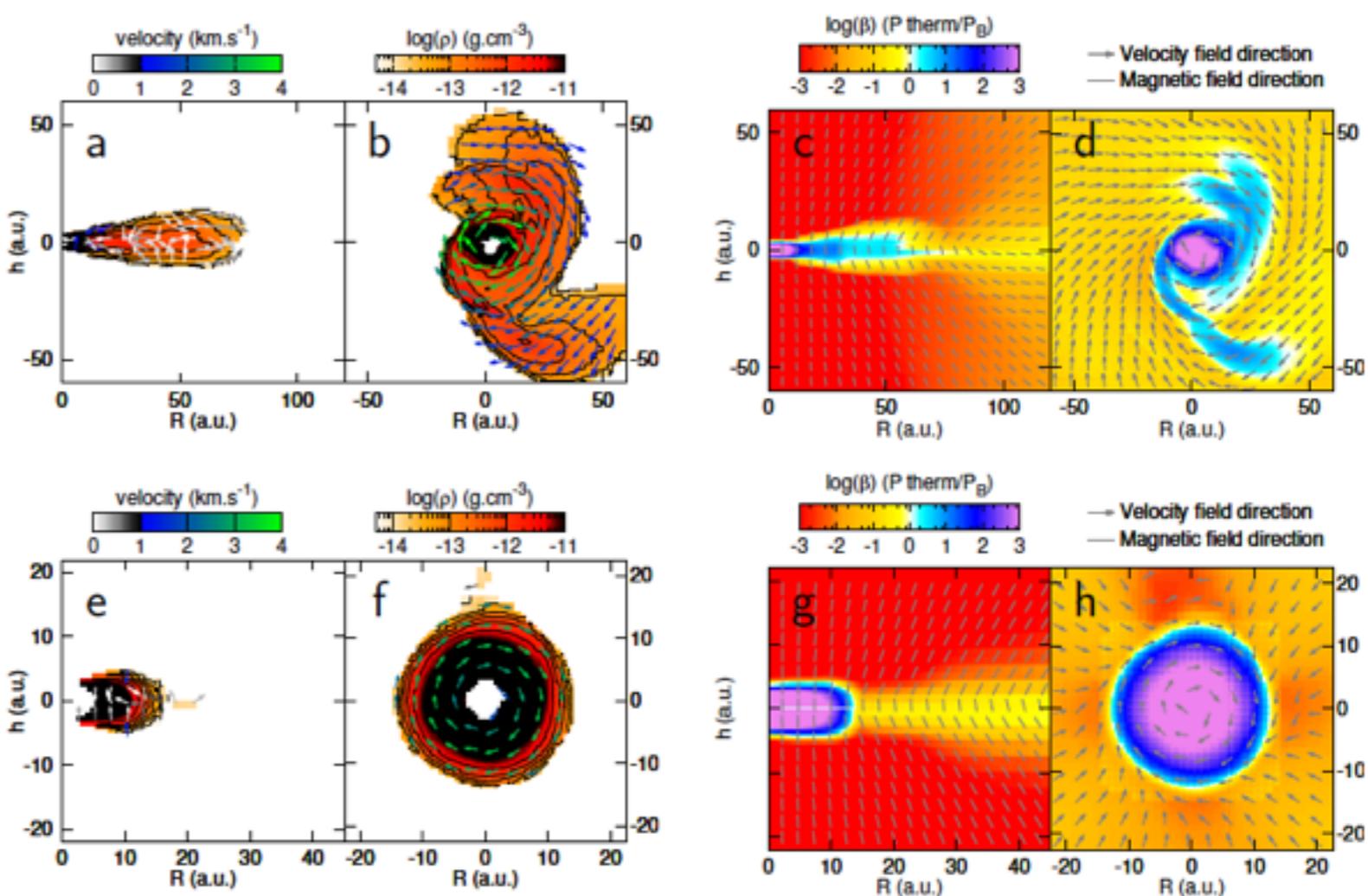


# Misalignment & ambipolar diffusion

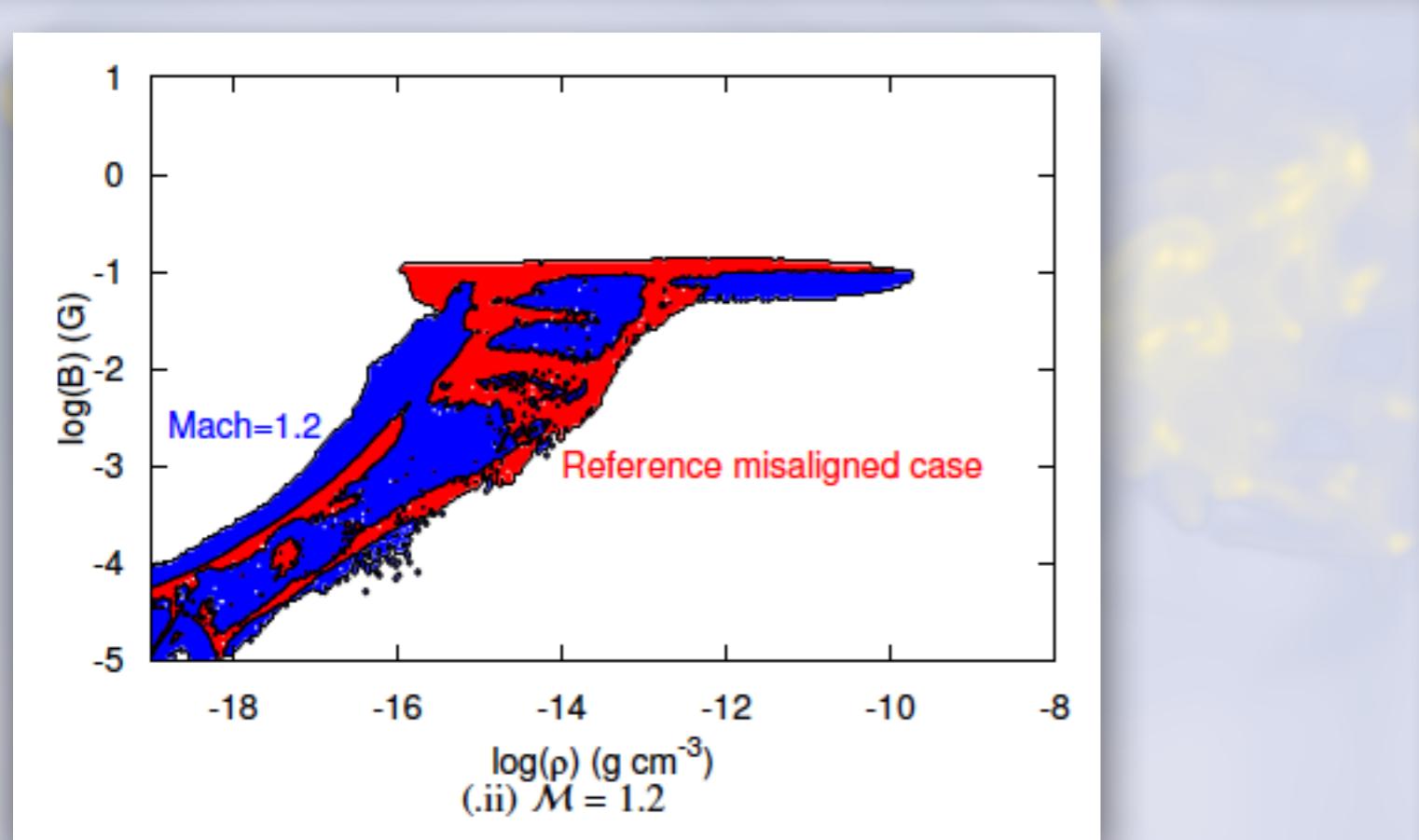
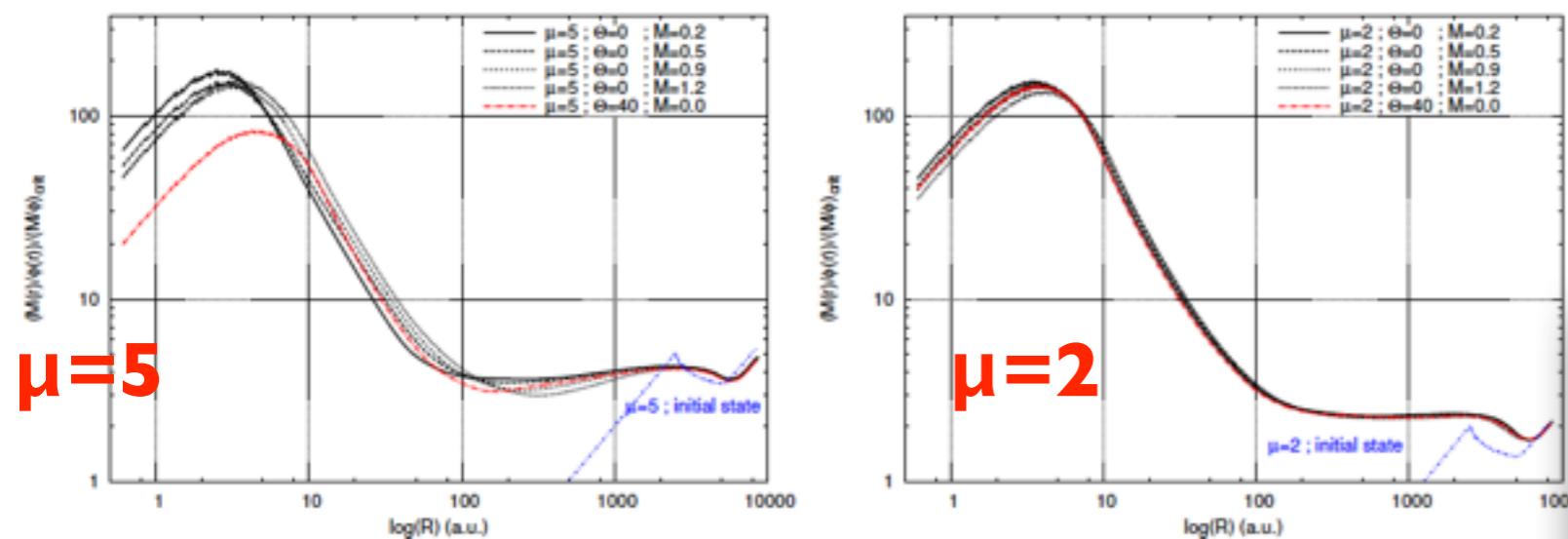


- Rotationally supported disk formation ( $R \sim 50$  AU) - consistent with obs.
- disk size **depends** on misalignment
- $P_{\text{therm}}/P_{\text{mag}} > 1$  within disks
- **poloidal** magnetic field  
 => initial conditions for protoplanetary disks studies

Masson et al. 2016

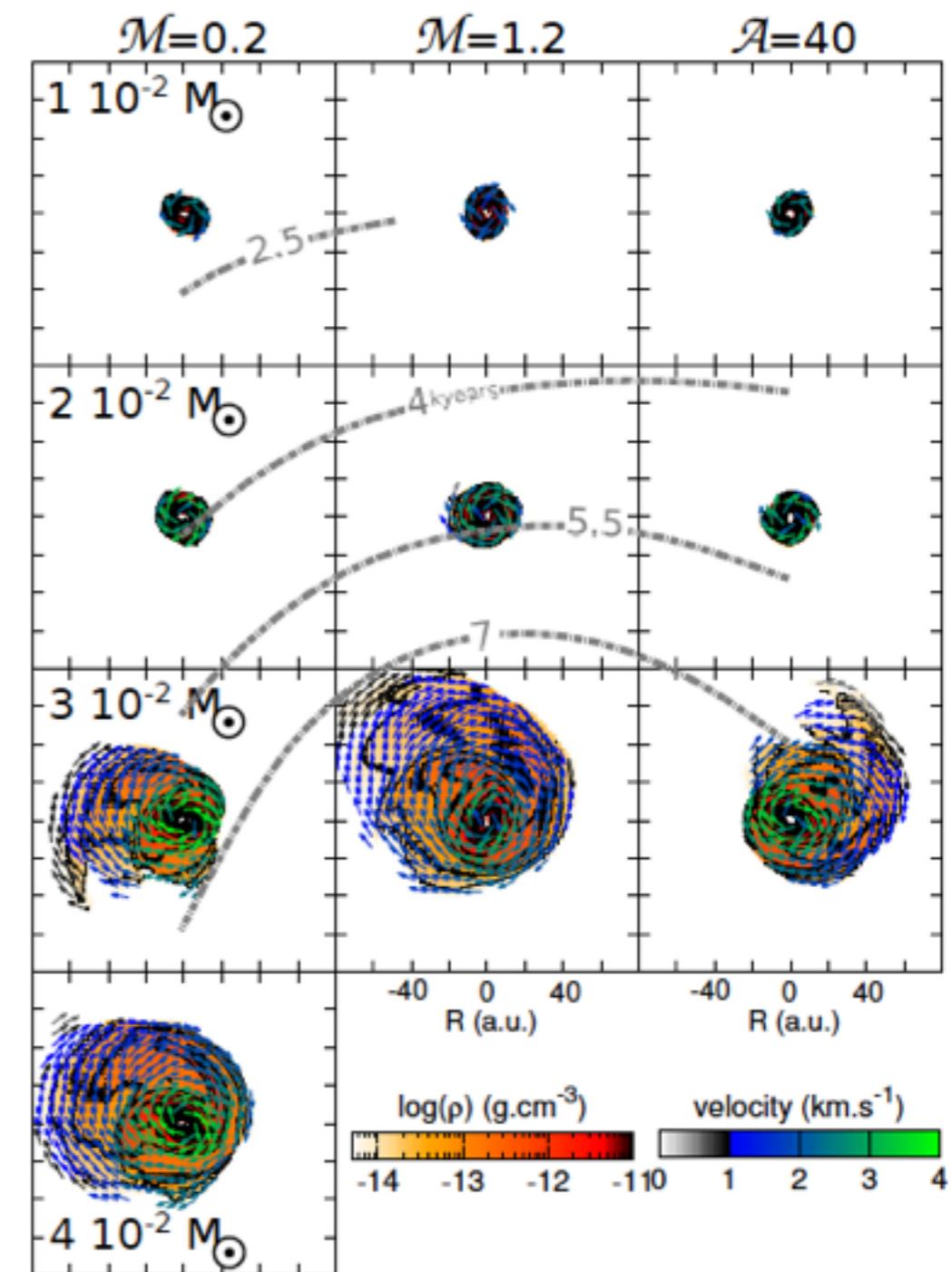


# Turbulence & ambipolar diffusion

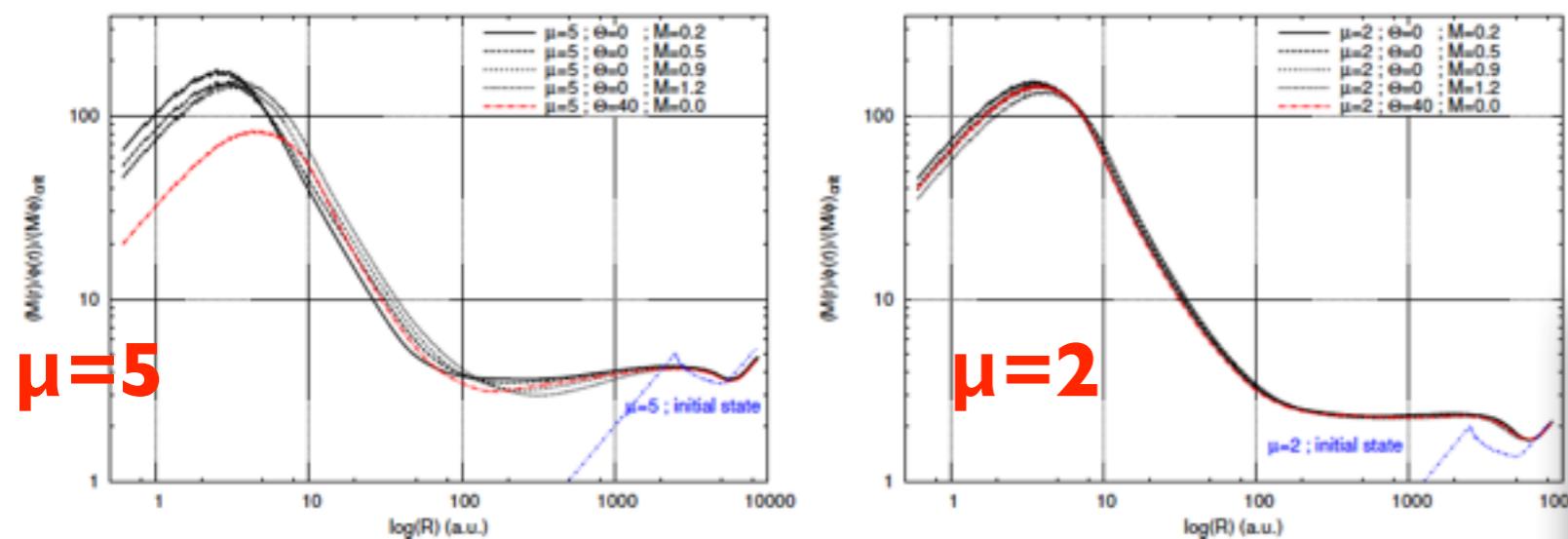


Masson et al. in prep.

- disk size **does not depend** on turbulence level  
=> combination between turbulent diffusion and ambipolar diffusion?

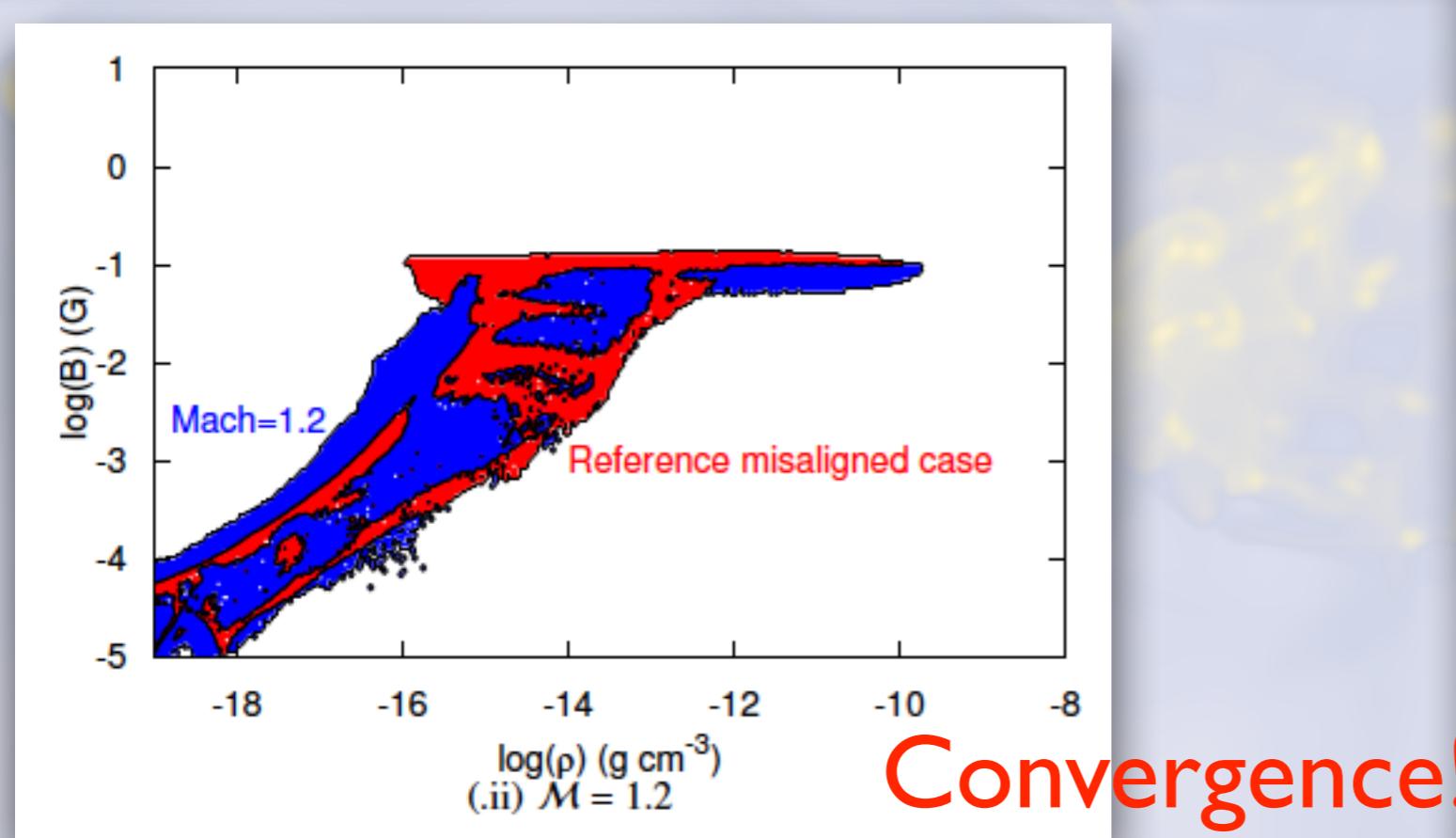


# Turbulence & ambipolar diffusion



$\mu=5$

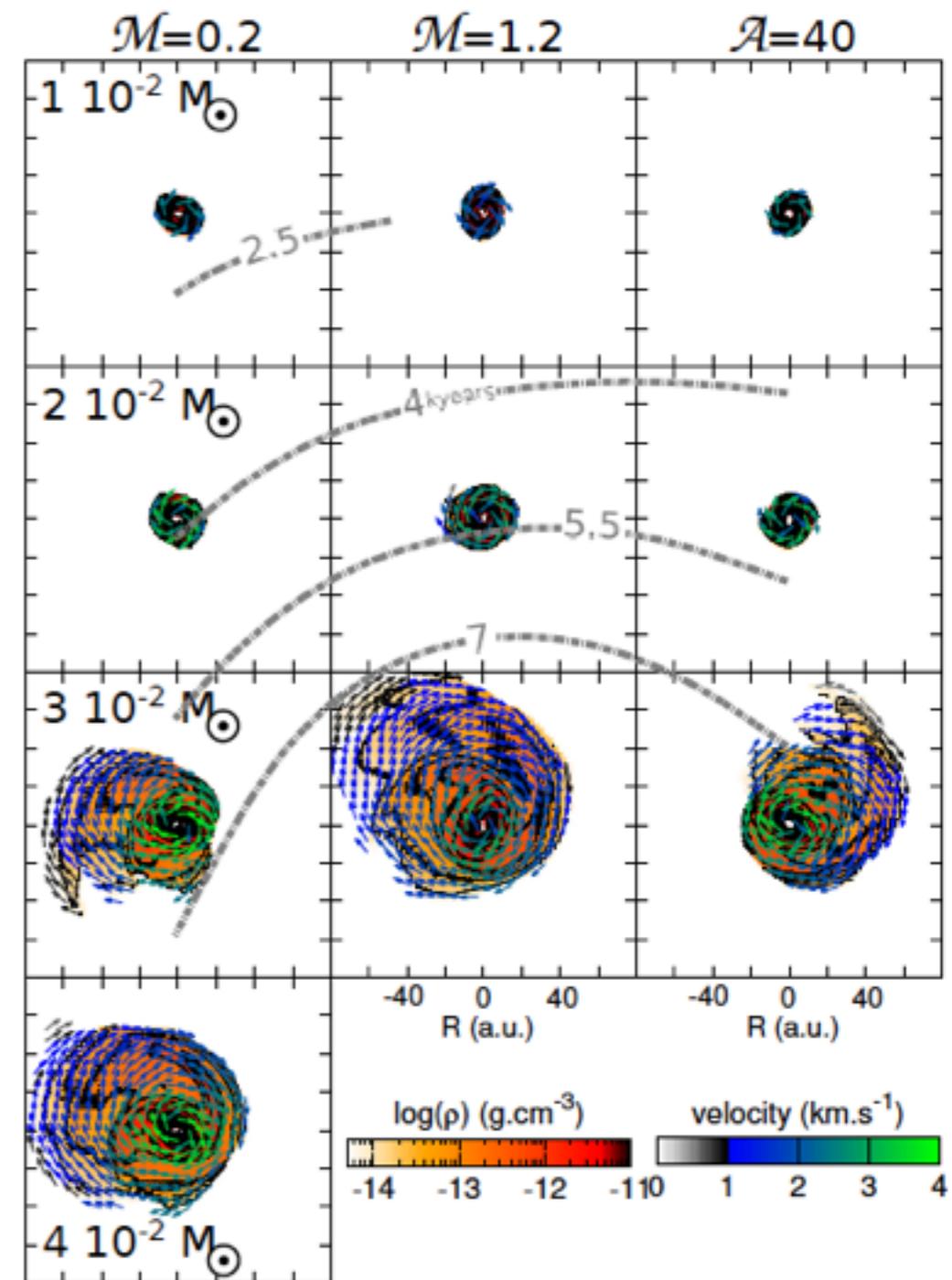
$\mu=2$



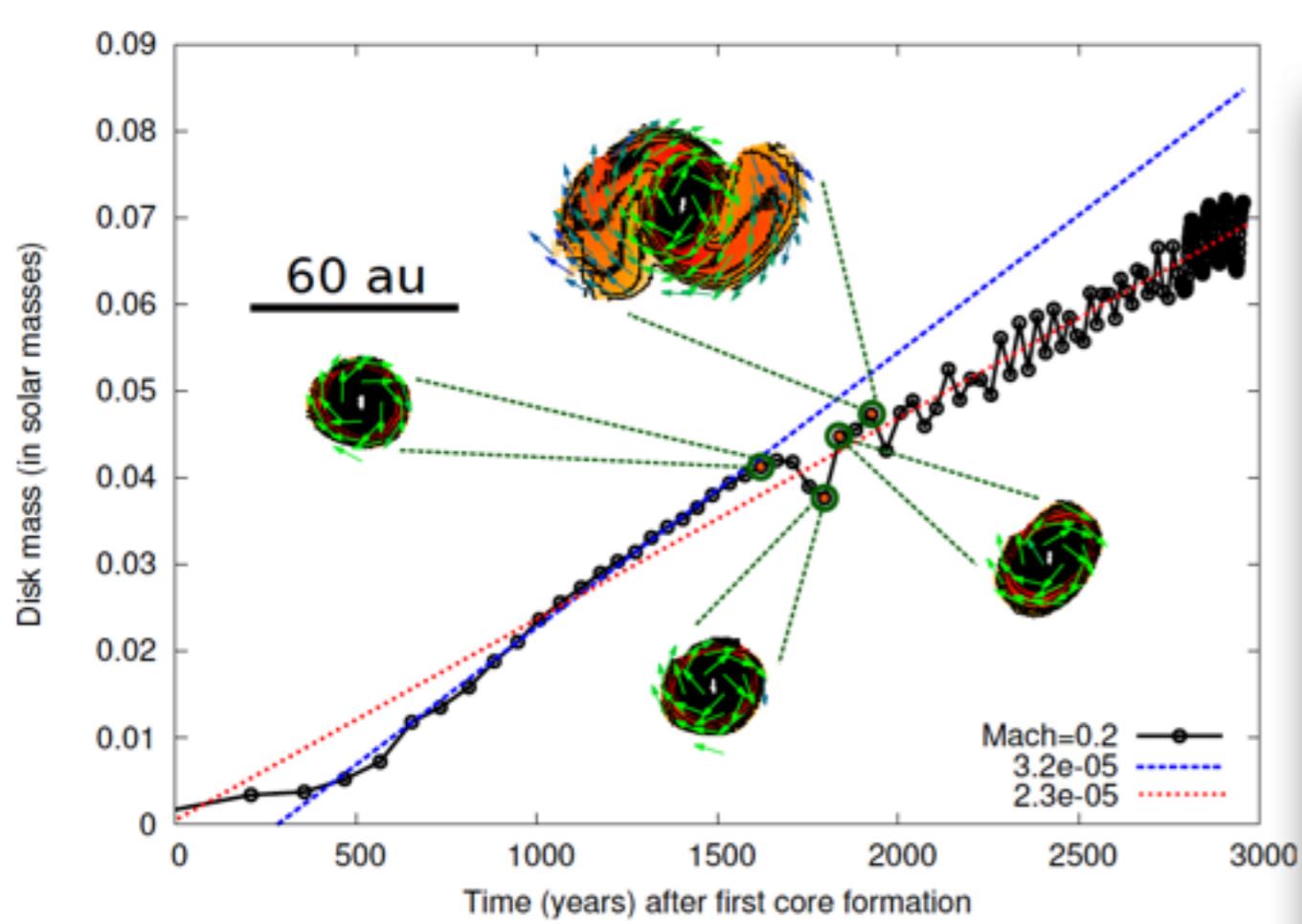
Convergence!

Masson et al. in prep.

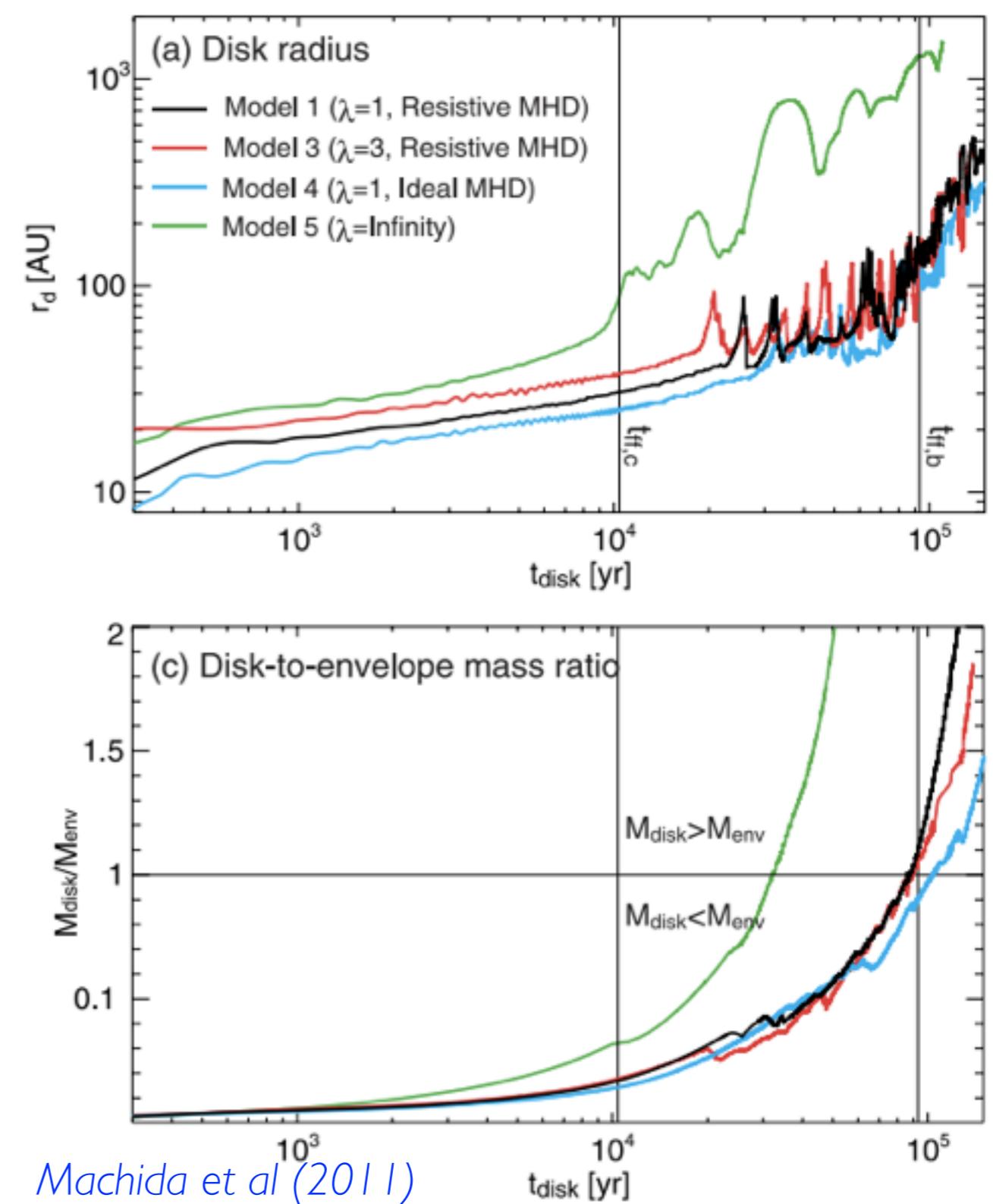
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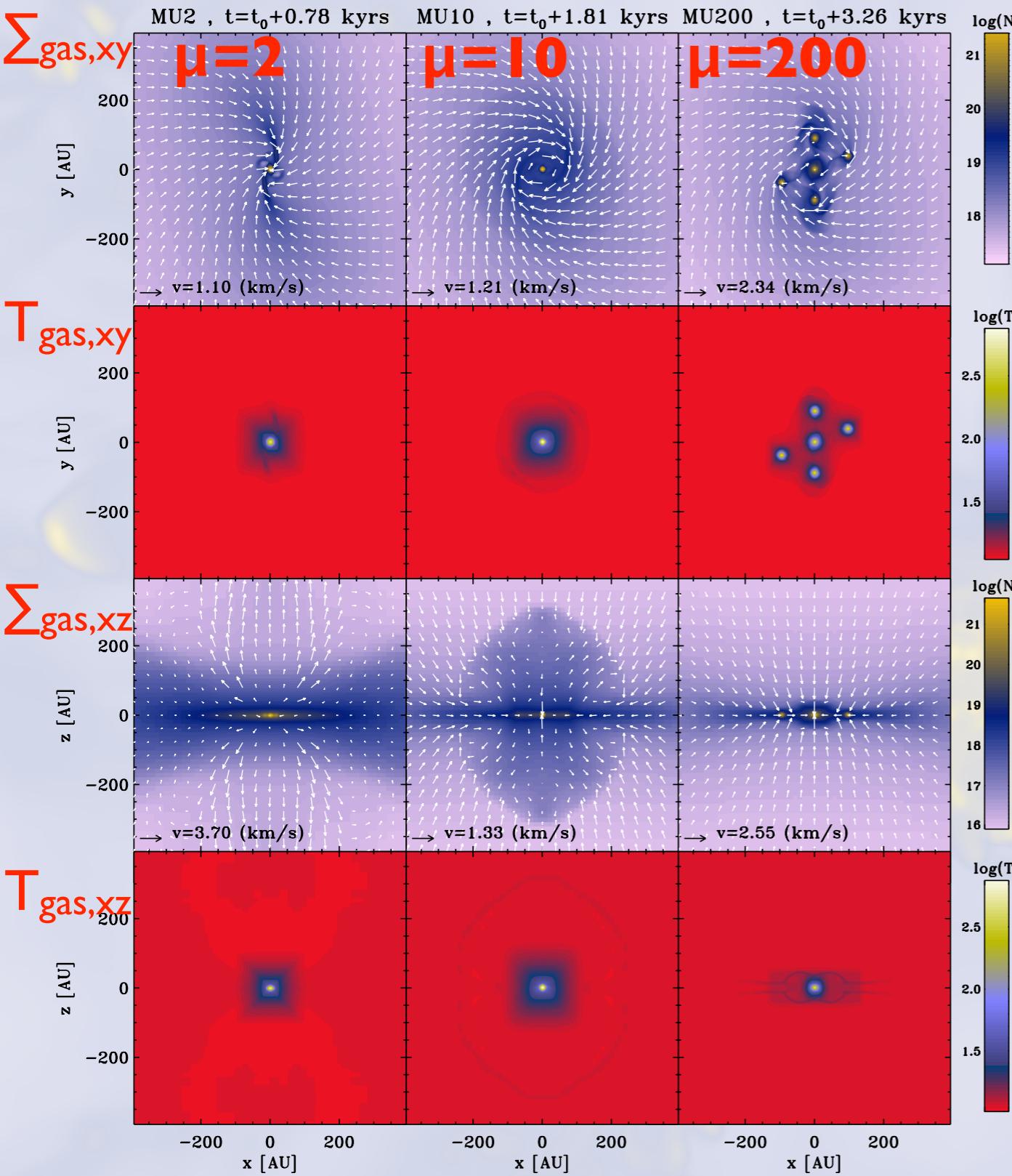
# Late evolution



Masson et al. in prep.



# Towards synthetic observations



- 3 representative cases

**MU2:** pseudo-disk + outflow

**MU10:** disk + pseudo-disk + outflow

**MU200:** disk + fragmentation

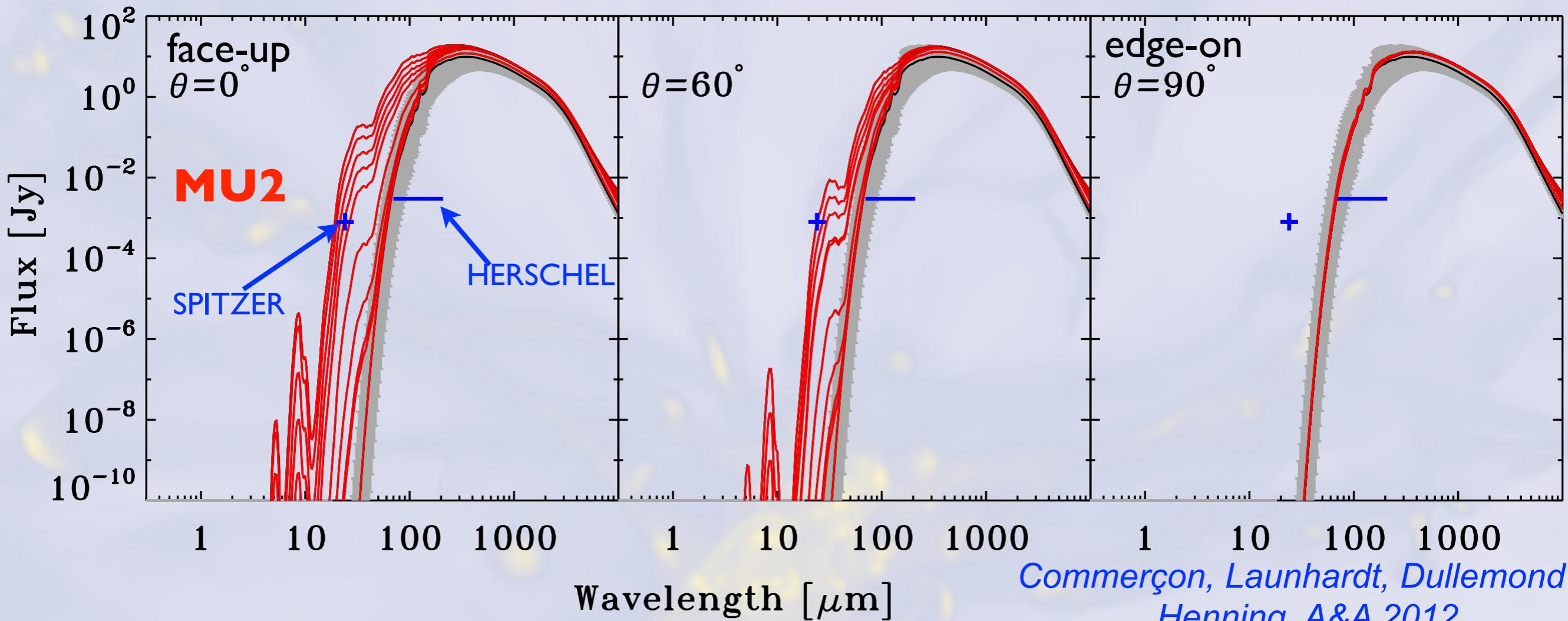
- First core lifetime:

<b>MU2</b>	<b>MU10</b>	<b>MU200</b>
1.2 kyr	3 kyr	> 4 kyr

- Images & SED computed with the radiative transfer code **RADMC-3D**, developed by C. Dullemond (ITA Heidelberg)

-  $T_{\text{dust}} = T_{\text{gas}}$  (given by the RMHD calculations)

# SED - Do we see a first core signature?

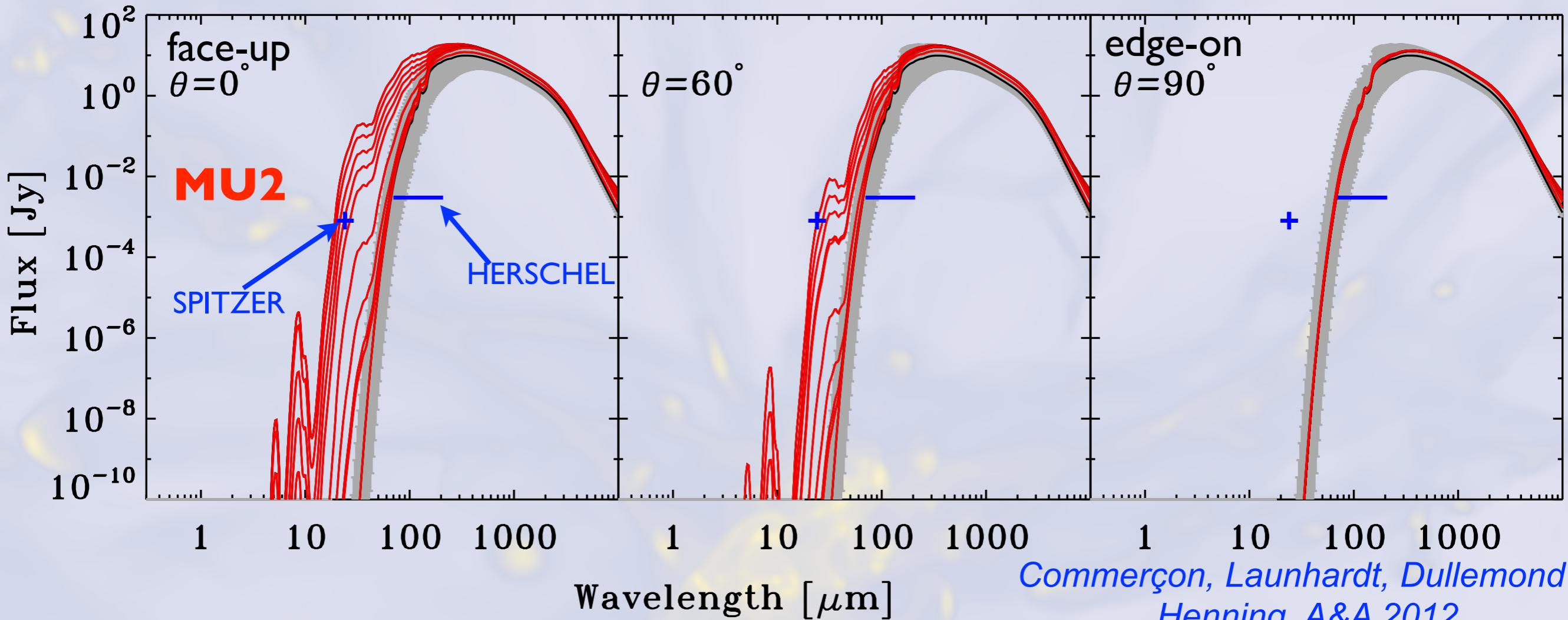


Commerçon, Launhardt, Dullemond &  
Henning, A&A 2012

- Objects at 150 pc, 3000 AU  $\times$  3000 AU region
- Prestellar core = initial conditions (black line)
- Emission in the FIR => **HERSCHEL, SPITZER**
- But similar SEDs in the MU200 model, i.e. **with a disk!**  
=> Issues in SED-fitting models for early Class 0?

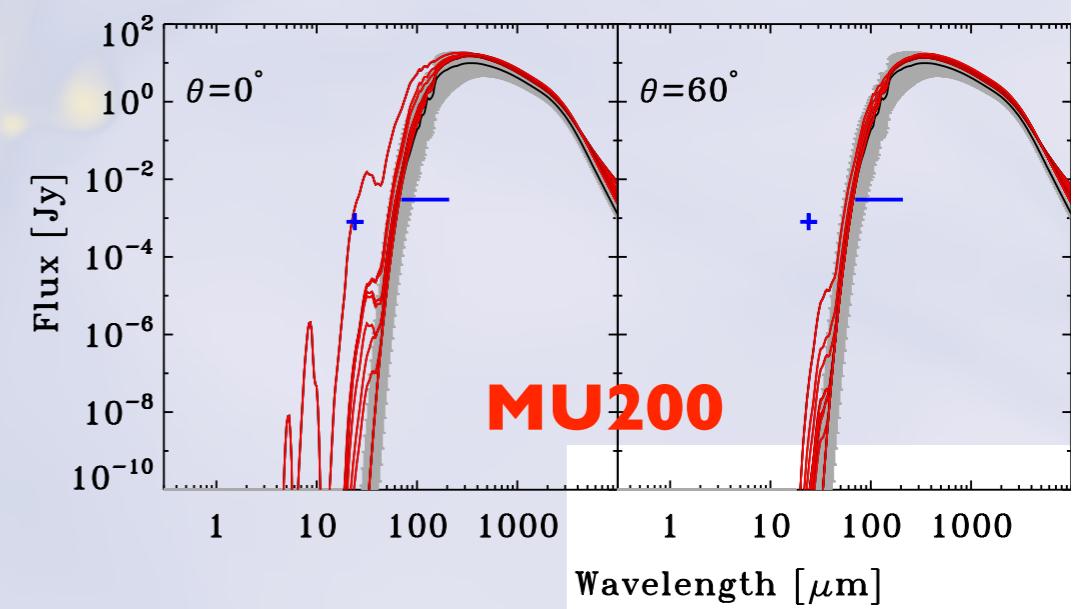
Help to select first core candidates & to distinguish  
starless cores and first cores

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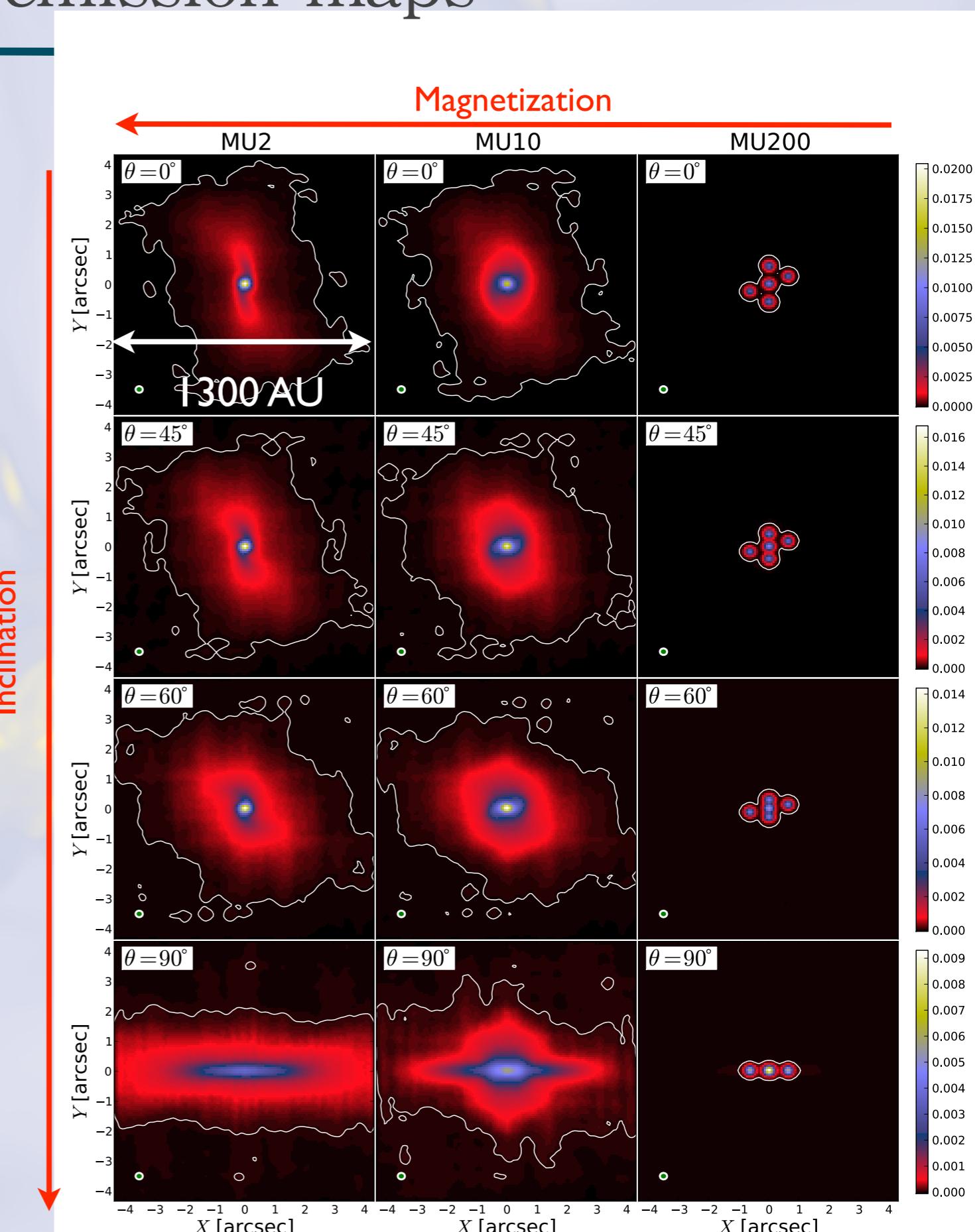
Help to select first core candidates & to distinguish starless cores and first cores



# Synthetic ALMA dust emission maps

ALMA Band 3 Config 20 @ 150 pc

Commerçon, Levrier et al. A&A, 2012



# Take Away I

---

- ✓ Fragmentation crisis at the Class 0 stage for low mass star formation - No massive, extended & **fragmented** disk
- ✓ Magnetic field cannot be neglected
- ✓ Supported by observations, no large disks (e.g. Maury et al. 2010)

# Outline

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## 1. Introduction

## 2. Methods

- AMR vs. SPH

## 3. Low mass dense core collapse

- RHD and RMHD collapse
- Disk formation and fragmentation crisis
- Synthetic observations

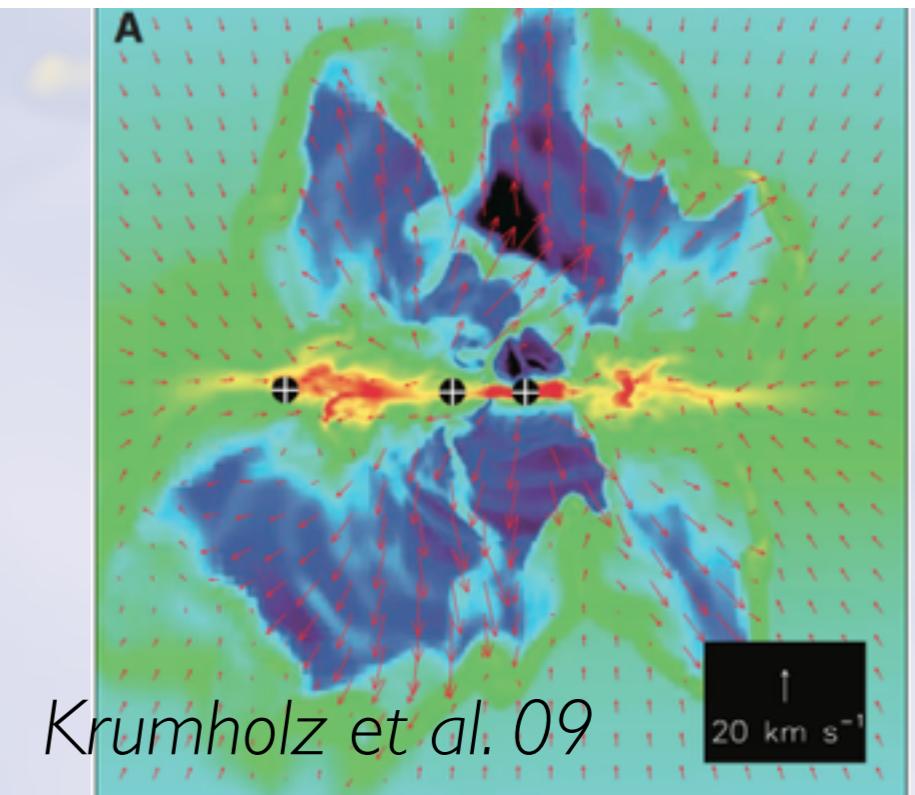
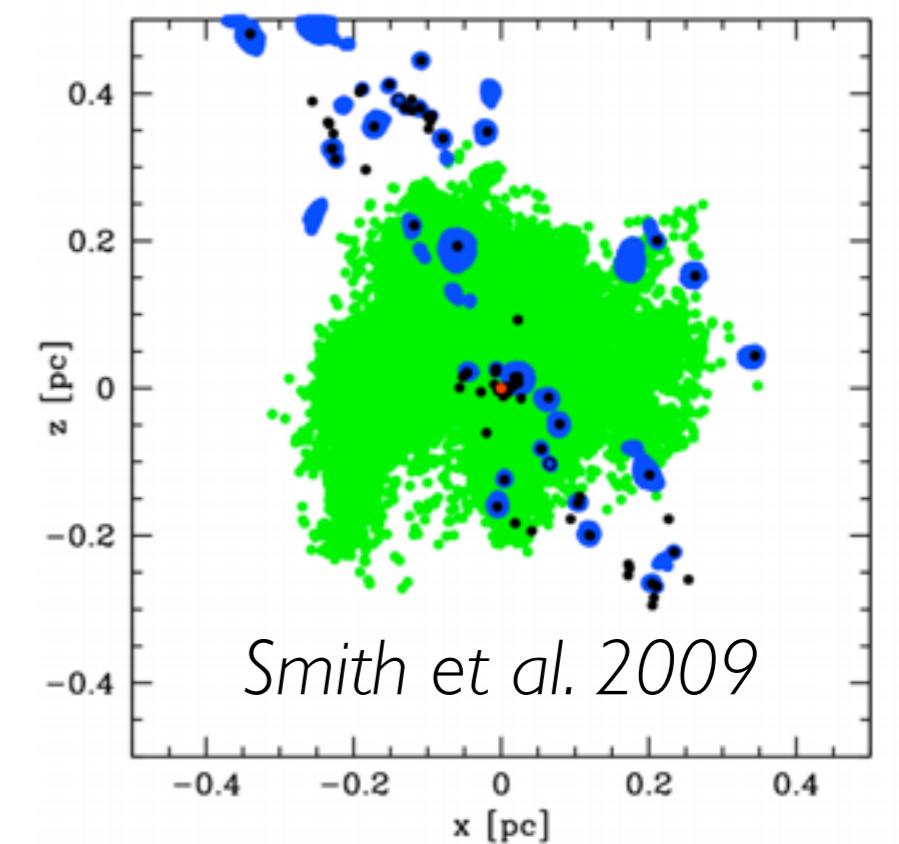
## 4. Massive dense cores collapse

- Early fragmentation inhibition
- Disk & outflow formation

# High mass star formation scenarii

- **Competitive accretion (Bate, Bonnell et al.)**
  - Massive prestellar core does not exist
  - Star clusters and massive stars form simultaneously (*Smith et al. 2009*)
- **Gravitational collapse (Krumholz et al.)**
  - Massive prestellar does exist
  - Fragmentation suppressed by protostellar feedback
  - Column density threshold  $\Sigma=1 \text{ g cm}^{-2}$

(Krumholz & McKee 2008)
- **But... to date:**
  - Magnetic field neglected
  - More or less crude resolution
  - Initial fragmentation



# 100 $M_\odot$ turbulent dense core collapse

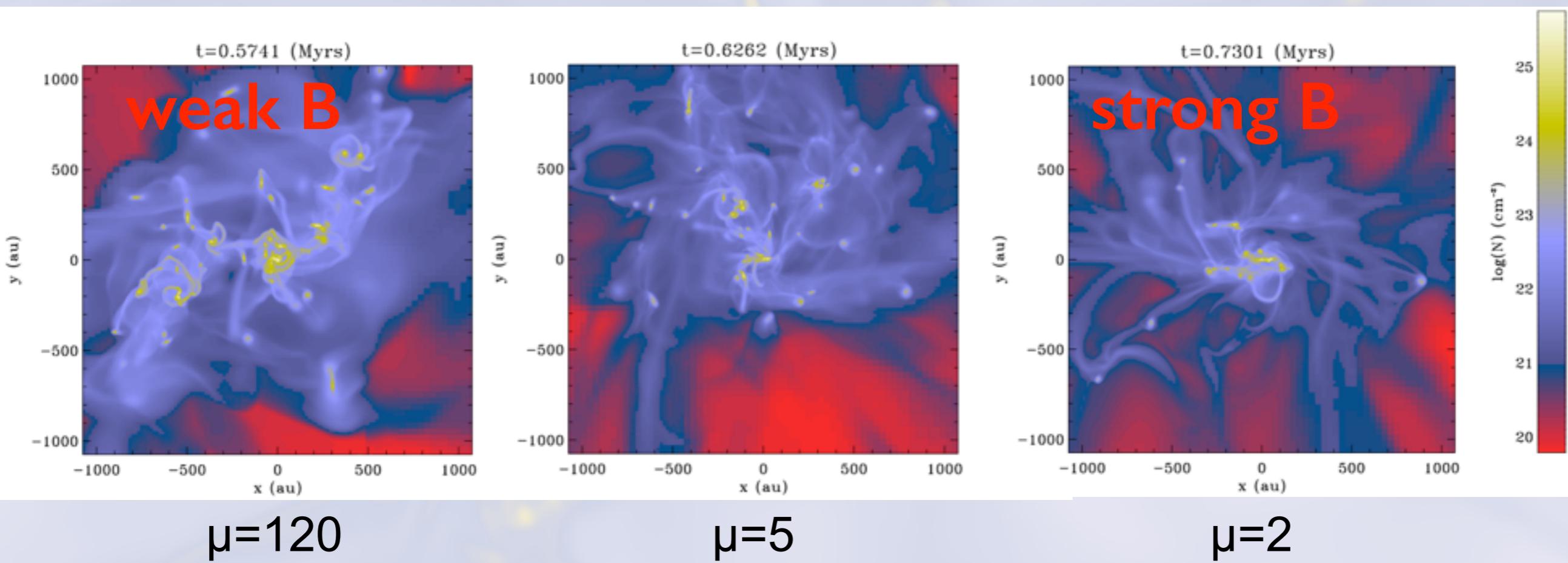
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**High-mass star formation: 100  $M_\odot$  magnetized, turbulent and dense core w. FLD** (follow-up of Hennebelle et al. 2011 barotropic study)  
==> Influence of the magnetic field strength and radiative transfer on collapse, outflow launching and fragmentation

- $T_0 = 10 \text{ K}$
- Kolmogorov initial power spectrum  
$$P(k) \propto k^{-5/3}$$
- Flat profile  
$$\rho(r) = \frac{\rho_c}{1 + (r/r_0)^2}$$
$$\rho_c = 1.4 \times 10^{-20} \text{ g cm}^{-3}$$
$$r_0 \sim 0.22 \text{ pc}$$

# 100 $M_{\odot}$ turbulent dense core collapse

**High-mass star formation: 100  $M_{\odot}$  magnetized, turbulent and dense core w. FLD** (follow-up of Hennebelle et al. 2011 barotropic study)  
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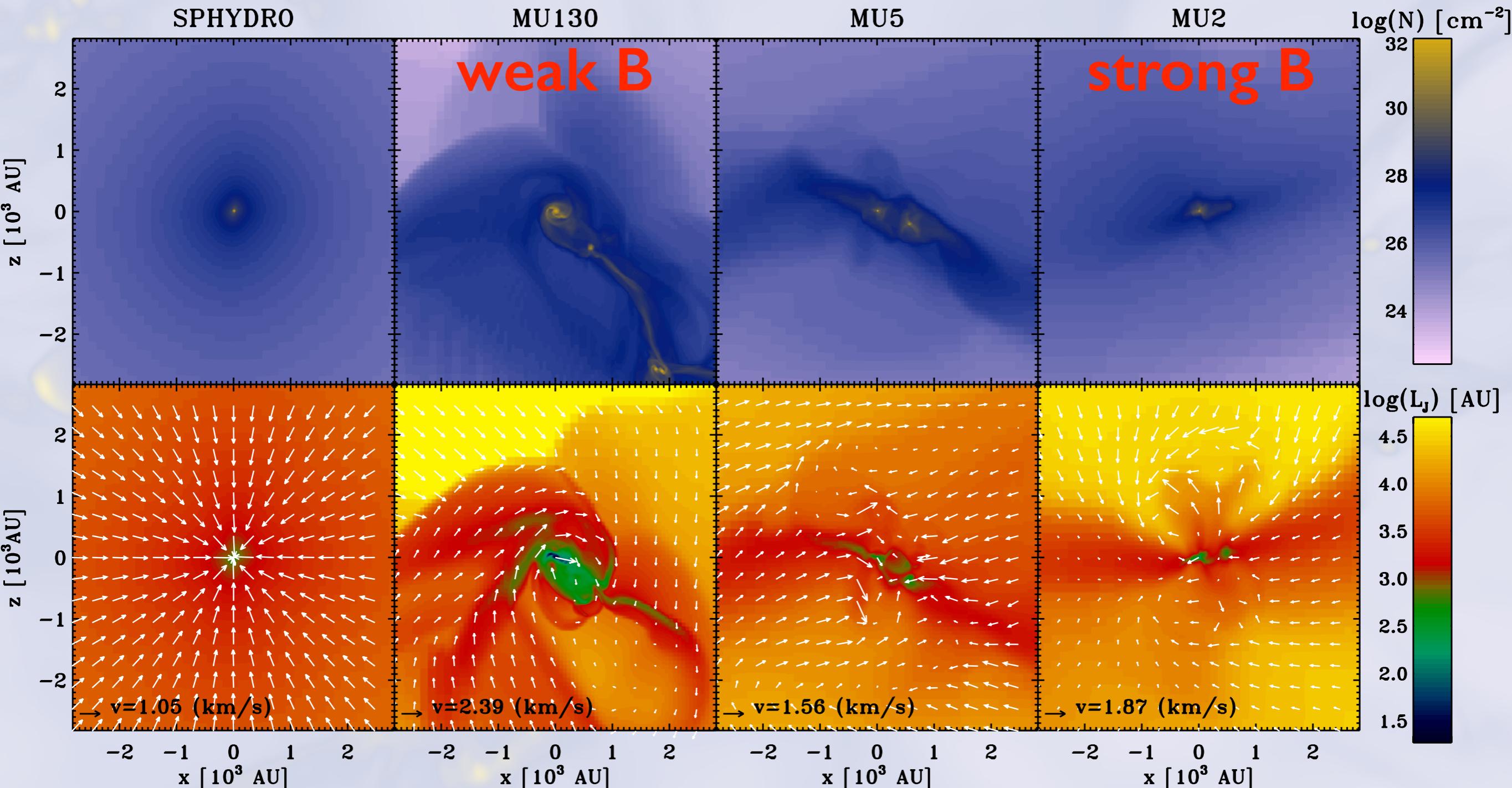
Hennebelle et al. 2011

# 100 $M_{\odot}$ turbulent dense core collapse

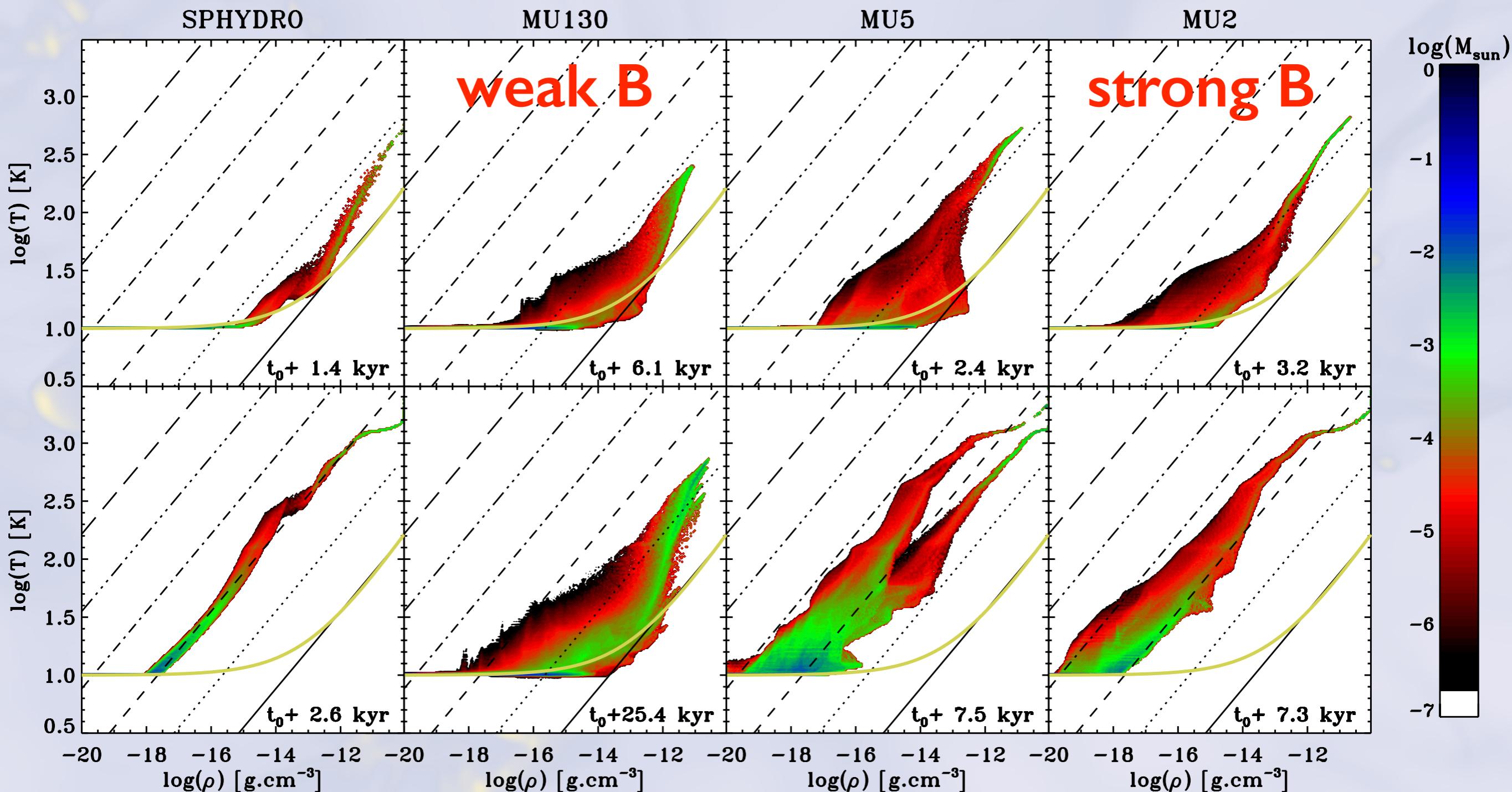
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Model	$\mu$	$\alpha_{\text{turb}}$	$\Delta x_{\min}$ (AU)	Coarse grid	$t_0$ (Myr)
SPHYDRO	$\infty$	$\sim 10^{-5}$	2.16	$128^3$	0.4786
MU130	$\sim 136$	$\sim 0.2$	2.16	$256^3$	0.4935
MU5	$\sim 5.3$	$\sim 0.2$	2.16	$256^3$	0.5397
MU2	$\sim 2.3$	$\sim 0.2$	2.16	$256^3$	0.5982

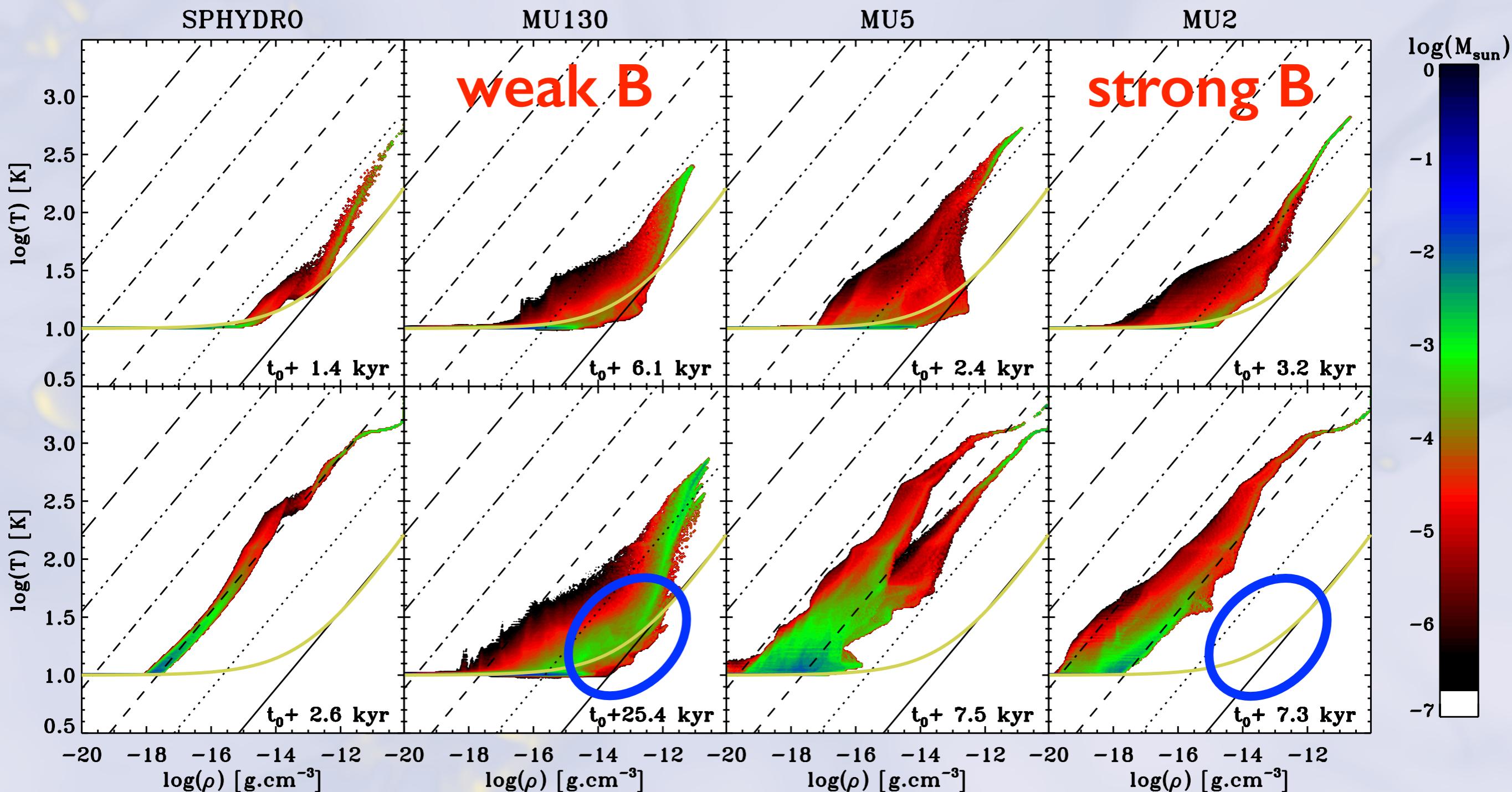
# 100 $M_{\odot}$ turbulent dense core collapse



# $100 M_{\odot}$ turbulent dense core collapse

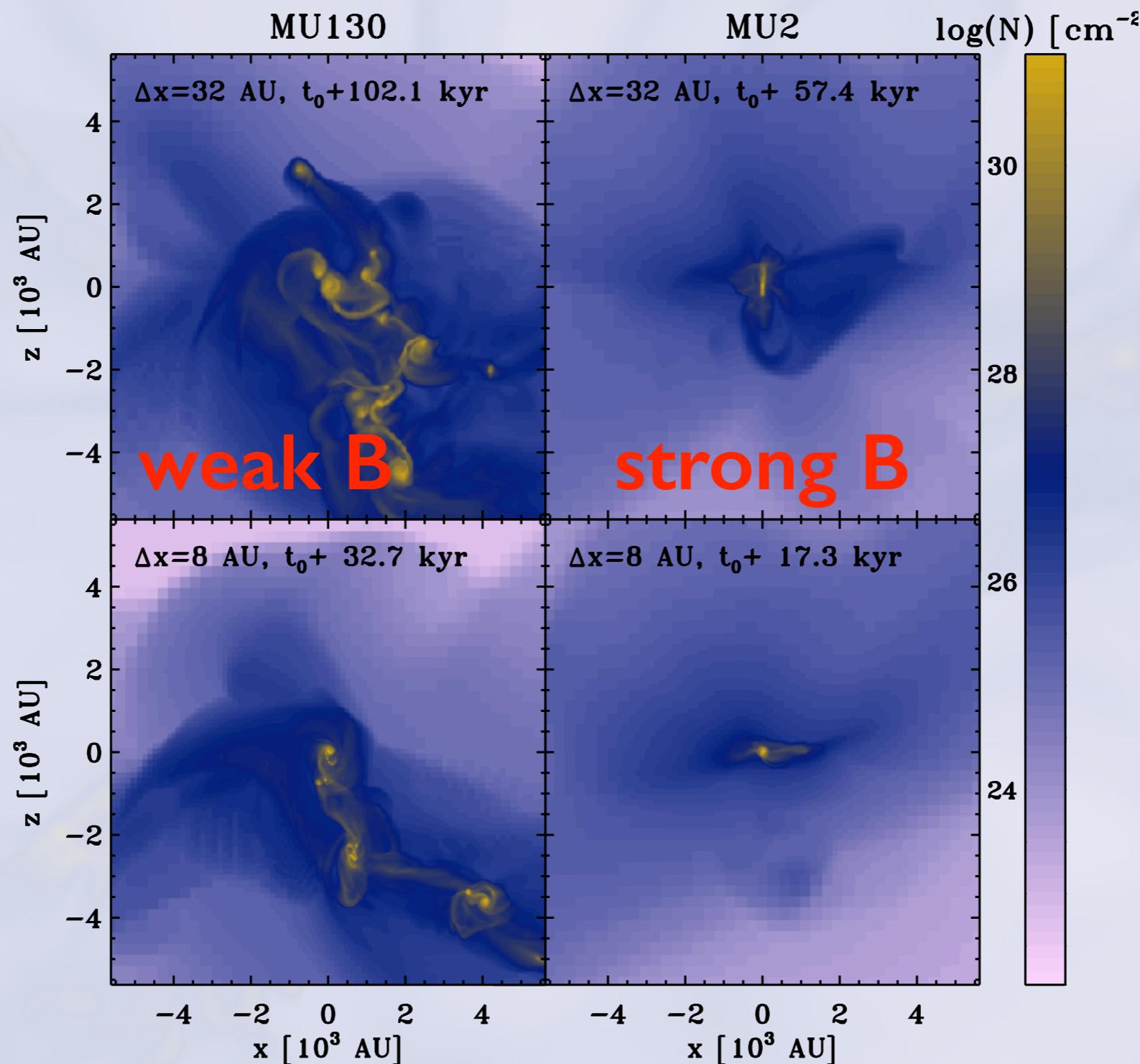


# $100 M_{\odot}$ turbulent dense core collapse



# $100 M_{\odot}$ turbulent dense core collapse

- ✓ Trend confirmed with lower resolution runs:



# What's different?

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- ☞ Key physical process: **combined** effect of magnetic braking and radiative transfer (Commerçon et al. 2010)

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- ✓ Magnetic braking: magnetization  $\nearrow$  accretion rate  $\nearrow$

# What's different?

---

- ☞ **Key physical process:** **combined** effect of magnetic braking and radiative transfer (*Commerçon et al. 2010*)
- ✓ **Magnetic braking:** magnetization  $\nearrow$  accretion rate  $\nearrow$
- ✓ **Accretion shock** on the 1st hydrostatic core: **all** the infall kinetic energy radiated away (*Commerçon et al. 2011b*)

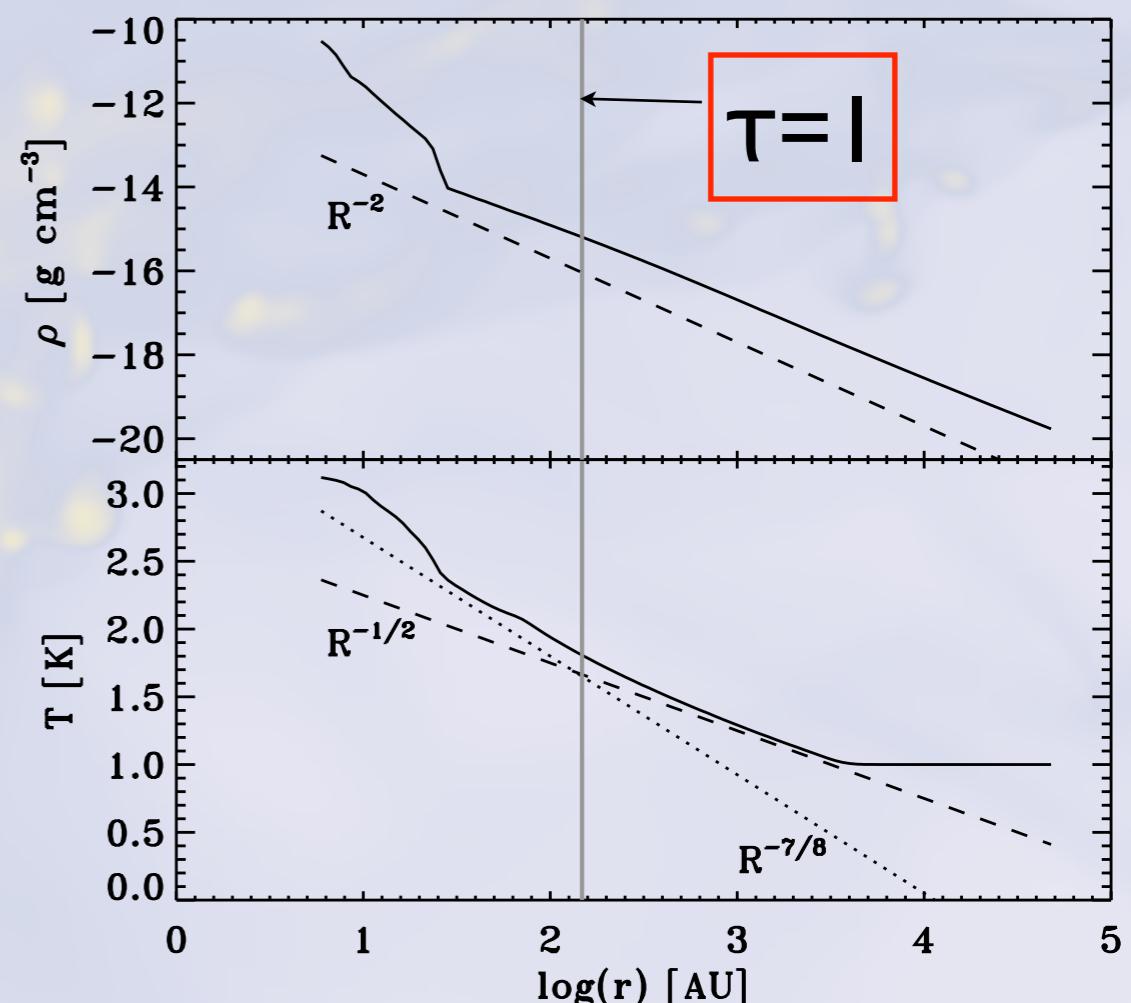
# What's different?

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✓ Magnetic braking: magnetization  $\nearrow$  accretion rate  $\nearrow$

✓ Accretion shock on the 1st hydrostatic core: **all** the infall kinetic energy radiated away (Commerçon et al. 2011b)

SPHYDRO	MU130	MU5	MU2
30	0,2	1,2	10

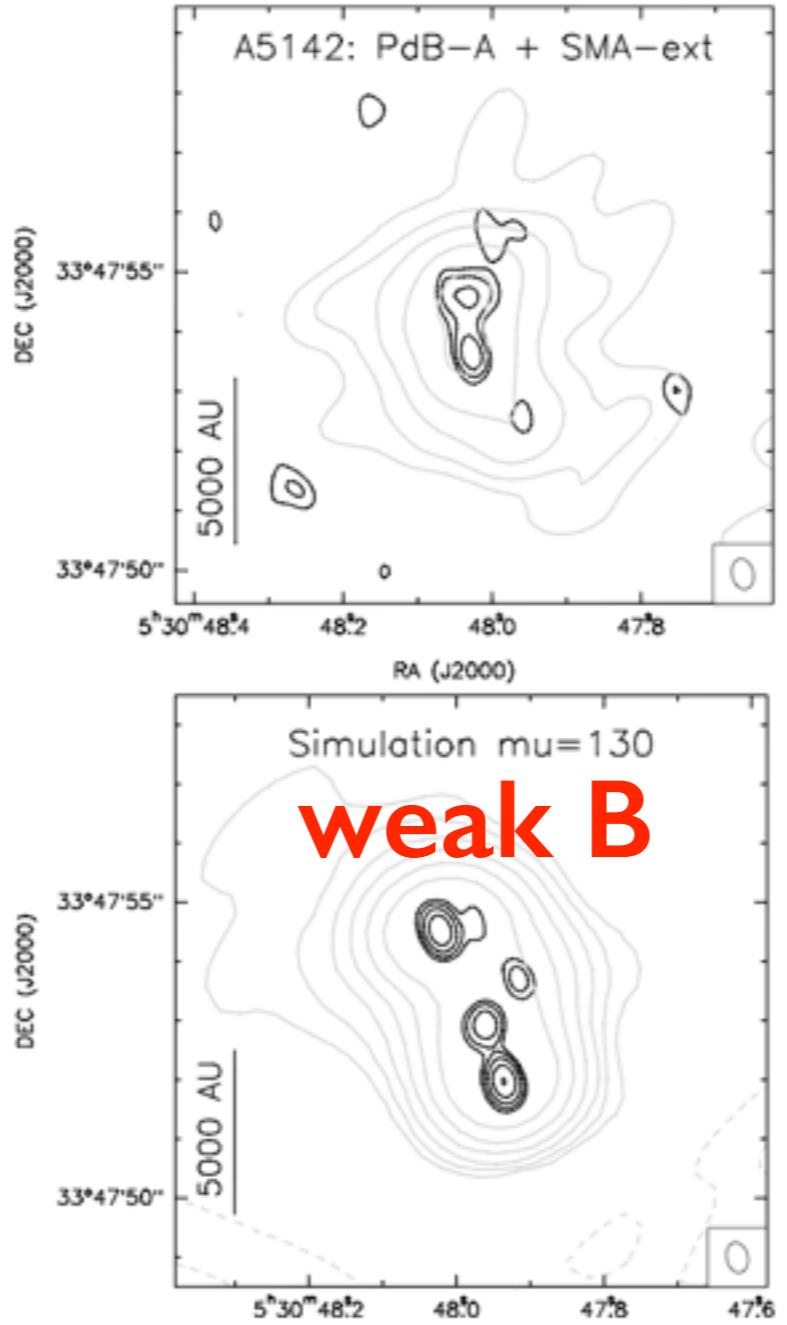
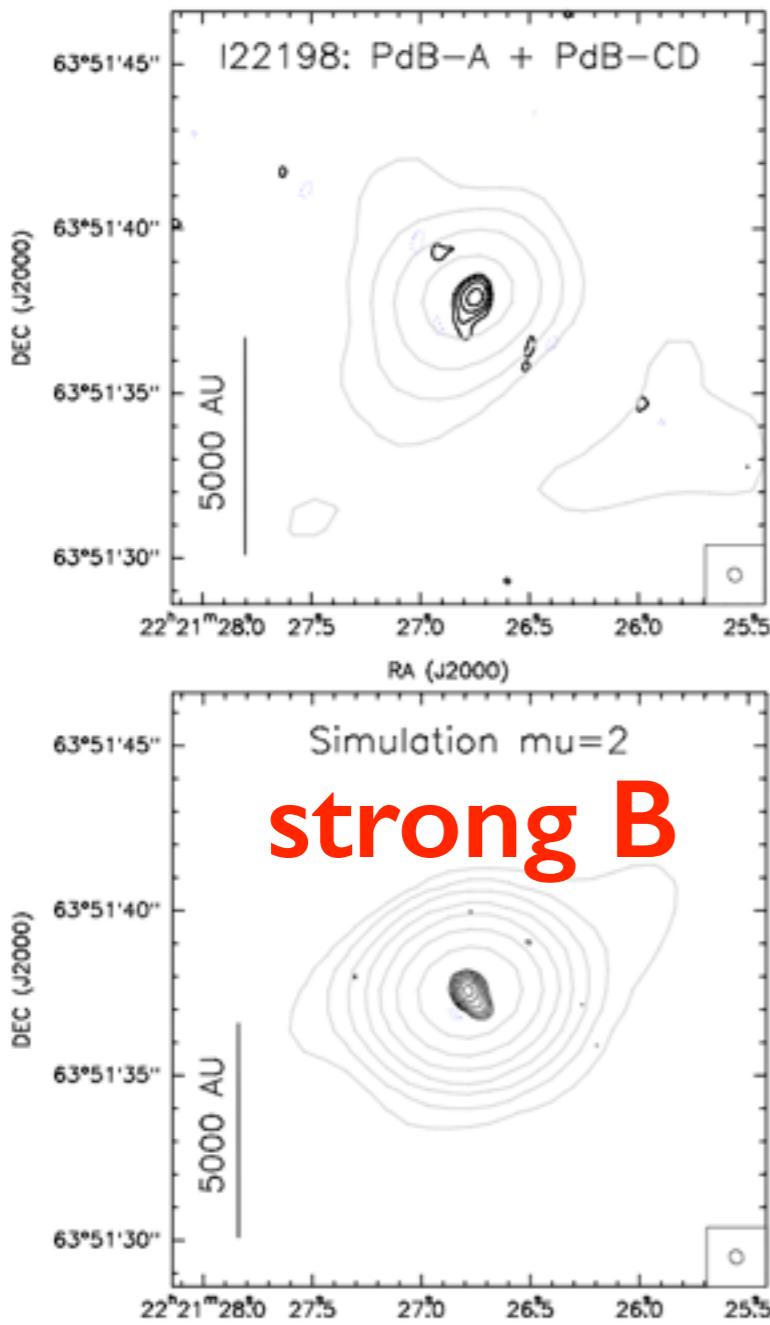


# Towards massive star formation?

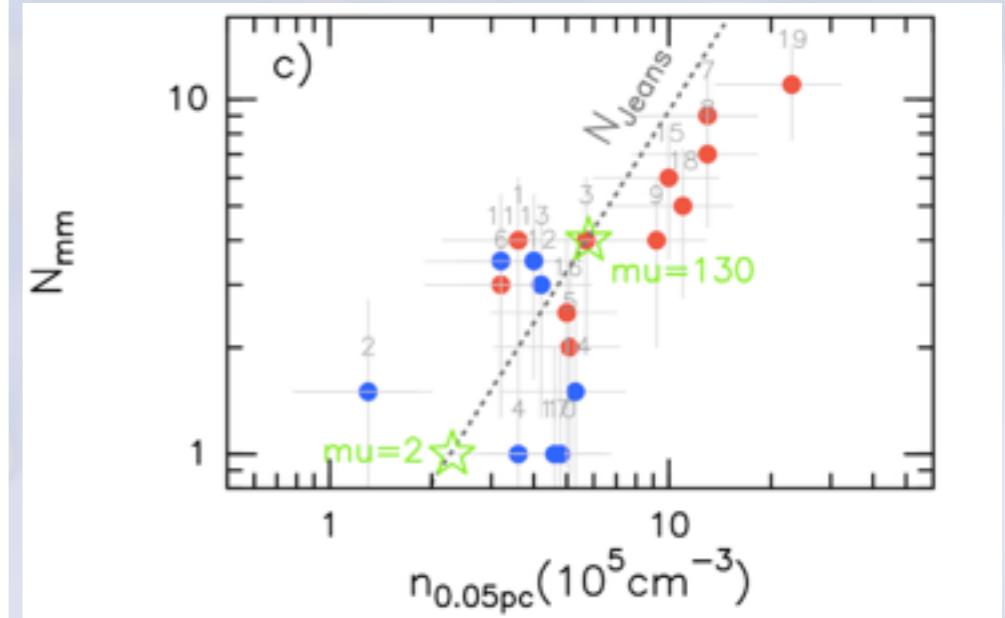
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- ✓ **Low magnetic field:** fragmentation crisis, protostellar feedback would not help
  - similar to previous studies neglecting magnetic fields (competitive accretion), or having a too low resolution (*Peters et al. 2011*)
  - ★ Can magnetic field be neglecting?
- ✓ **Intermediate magnetization:** 2 fragments arranged in a filamentary like structure. Secondary fragment not produced by disk fragmentation (*Krumholz et al.*).
  - OB association formation
- ✓ **High magnetization:** 1 single fragment
  - Isolated massive star formation (e.g. observations by *Girart et al.*, *Bestenlehner et al.* & *Bressert et al.*)
  - Further evolution by disk accretion (e.g. *Kuiper et al. 2010*)
  - ★ Need longer time integration, sink particles

# 100 M<sub>⊙</sub> turbulent dense core collapse



- Simulations reproduce remarkably well observations, but... for both the strong and weak magnetized cases.
- find only one correlation for the number of mm-clumps versus the density at 0.05 pc, i.e., the denser the more fragmented.



Palau et al., 2013 & 2014, ApJ

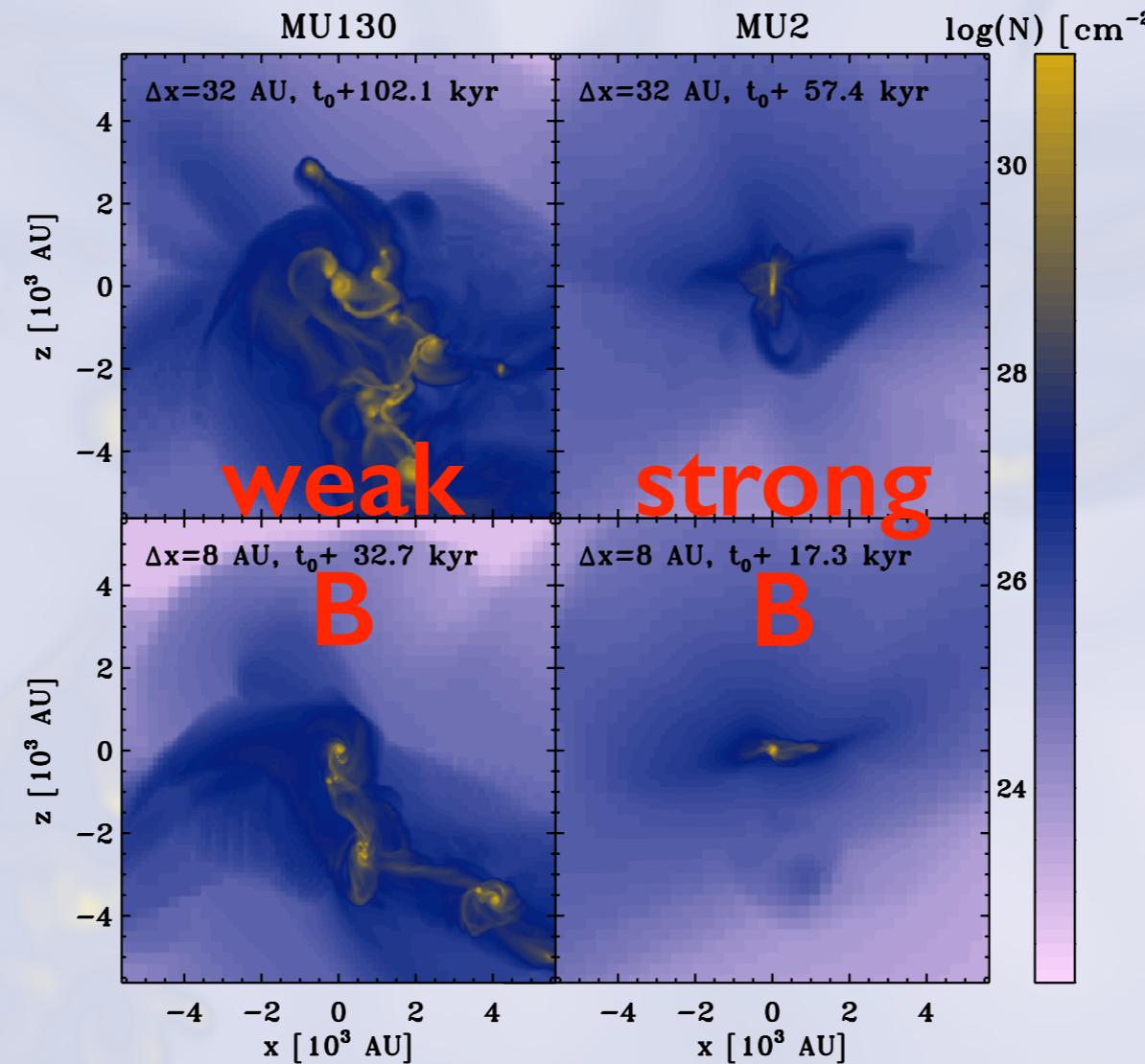
## Take Away II

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- ✓ Fragmentation can be inhibited in massive dense cores
- ✓ Highly magnetized massive dense cores => progenitors of high mass stars

# Formation of massive stars in magnetised cores

- ✓ Focus on isolated massive core, threaded by regular magnetic fields
- ✓ Interplay between magnetic braking and radiative feedback reduces efficiently fragmentation ([Commerçon et al. 2011](#), [Myers et al. 2013](#))
- ✓ *Choice of slowly rotating cores to focus on the star-disk-outflow system formation, without strong fragmentation*



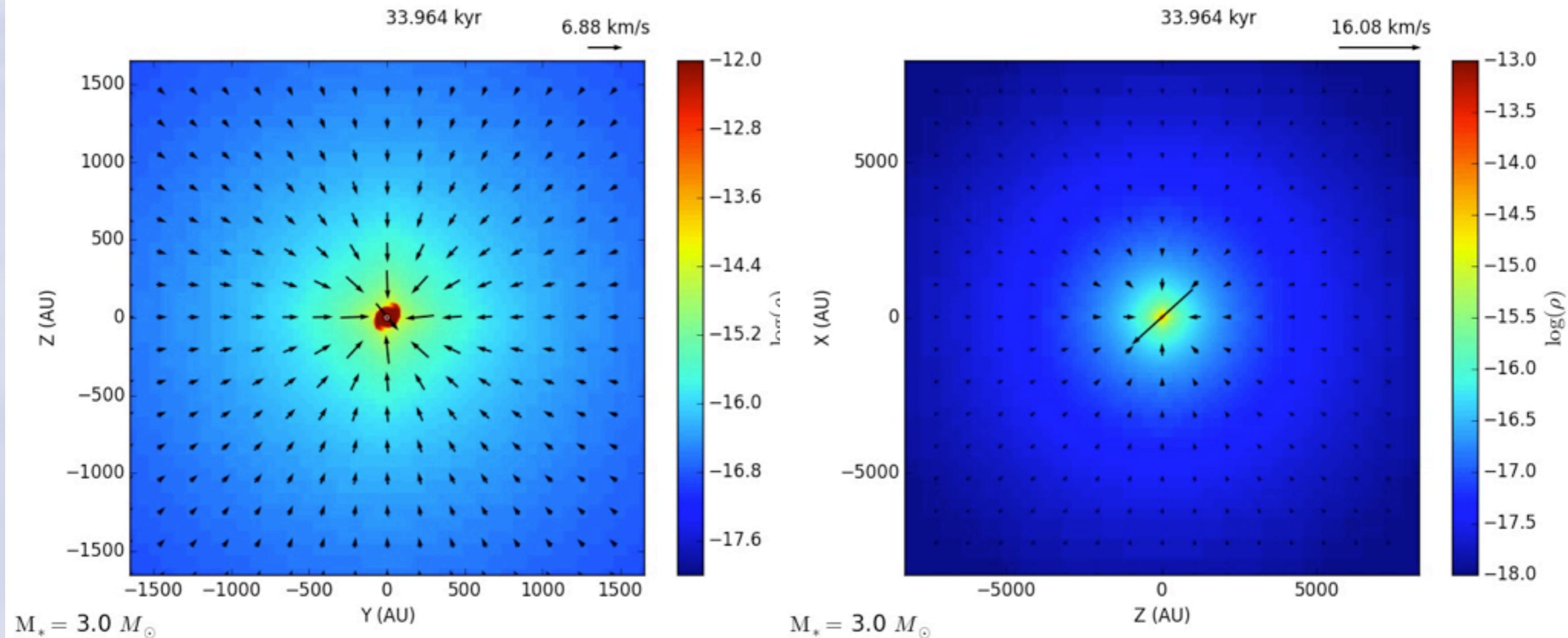
[Commerçon et al. 2011](#)

# Initial conditions and stellar evolution

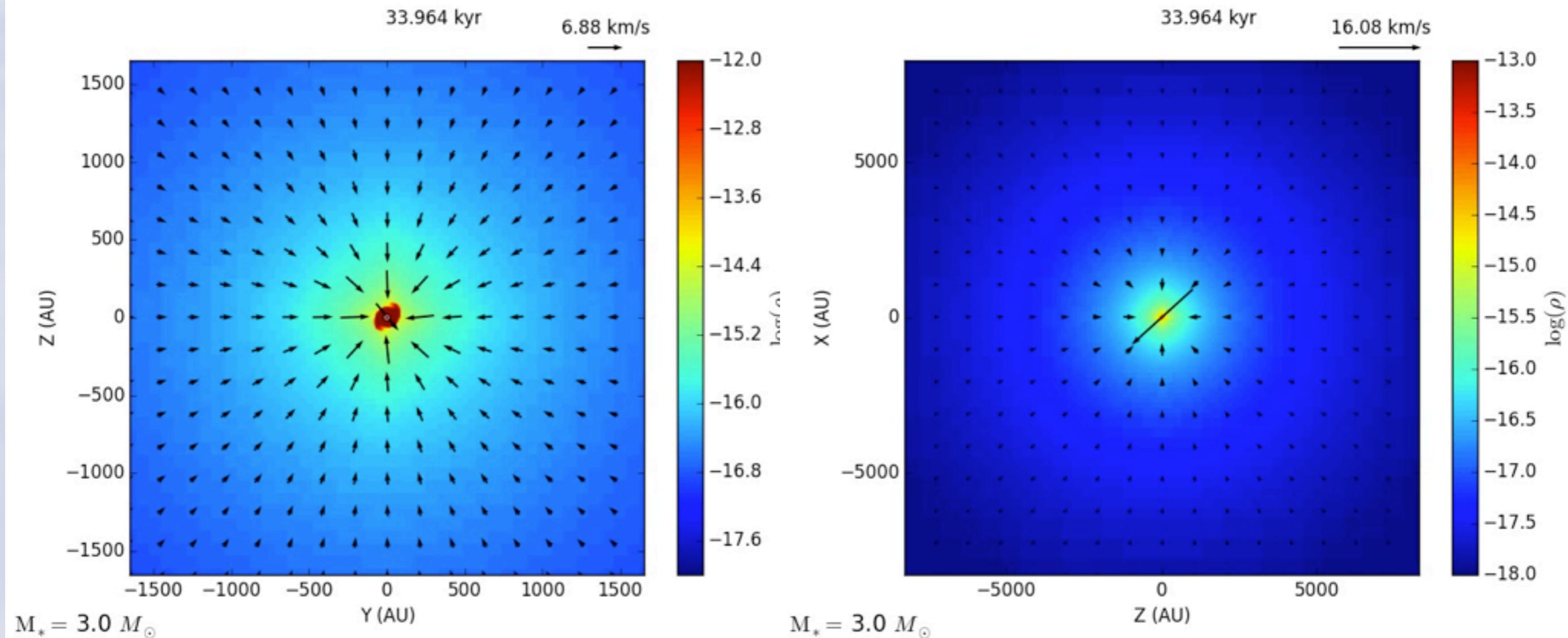
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- ✓  $100 M_{\odot}$ ;  $\rho \propto R^{-2}$  ( $\rho_c = 2 \times 10^6 \text{ cm}^{-3}$ );  $T = 20 \text{ K}$ ;  $R_0 = 0.2 \text{ pc}$
  - ✓ Solid body rotation  $\Omega = 3 \times 10^{-15} \text{ Hz}$  ( $r_d \sim 650 \text{ AU}$ )
  - ✓ Uniform magnetic field ( $\mu_{\text{uni}} = 2, 5, \infty$ ) ( $B = 170, 68, 0 \mu\text{G}$ ), aligned with rotation axis (x-axis)
  - ✓ at least 10 cells/Jeans length
- 
- ✓ Sink particles :  $\rho_{\text{thre}} = 10^{10} \text{ cm}^{-3}$ ,  $r_{\text{sink}} = \sim 20 \text{ AU}$  ( $4\Delta x_{\min}$ )
  - ✓ Protostellar feedback sources associated to the sink:
    - ★ internal luminosity given by Hosokawa et al. tracks (R. Kuiper),  $L_{\text{acc}} = 0$
    - ★ all the accreted mass goes in stellar content (**most** favorable case)
    - ★ NO sub-grid model for outflow
  - ✓ 4 models: Hydro, IMHD  $\mu=2$ , ambipolar diffusion  $\mu=2$  and  $\mu=5$

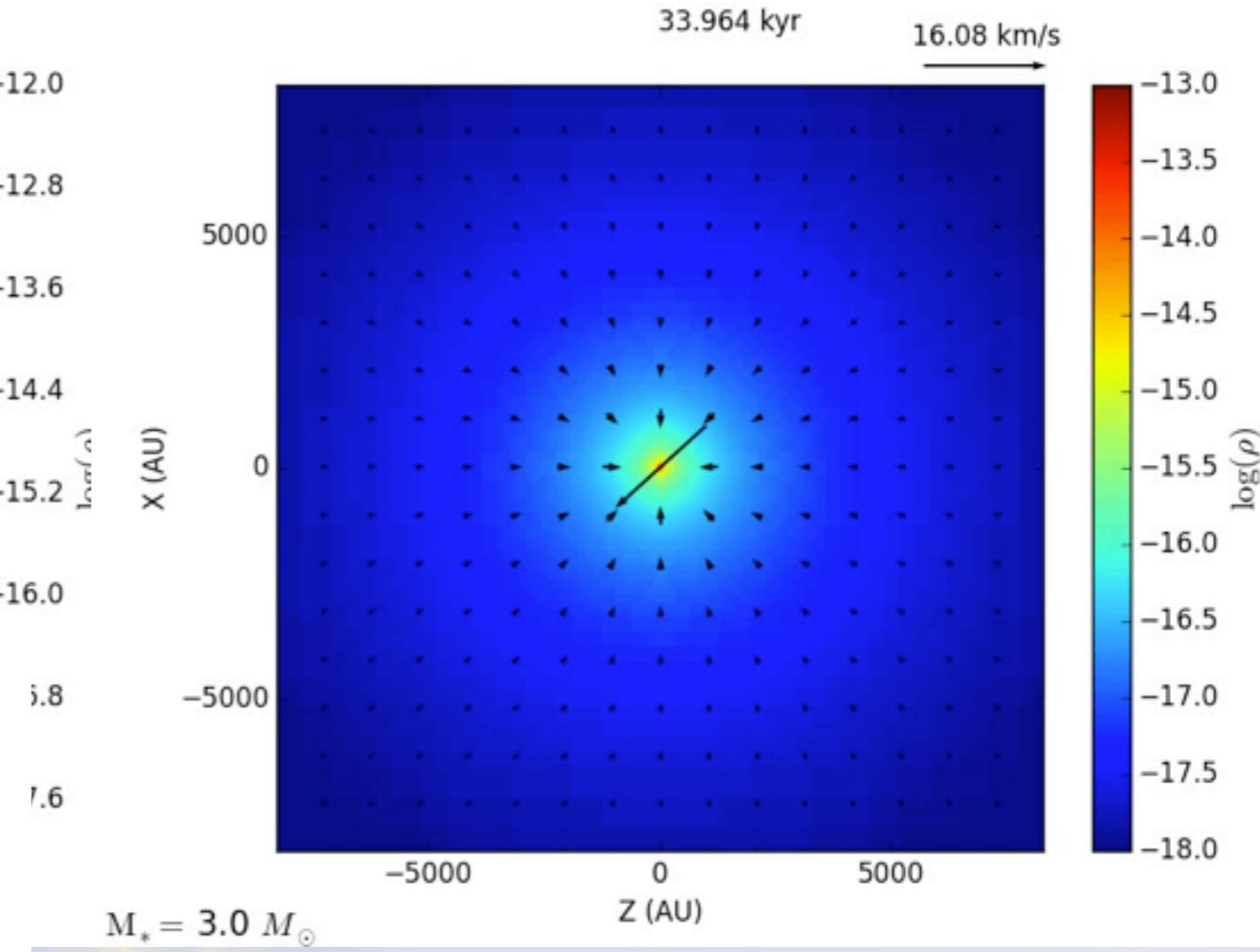
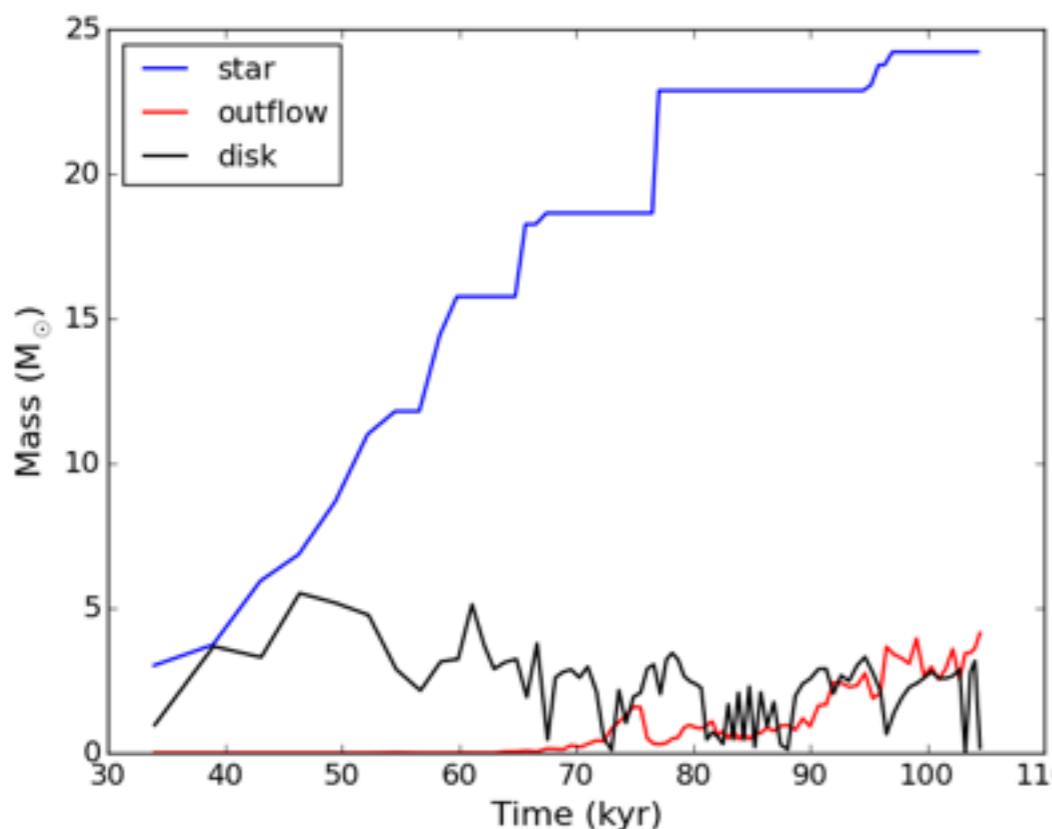
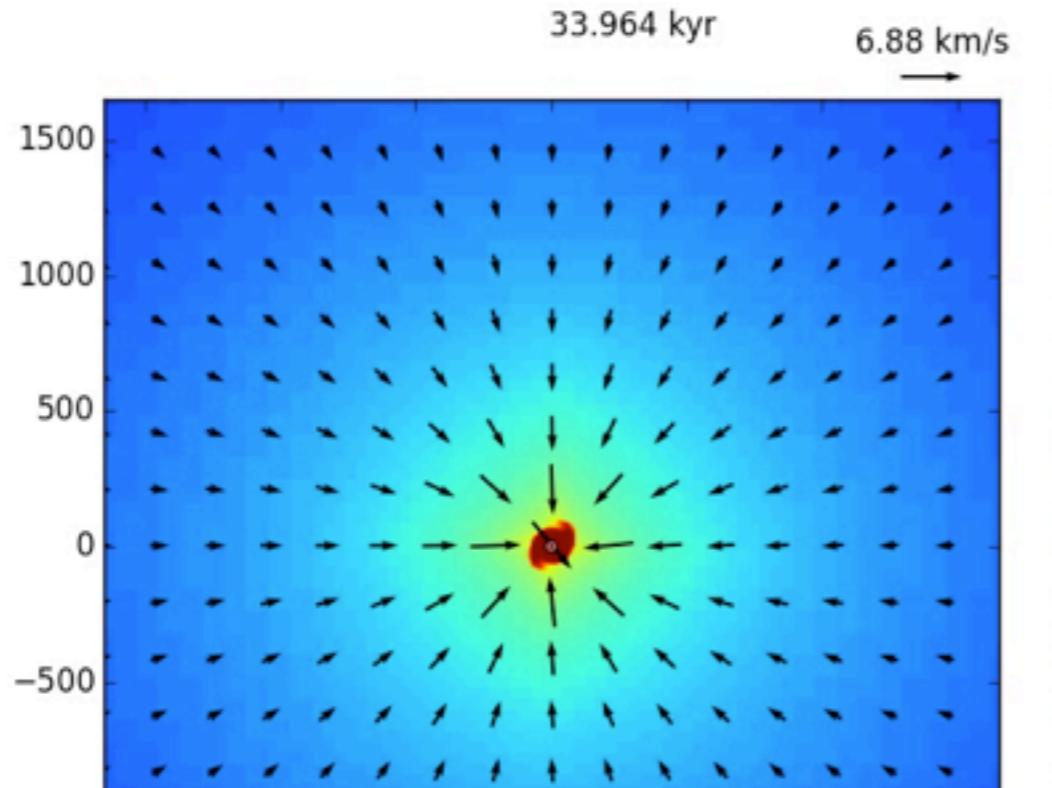
# Hydro collapse



# Hydro collapse

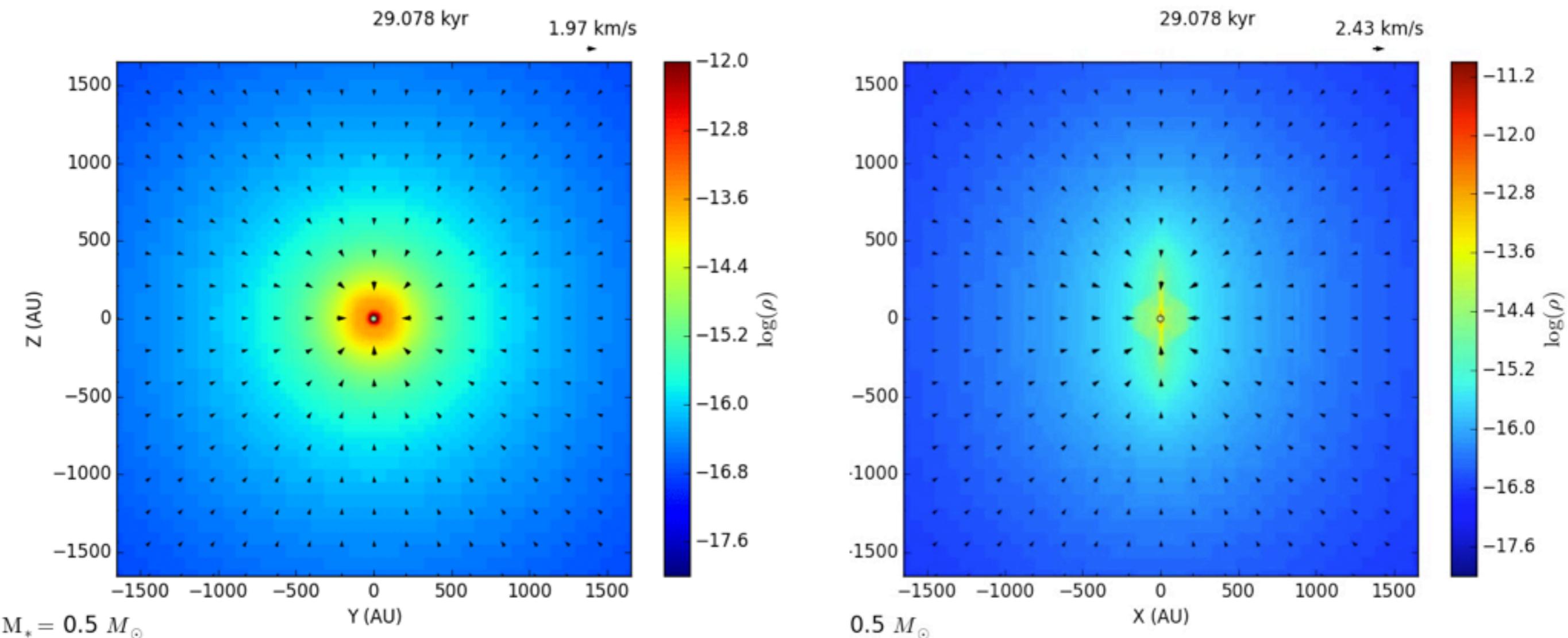


# Hydro collapse

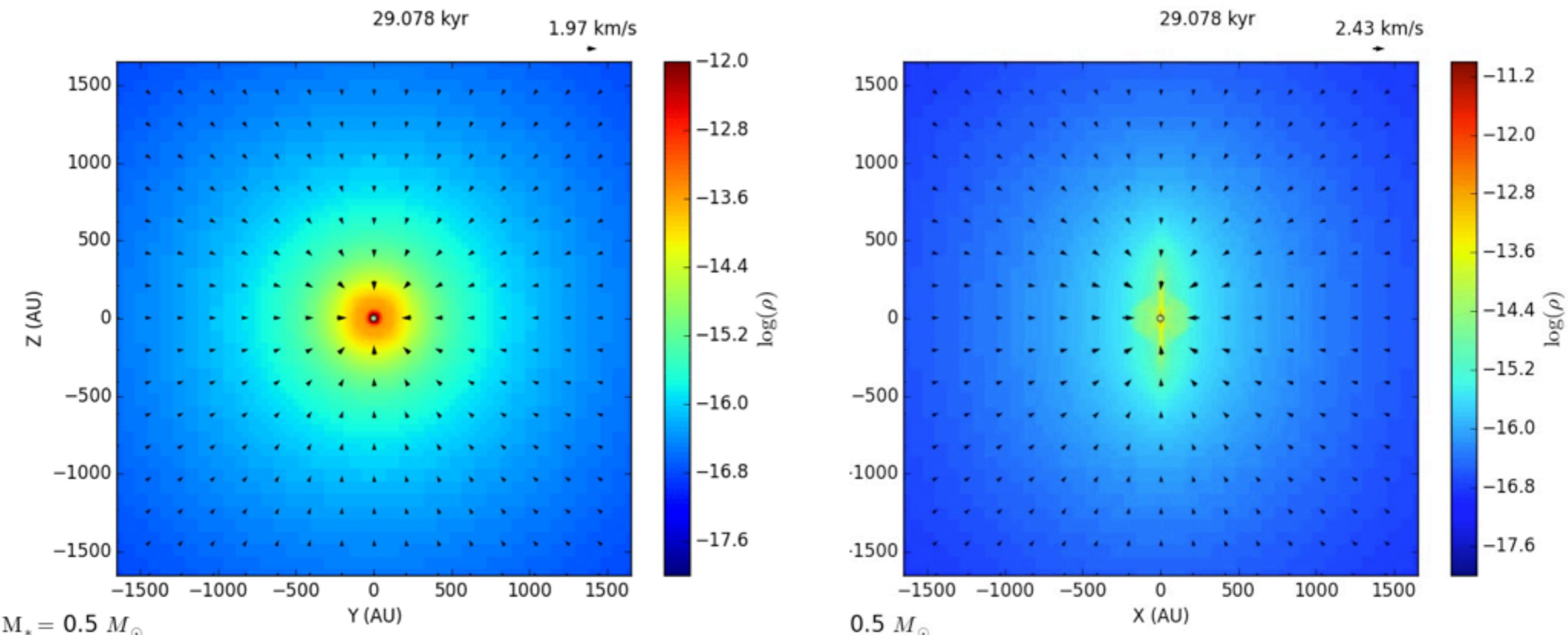


- ✓ Formation of a large disk:  $R \sim 1000$  AU
- ✓ Binary system: 24 and  $13 M_{\odot}$
- ✓ Radiative outflow/bubble (1500 AU)

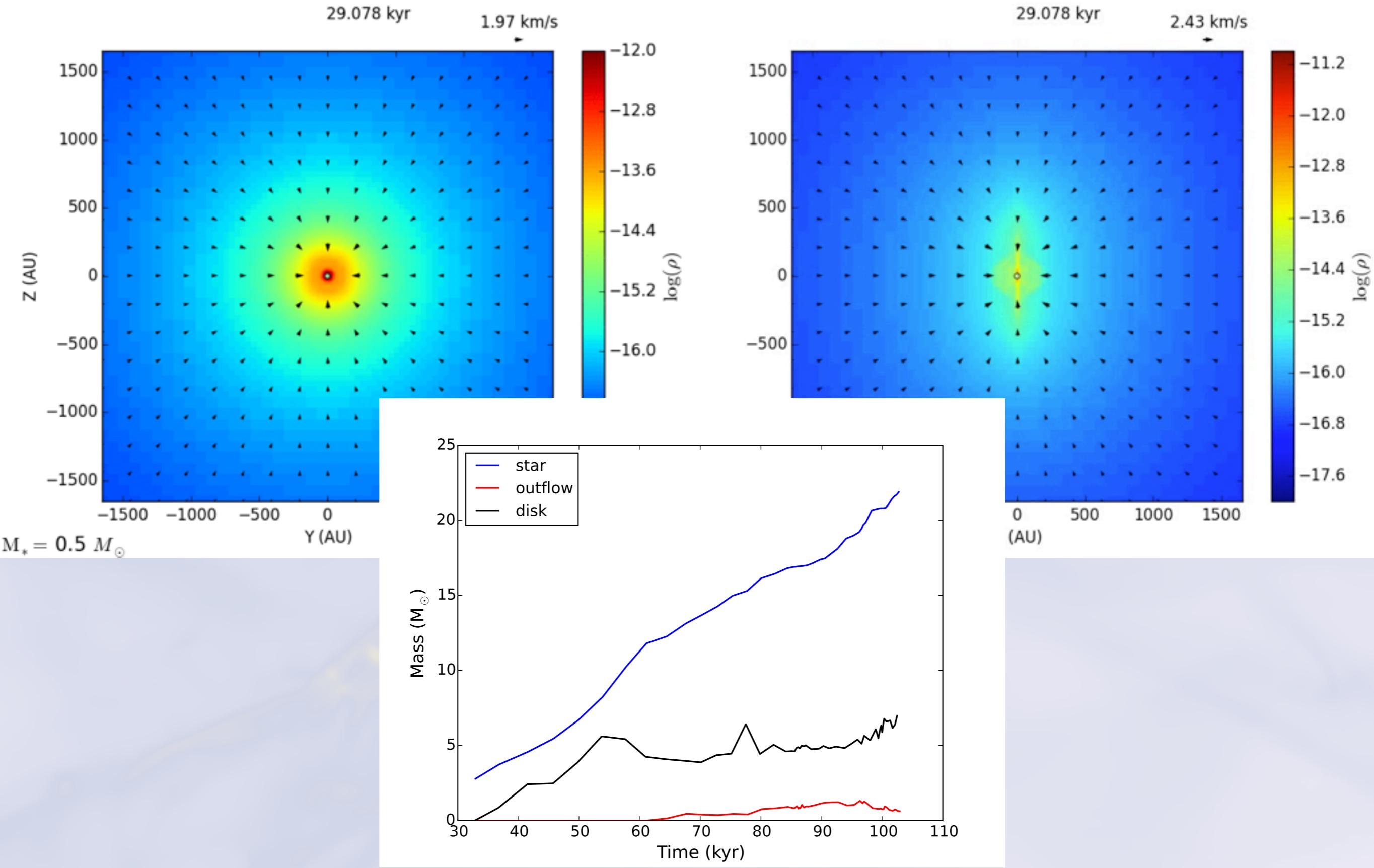
# iMHD collapse, $\mu = 2$



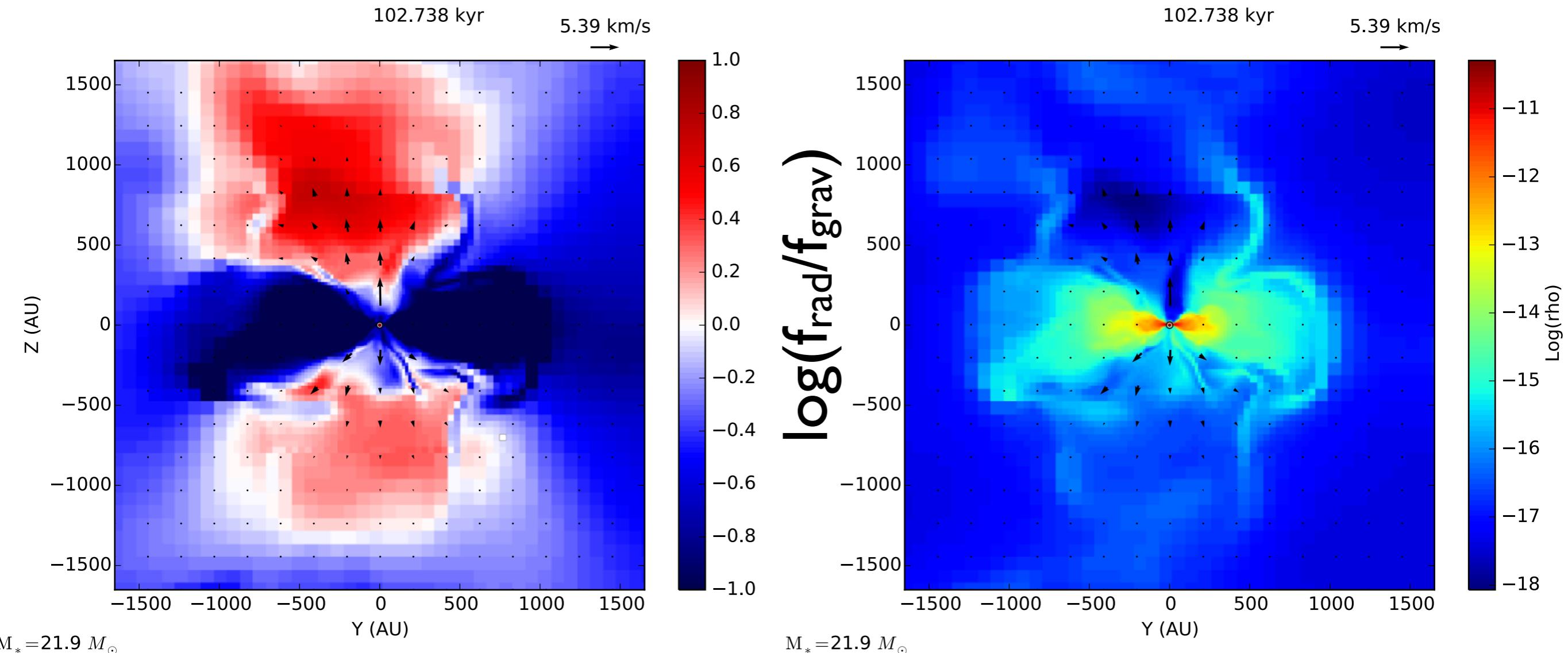
# iMHD collapse, $\mu = 2$



# iMHD collapse, $\mu = 2$

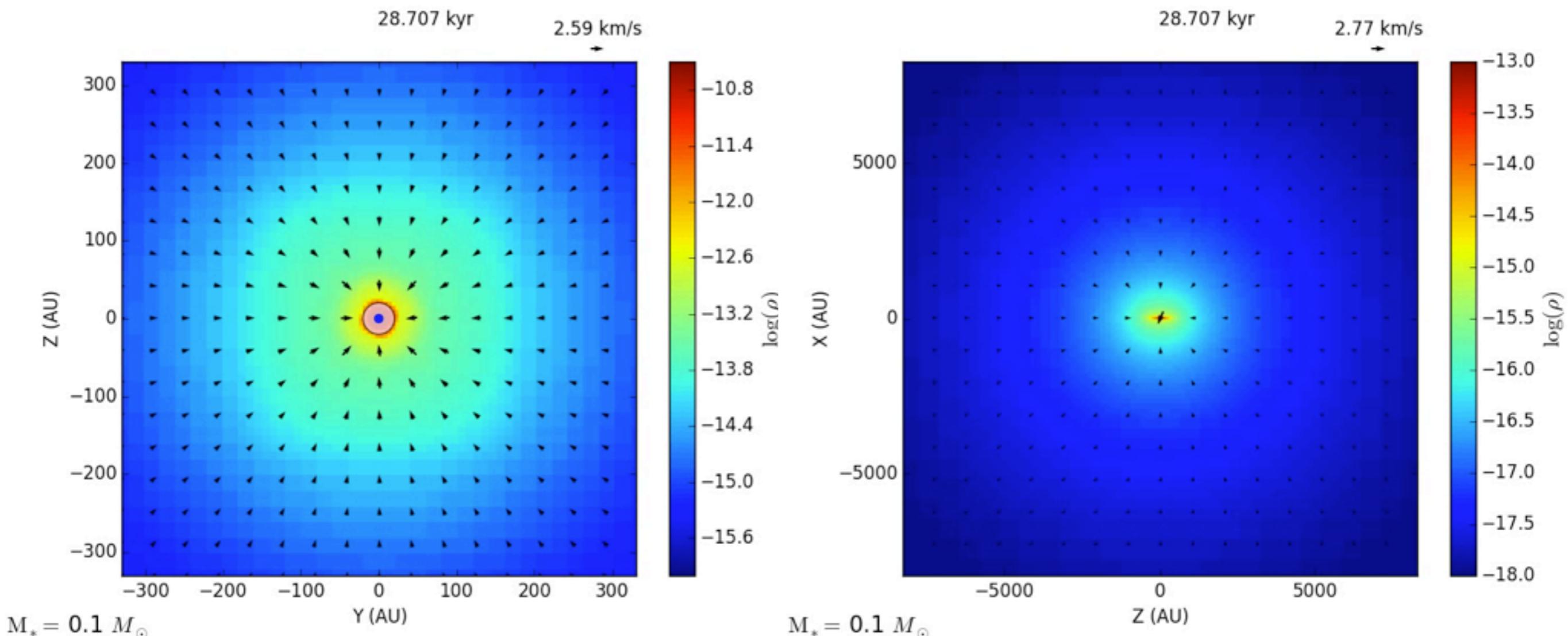


# Hydro & iMHD: origin of the outflow

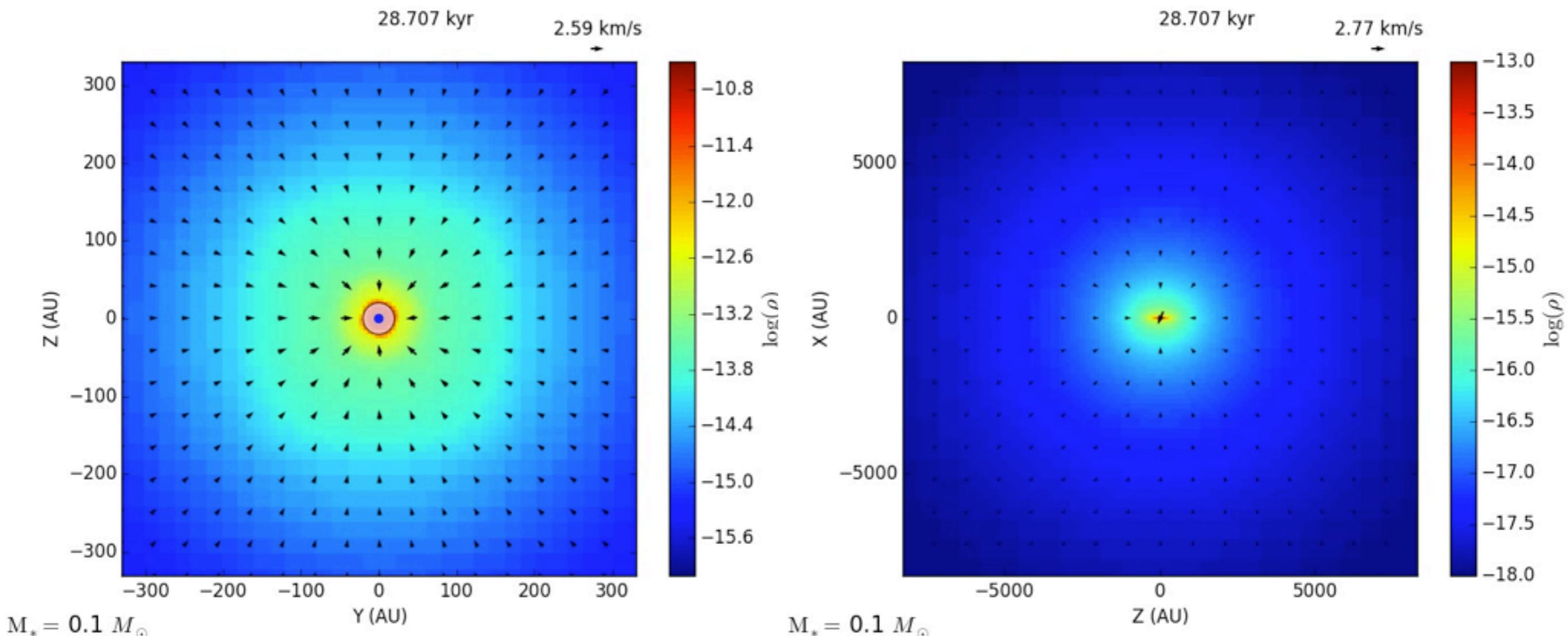


- Outflow has a radiative origin
- Magnetic fields disorganised by magnetic flux expulsion  
(interchange instability, e.g., [Masson et al. 2016](#))

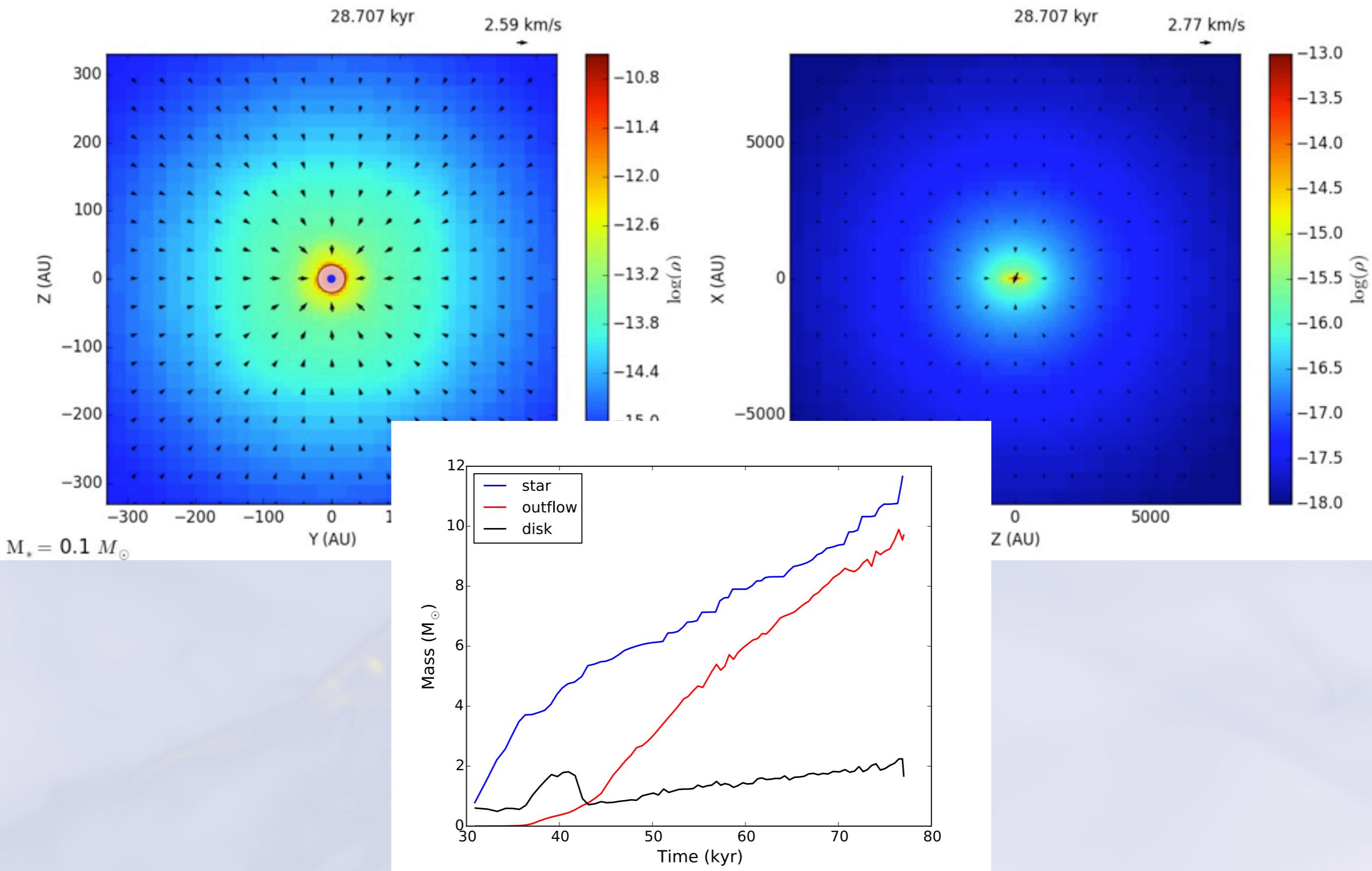
# Ambipolar diffusion, $\mu = 2$



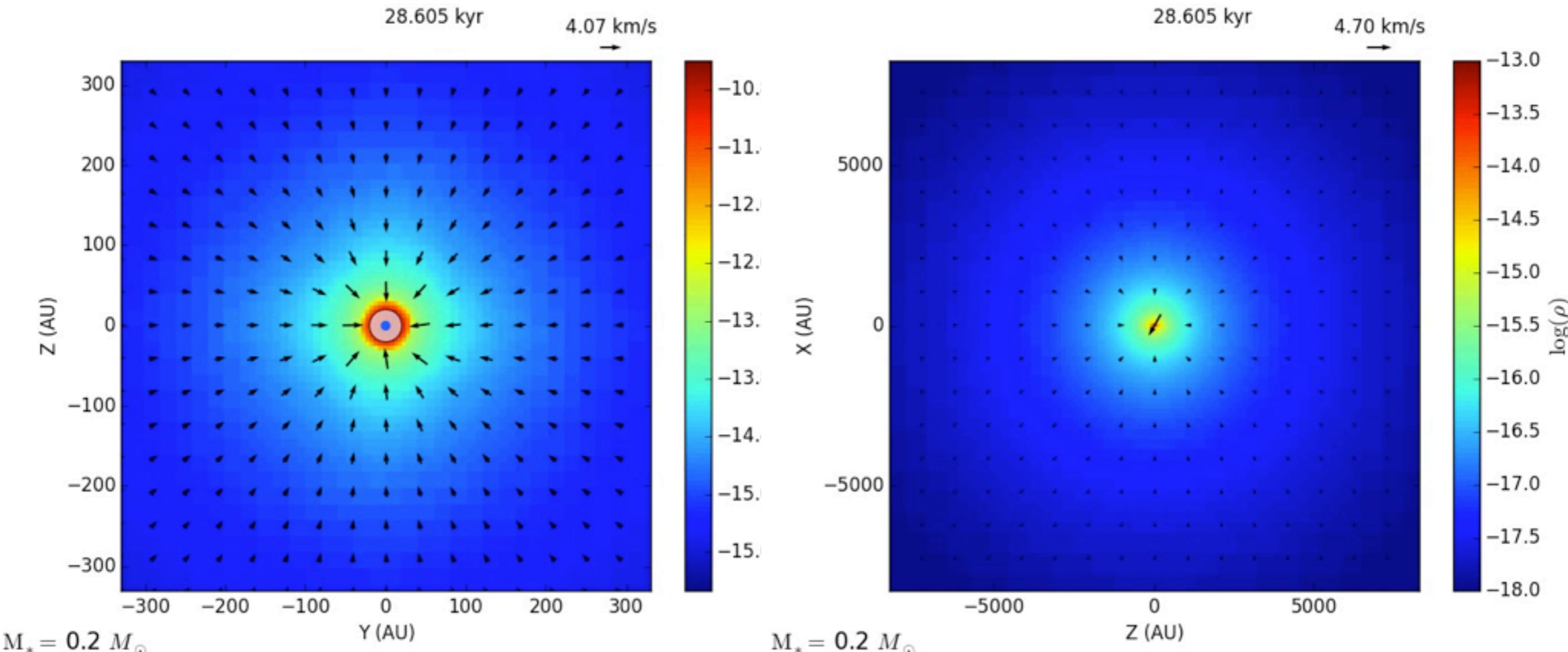
# Ambipolar diffusion, $\mu = 2$



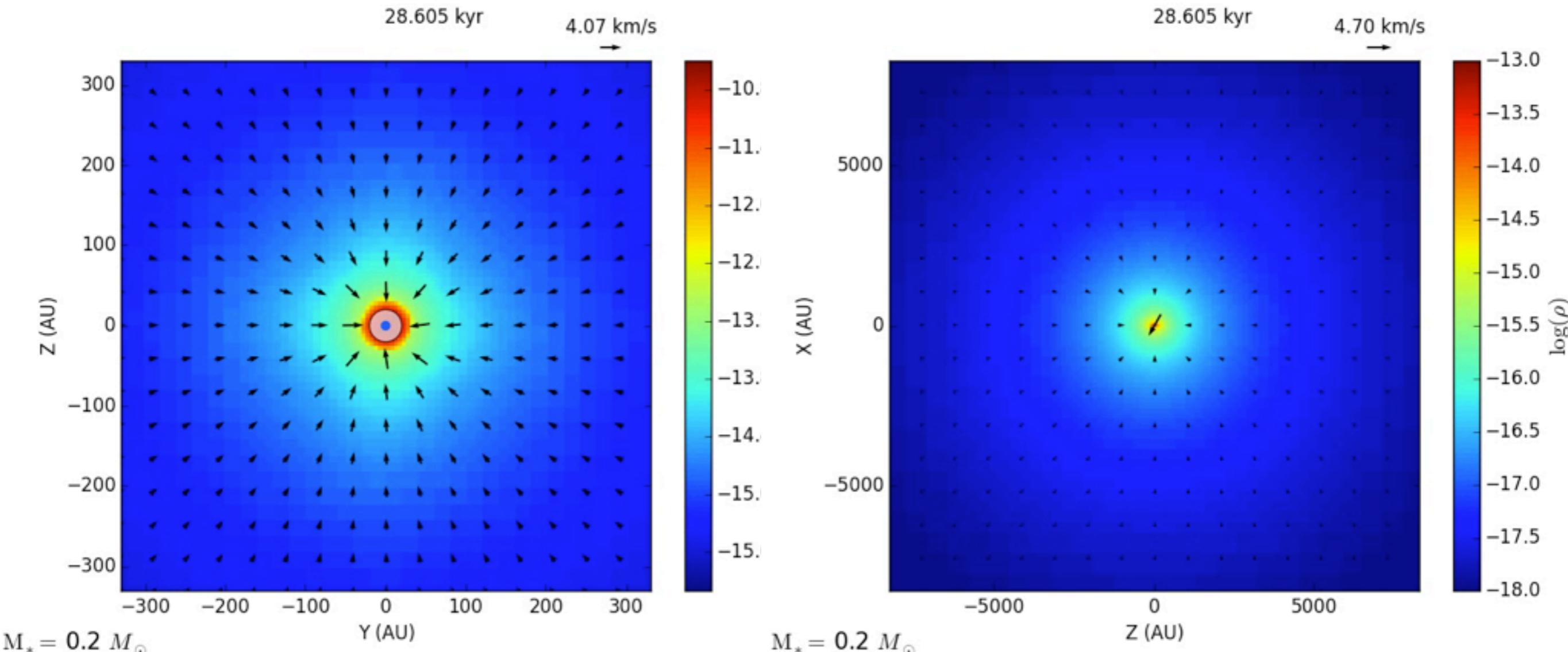
# Ambipolar diffusion, $\mu = 2$



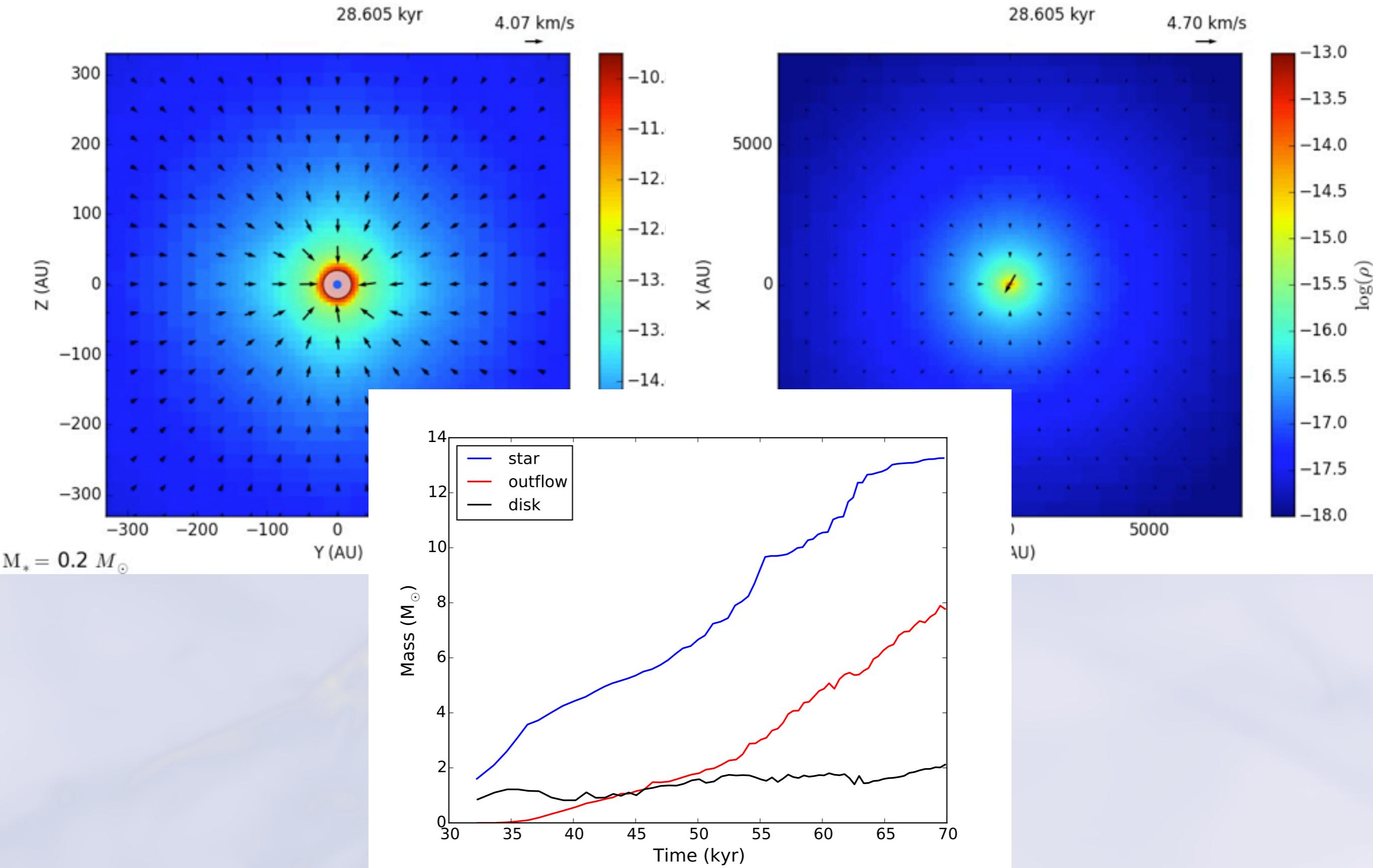
# Ambipolar diffusion, $\mu = 5$



# Ambipolar diffusion, $\mu = 5$



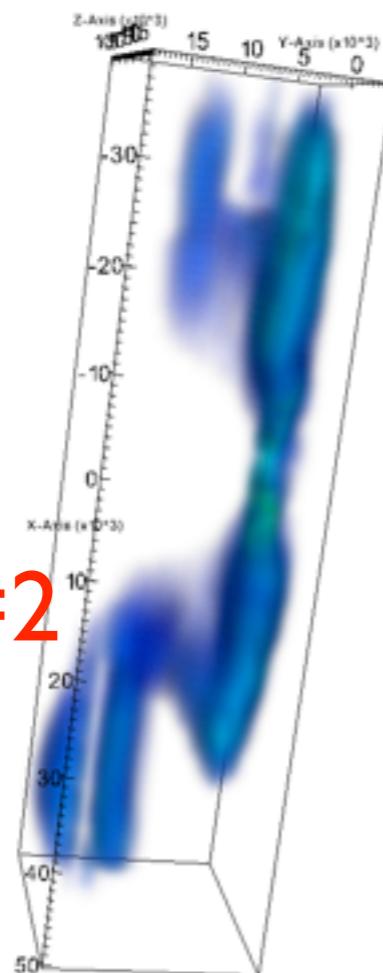
# Ambipolar diffusion, $\mu = 5$



# Outflow morphology

DB: Vr.3D  
Cycle: 0

Volume  
Var: VALUE  
Constant:  
-23.15  
-17.61  
-12.07  
-6.536  
-1.000  
Max: 23.15  
Min: 0.6643

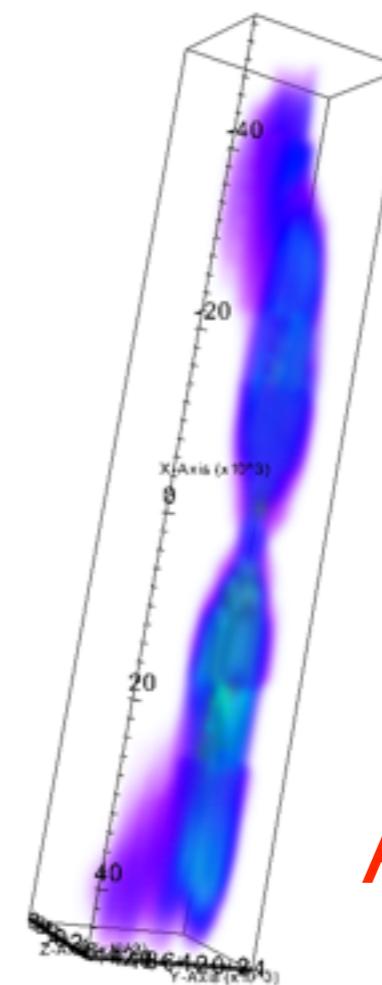


AMBI  $\mu=2$

user: ben  
Fri Mar 25 19:31:43 2016

DB: Vr.3D  
Cycle: 0

Volume  
Var: VALUE  
Constant:  
35.38  
27.03  
18.69  
10.34  
2.000  
Max: 35.38  
Min: 0.7460



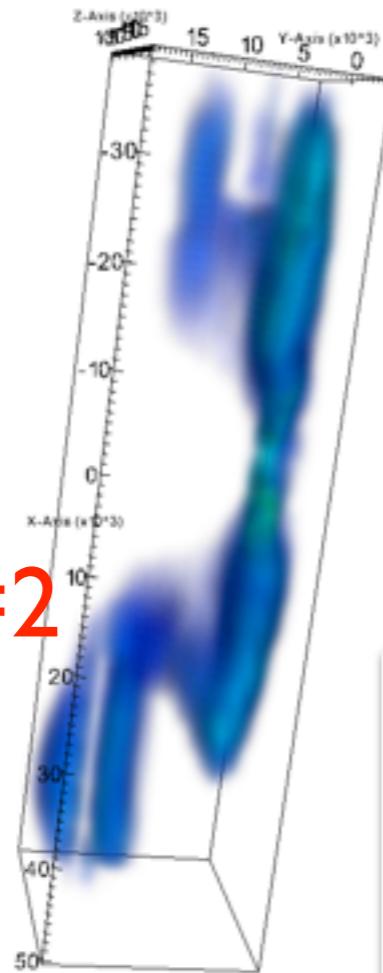
AMBI  $\mu=5$

user: ben  
Fri Mar 25 19:28:56 2016

# Outflow morphology

DB: Vr.3D  
Cycle: 0

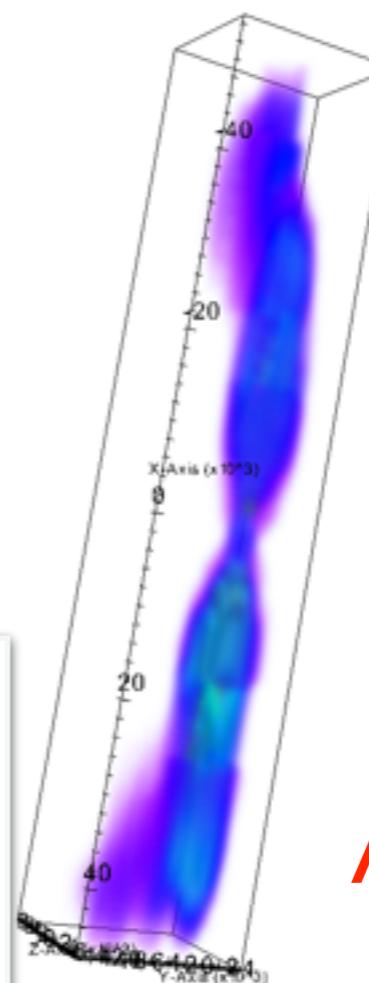
Volume  
Var: VALUE  
Constant:  
-23.15  
-17.61  
-12.07  
-6.536  
-1.000  
Max: 23.15  
Min: 0.6643



AMBI  $\mu=2$

DB: Vr.3D  
Cycle: 0

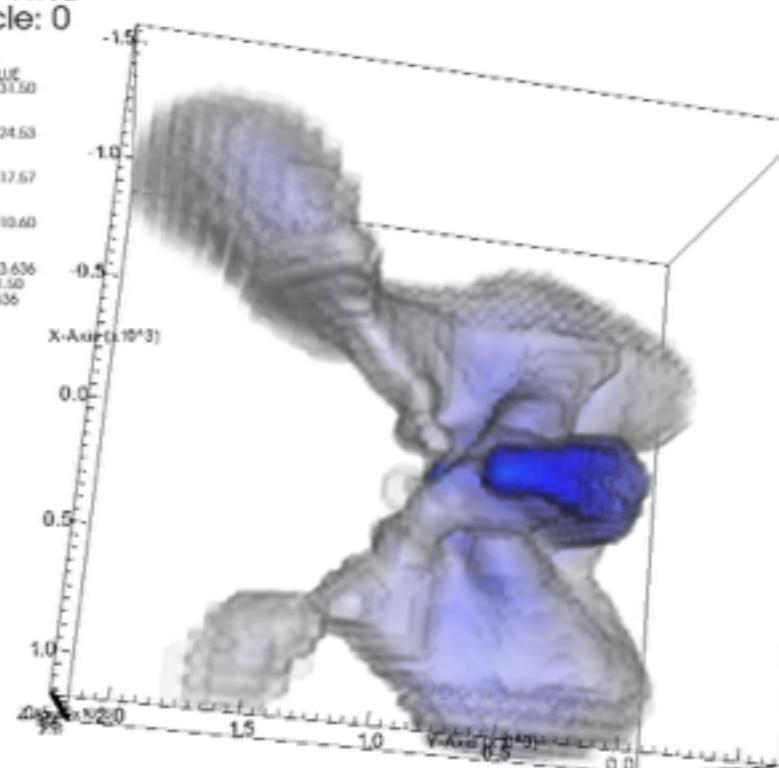
Volume  
Var: VALUE  
Constant:  
35.38  
27.03  
18.69  
10.34  
2.000  
Max: 35.38  
Min: 0.7460



AMBI  $\mu=5$

DB: Vr.3D  
Cycle: 0

Volume  
Var: VALUE  
Constant:  
31.50  
24.53  
17.67  
10.60  
-3.636  
Max: 31.50  
Min: 3.636

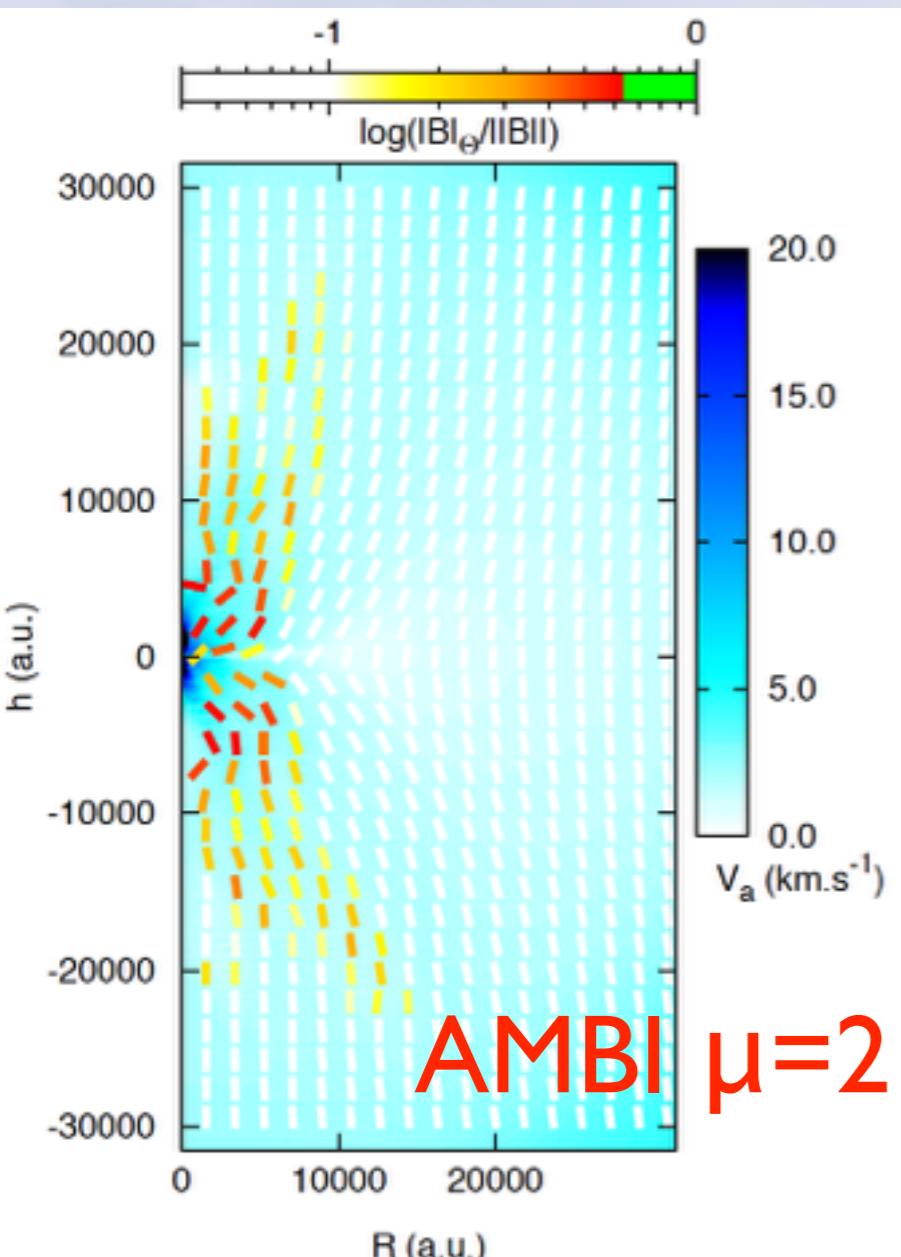


HYDRO

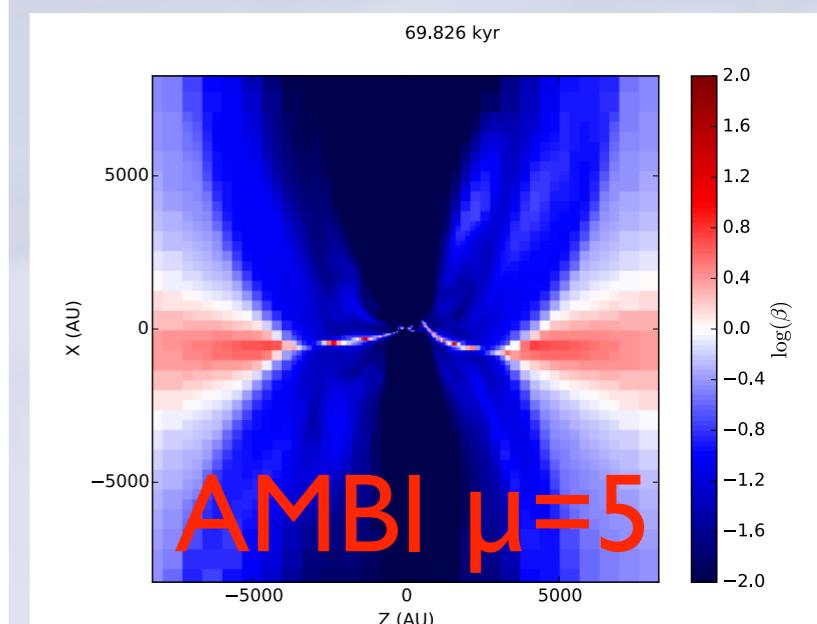
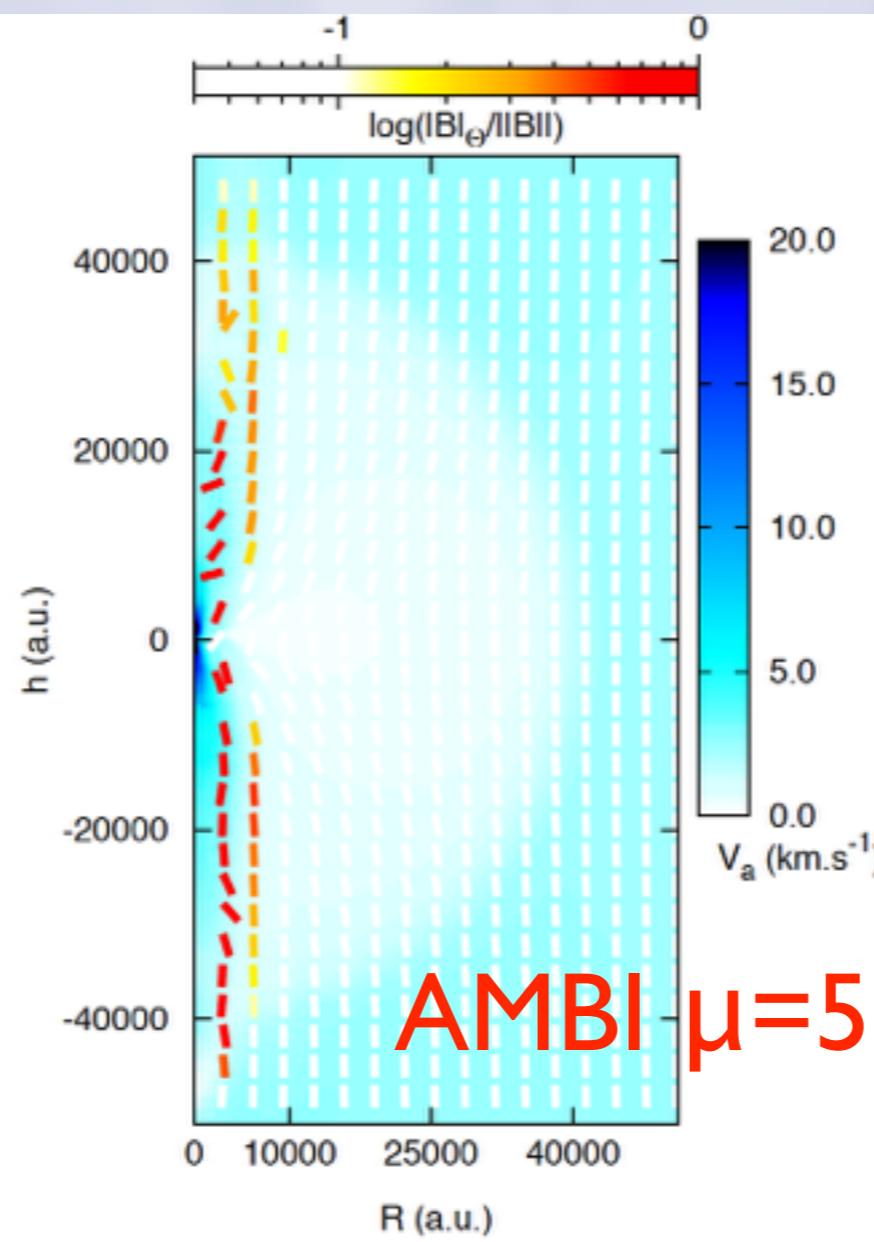
user: benoit  
Wed Mar 30 14:51:50 2016

user: ben  
Fri Mar 25 19:28:56 2016

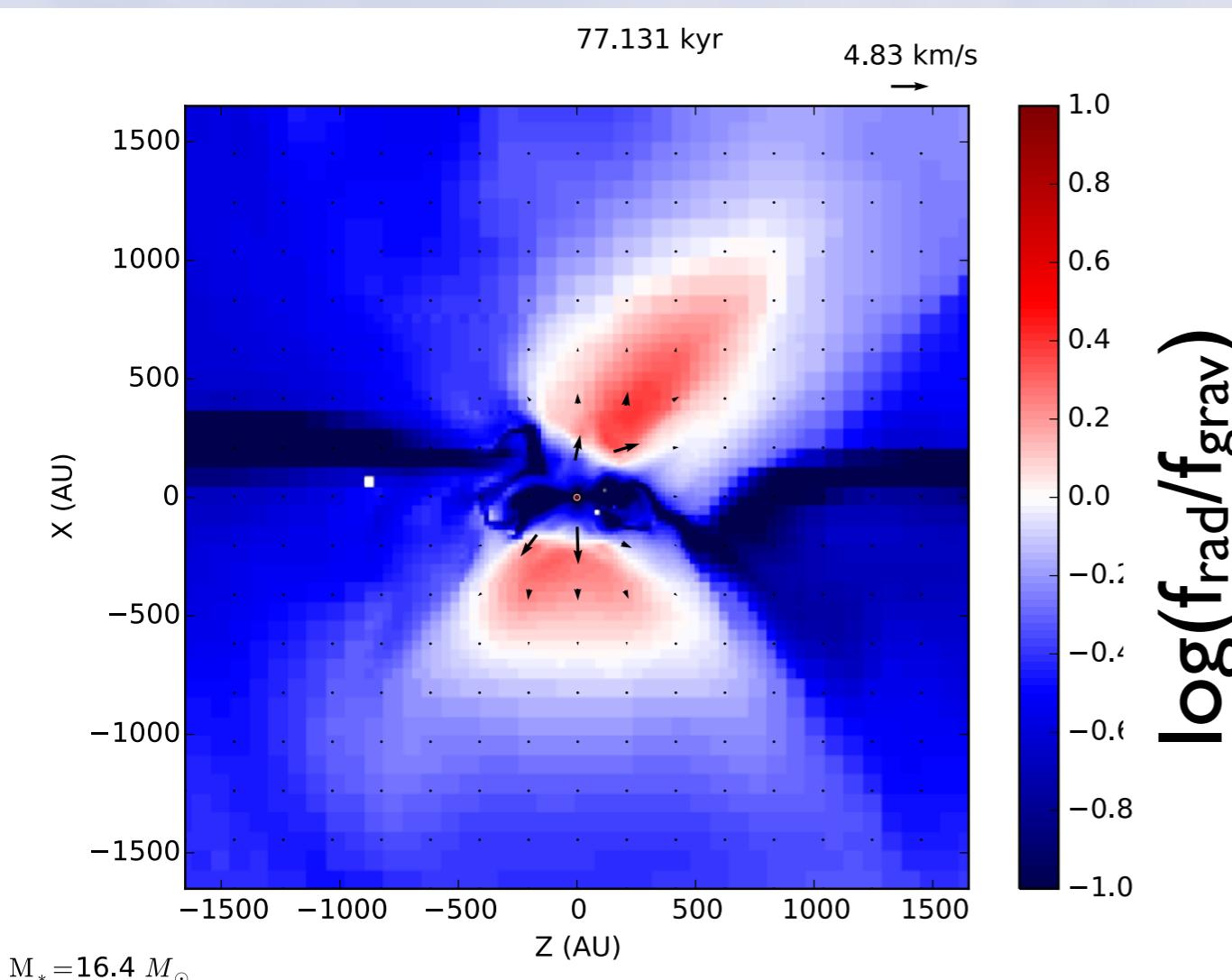
# Outflow collimation



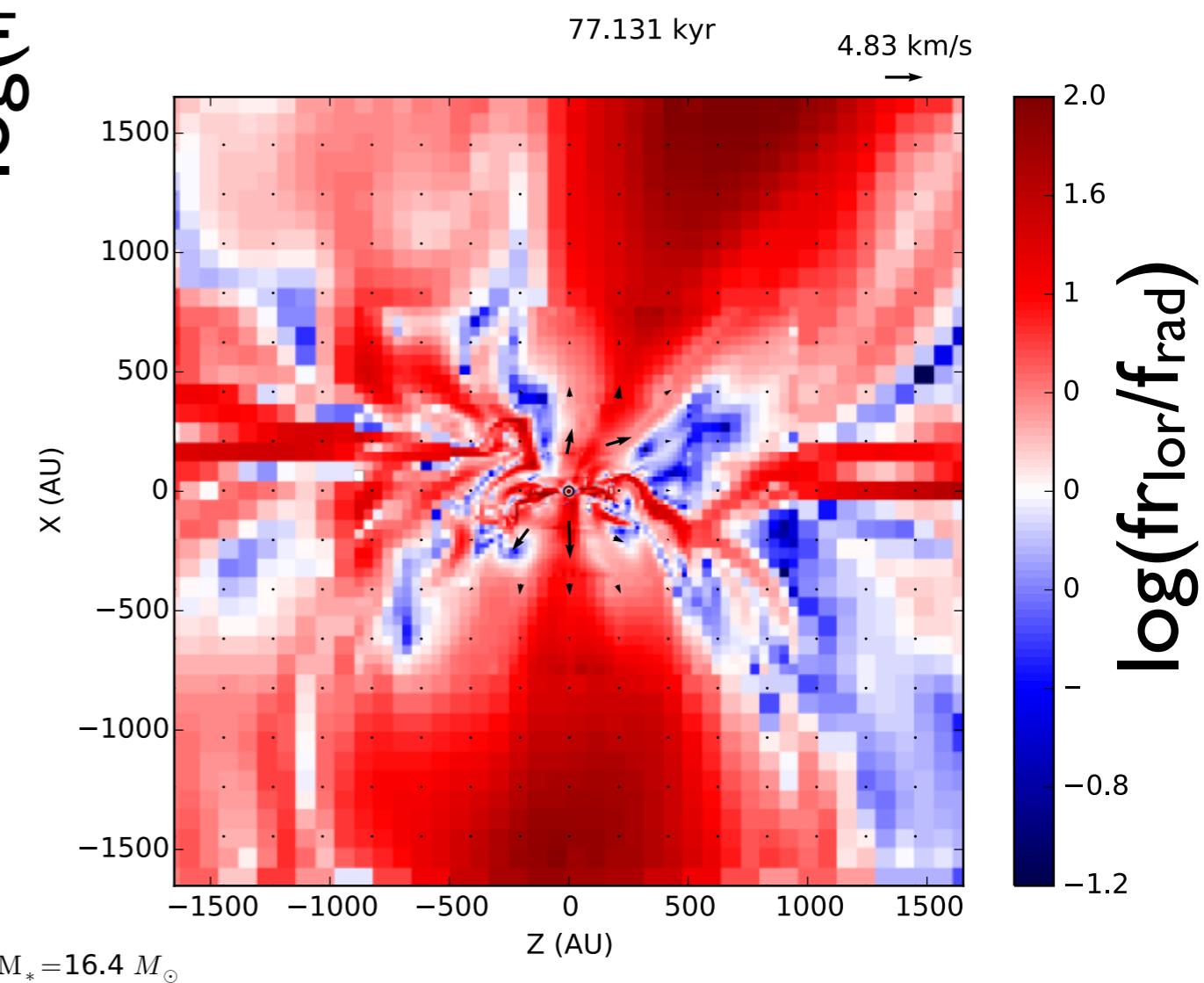
- ✓ outflow collimated by toroidal B-field
- ✓ outflow extends up to 50 000 AU when  $M_\star = 12 M_\odot$ ,  $V_{\text{out,max}} = 40$  km/s
- ✓ outflow is strongly magnetized



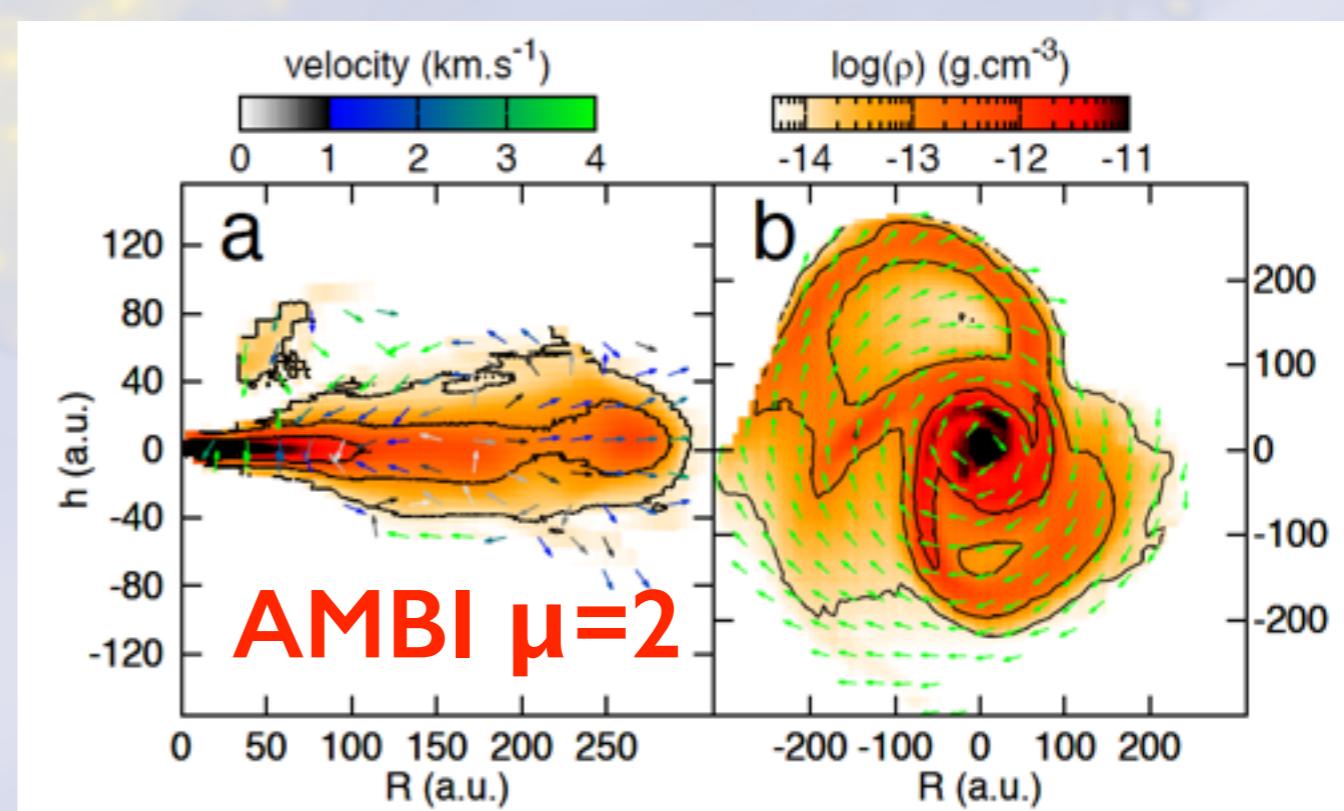
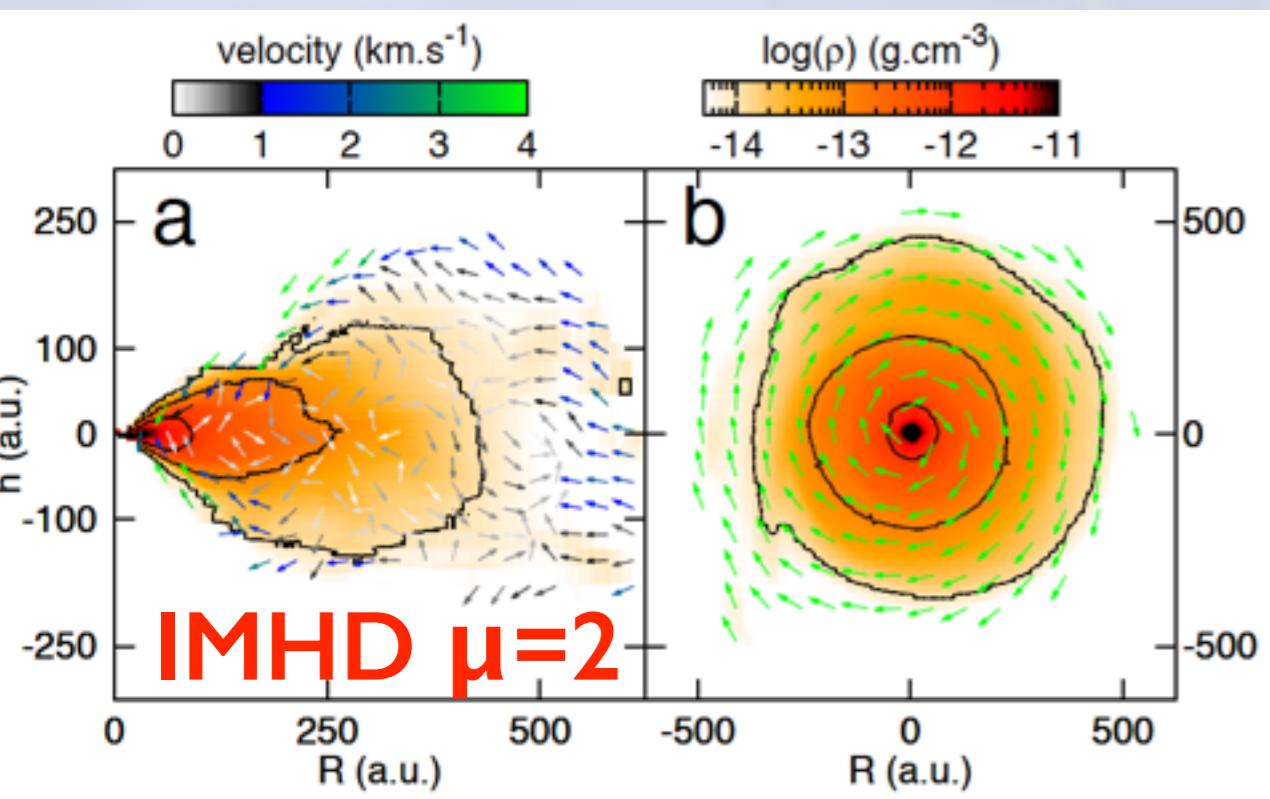
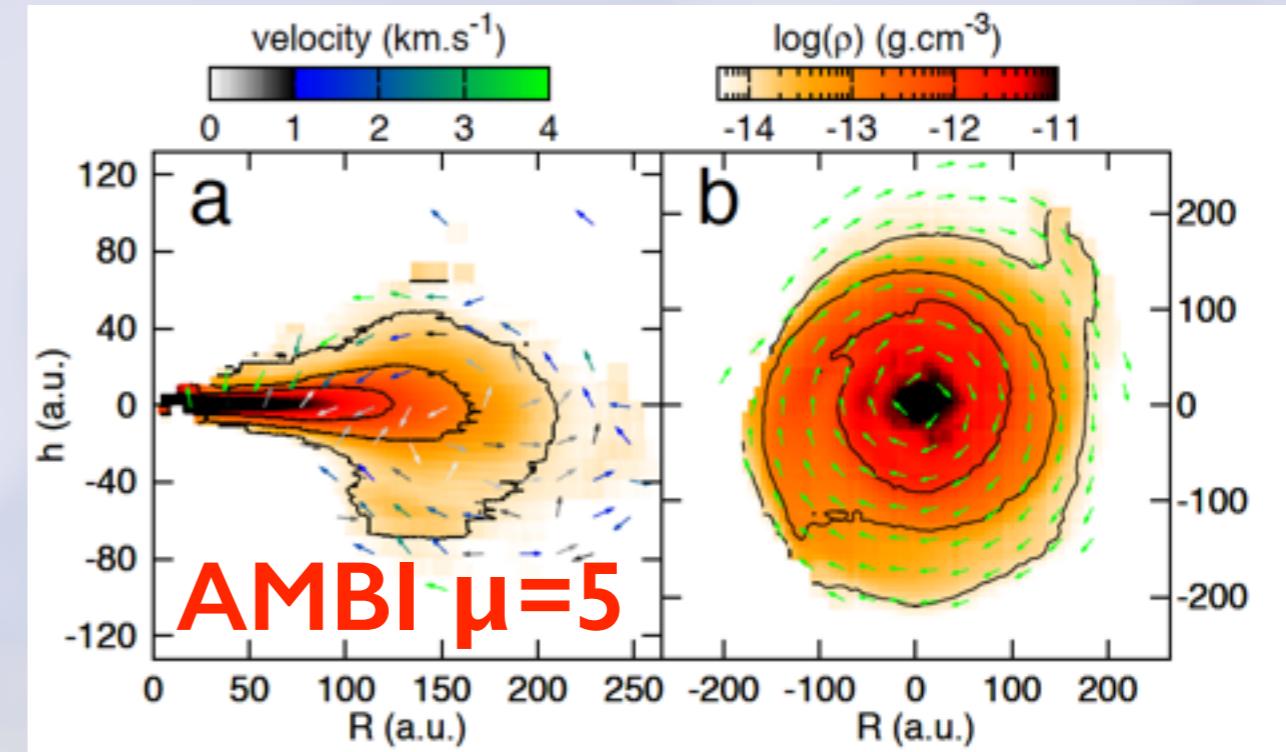
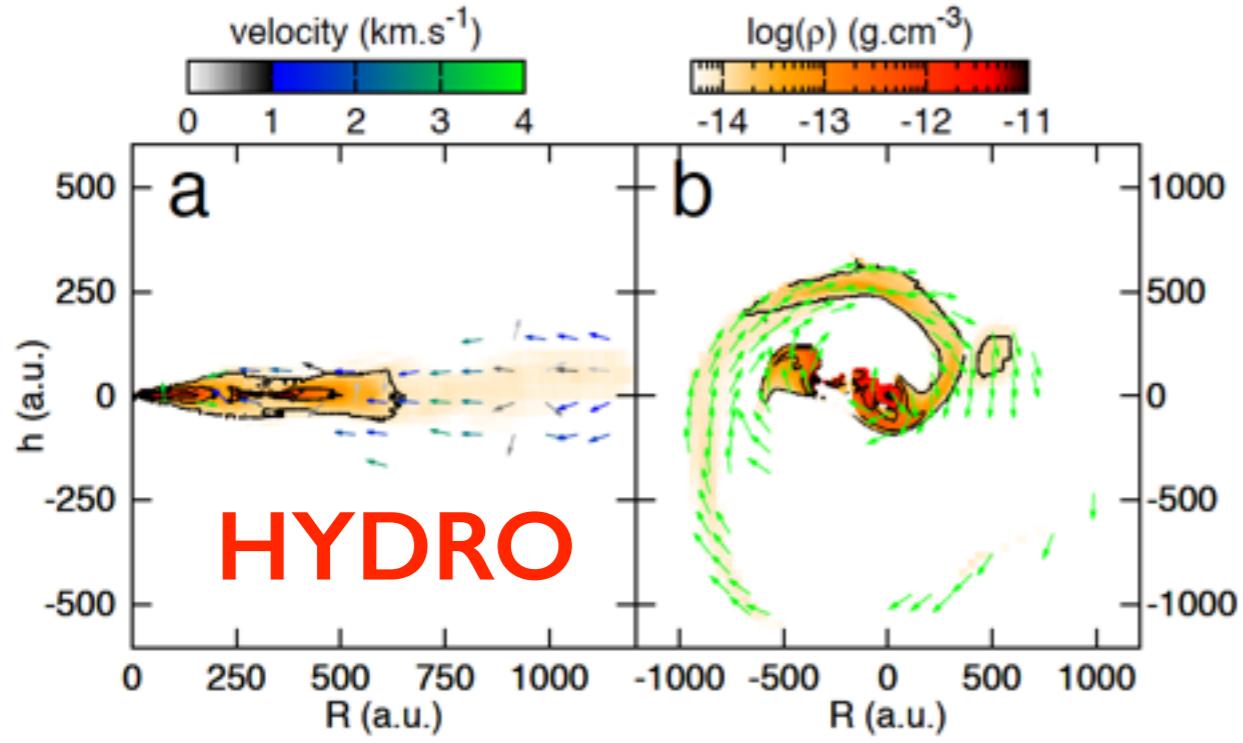
# Is radiative feedback important?



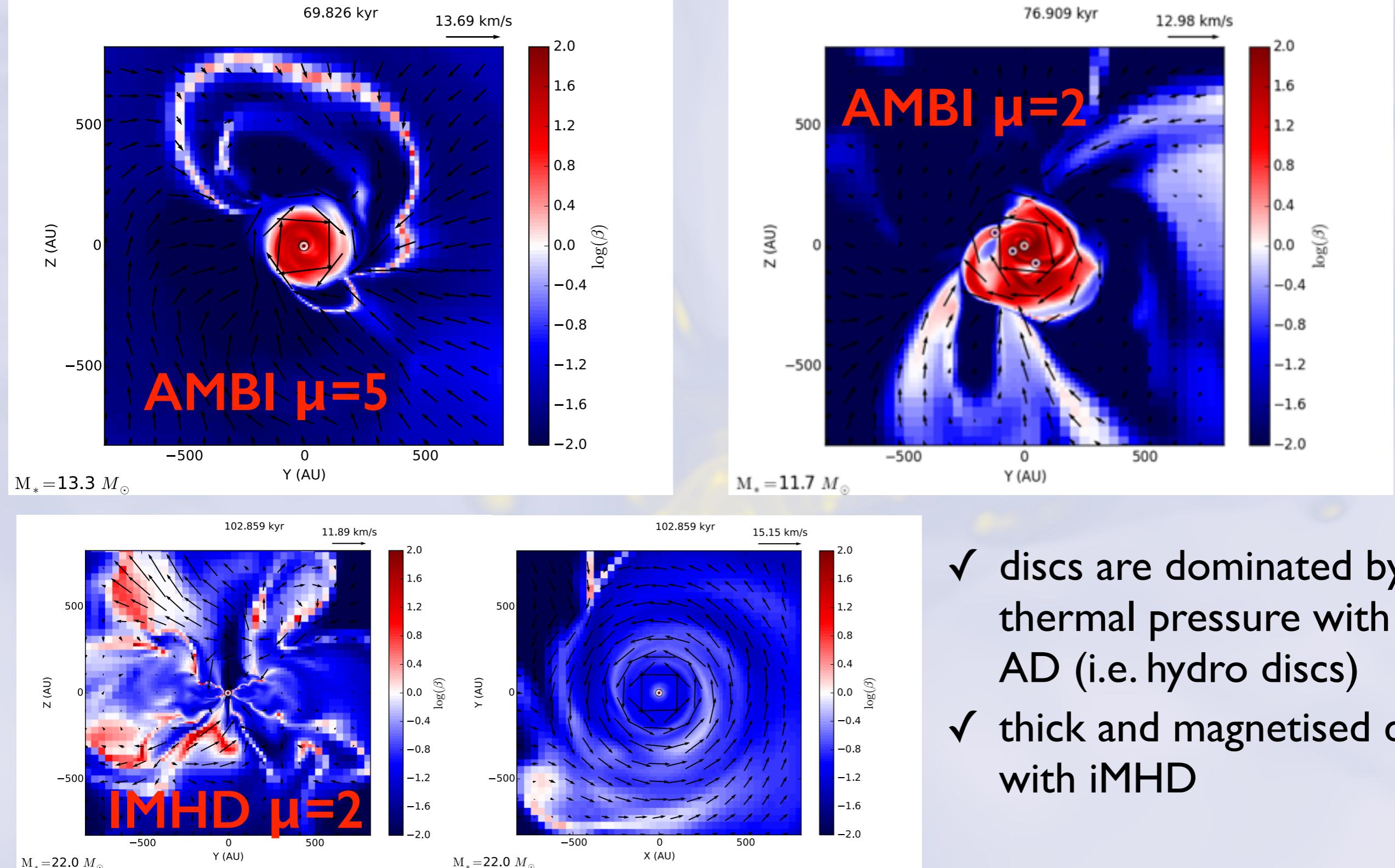
✓ radiative force contributes to the outflow, but does not dominate over the Lorentz force



# Discs properties

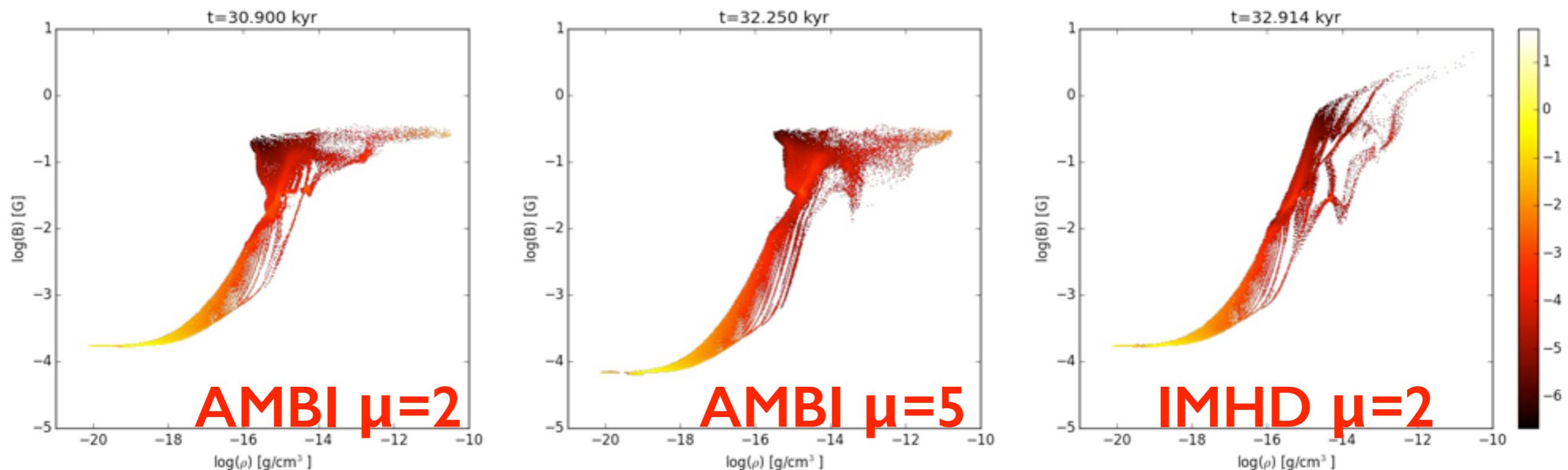


# Discs properties



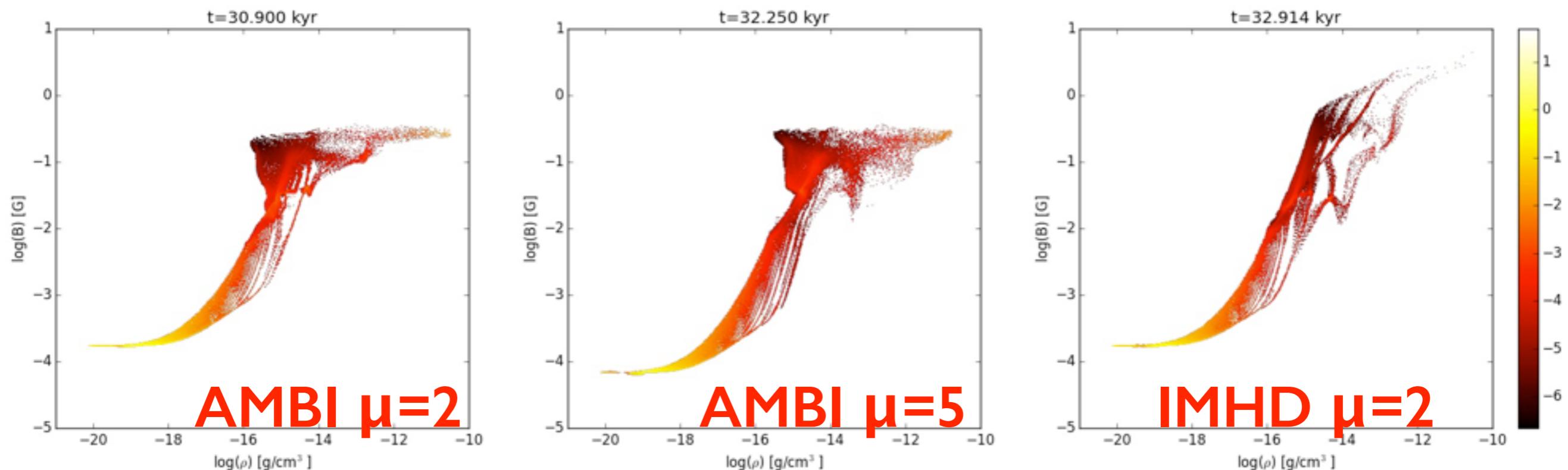
- ✓ discs are dominated by thermal pressure with AD (i.e. hydro discs)
- ✓ thick and magnetised disk with iMHD

# Magnetisation



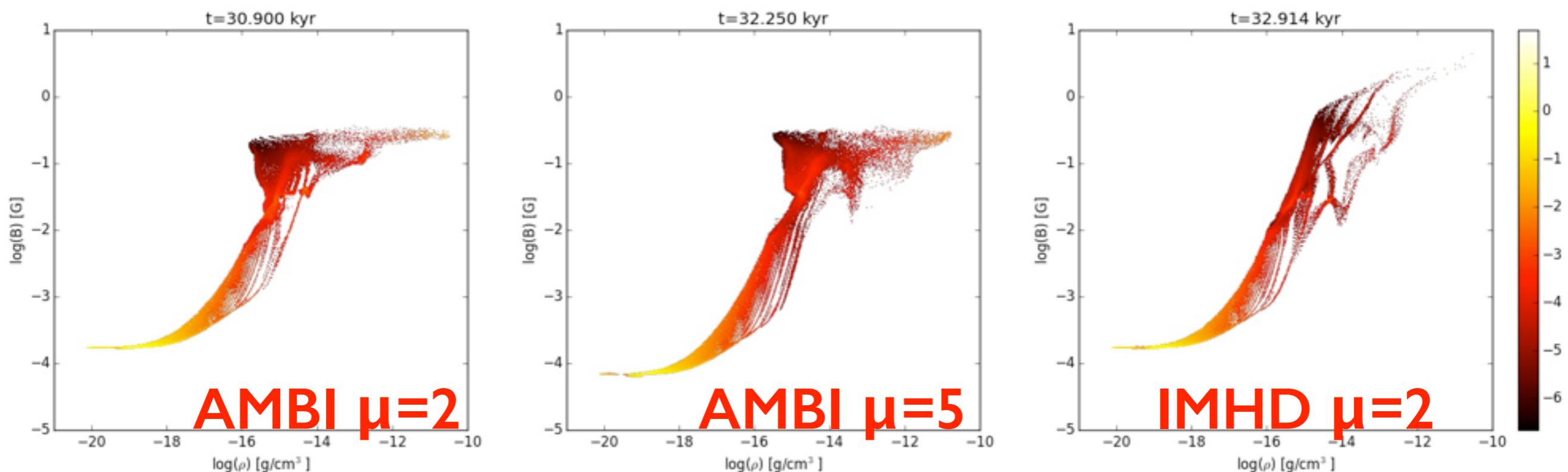
- ✓ Bmax reduced by > 1 order of magnitude by AD
- ✓ plateau @  $B < 1$  G
- ✓ similar to results found in  
low mass star formation

# Magnetisation

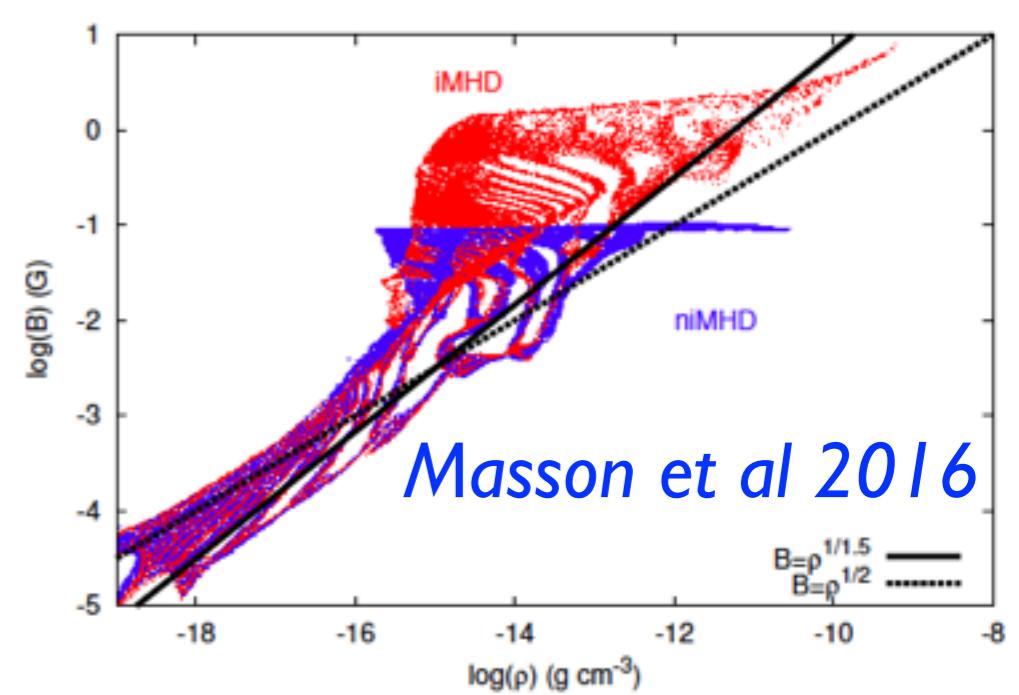


- ✓ Bmax reduced by > 1 order of magnitude by AD
- ✓ plateau @  $B < 1G$
- ✓ similar to results found in  
low mass star formation

# Magnetisation



- ✓  $B_{\max}$  reduced by  $> 1$  order of magnitude by AD
- ✓ plateau @  $B < 1 \text{ G}$
- ✓ similar to results found in low mass star formation



## Take away III

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- Outflow is primarily of magnetic origin
- Magnetic outflow extends up to 50 000 AU in massive cores
- Radiative force does not overtake with  $M_\star < 15 M_\odot$ , but contributes to acceleration
- No large disk -  $R < 500$  AU
- observational diagnostics
- ideal MHD and hydro models have **strong limitations** wrt
  1. outflow launching
  2. disk properties (as well as for low-mass star formation...)
  3. angular momentum transport

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**THANK YOU**